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Plasmon-enhanced polymer photovoltaic cells based on large aspect ratio gold nanorods and the related working mechanism

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Two types of Au nanorods (NRs) possessing longitudinal/transverse axes of 55/11 (NR₁₁) and 90/18 nm (NR₁₈) are, respectively, incorporated into the hole extraction layer to improve optical-to-electrical conversion performances in polymer photovoltaic cells. Totally different improvement factors in short-circuit current and power conversion efficiency occur in the NR₁₁- and NR₁₈-doped cells. Optical simulations, electrical analysis, and morphology alteration accompanying with the incorporation of NRs were proceeded to investigate the reason, and analysis demonstrates that a slower damping of field around NR₁₈ (results in a field and absorption enhancement around the active layer) and one order higher scattering cross section in the NR₁₈-incorporated cell are key factors contributed to the improvement of cell performances.

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Organic photovoltaic (OPV) cells are attracting many attentions due to their potential for low-cost, high-throughput processing. However, the excitonic bottleneck (exciton diffusion length of ~ 10 nm) in most organic polymers results in a tradeoff between light absorption and exciton harvesting efficiency in OPVs. Architectures used to overcome this problem have included bulk¹ and mixed² heterojunctions and the use of phosphorescent materials.³ While the bulk heterojunction blended architecture partially alleviates the problem of exciton dissociation in optically thick films, the internal quantum efficiency (IQE) in bulk heterojunction cells often decreases rapidly with increasing film thickness. This drop in IQE is particularly significant for many new low band gap, red, and near-IR absorbing materials because they typically have lower absorption coefficients.⁴ As an alternate approach, surface plasmons (SPs) have been exploited to improve the absorption efficiency. Ag and Au have dominated experimental researches in this area although other metals also support SPs. Up to now, there are many work exploring the influence of Au or Ag nanoparticles or nanostructures on OPV's performance by locating them into carrier extraction layer or active layer.^{5–11} Unfortunately, the photocurrent enhancement from spherical Ag or Au nanoparticles is usually restricted due to their localized surface plasmon resonance (LSPR) around 430 nm and 530 nm, respectively. Here, it should be mentioned that rod-like Ag and Au nanostructures are attractive candidates since their longitudinal plasmon absorption can be tuned from visible, NIR and to the infrared region by simply manipulating the aspect ratio (AR),¹²

providing a unique opportunity for utilizing the low energy range of the solar spectrum. In addition, Ag or Au nanorods (NRs) can be processed through wet chemical synthesis¹³ with the well-dispersion in a variety of aqueous/organic solutions and their size, shape, density can also be easily controlled.¹⁴ This approach of obtaining Ag or Au NRs present a less expensive choice compared with other methods, e.g., laser ablation,¹⁵ electron beam lithography,¹⁶ etc.

Although many researches on Au or Ag NR's synthesis methods and optical properties, theirs application in OPVs is rarely reported. Janković *et al.*¹⁷ incorporated octadecyltrimethoxysilane (OTMS)-functionalized Au/SiO₂ core/shell NRs into active layers in 2013. They found that the greatest enhancement in power conversion efficiency (PCE) was observed in spectral regions where the OPV polymer absorbs poorly. In their work, they did not further explore quantitatively the field distribution around Au NRs induced by LSPR and not consider the influence of scattering on PCE at all. Hsiao *et al.*¹⁸ first introduced series of Au nanospheres (NSs) with the LSPR peaks of 520, 530, and 540 nm and NRs with the longitudinal axis LSPR peaks of 660, 780, and 850 nm, covering from the visible to the NIR region, into OPVs to investigate the effects of the shape and size of Au NSs and NRs on optoelectrical performances in OPVs. By systematical analysis on film's extinction and photoluminescence (PL) spectra, they deduced that LSPR and light scattering, respectively, play an important and a minor role in the enhancement of OPV's performance, especially for Au NR780 (the LSPR peak of 780 nm). They also concluded that the integration of two kinds of Au NPs covering the whole absorption band-edge of the active layer is especially beneficial to the acquirement of a highest enhancement factor in OPVs, which is also powerfully proved recently by Lu *et al.* using Ag and

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FIG. 1. (a) J - V and (b) EQE curves of P3HT:PC₇₁BM devices without or with Au NRs. Inset is dark current characteristics and schematic structures for our OPV devices.

Au NSs with complementary absorption spectra.¹⁹ In Hsiao’s work,¹⁸ differences of shapes, sizes, aspect ratios, absorption spectral ranges for those Au NSs or NRs bring too many variable factors, making rigorous analysis on a certain factor very difficult.

In order to further explore the influences of Au NRs on the optoelectrical conversion performances in OPVs and their major working mechanism, two kinds of Au NR, namely, NR₁₁ and NR₁₈ with the same AR but different sizes ($55 \pm 5/11 \pm 3$ and $90 \pm 10/18 \pm 3$ nm for NR₁₁ and NR₁₈’s longitudinal/transverse axes) are used in this paper, where they generate the same LSPR wavelength in the NIR region (940 nm). Synthesis method of these NRs refers to Ref. 20. The NRs₁₁ and NRs₁₈ are, respectively, doped into the poly(3,4-ethylene dioxythiophene):poly(4-styrenesulfonate) (PEDOT:PSS) hole extraction layer to observe their influences on photovoltaic performances. Before use, the Au nanorods were centrifugated for about two times to remove reactants and stabilizing agents with the final concentration of $\sim 10^{17}$ particles/ml in aqueous solution. Each type of Au NR’s concentration is further optimized to acquire the best OPV performance (with structure in the inset of Figure 1). For NR₁₁, the optimized volume ratio of rods to PEDOT:PSS is around 30%, resulting in a short-circuit current density (J_{sc}) and a PCE of 7.76 mA/cm² and 3.17%, compared to 7.48 mA/cm² and 3.07% in a standard cell without NRs, as the curves shown in Figure 1(a) and the result summarized in Table I. While for NRs₁₈, the optimal concentration is $\sim 3\%$, and the corresponding J_{sc} and PCE exhibit enhancement factors of 12.2% and 12.7%, reaching 8.39 mA cm⁻² and 3.46%, respectively. Both the corresponding external quantum efficiency (EQE) curves with an optimal NRs₁₁ and NRs₁₈ doping concentration (Figure 1(b)) exhibit some improvements over a wide wavelength range of 400–650 nm compared to that in the standard device, while for NRs₁₈, the magnitude of improvement is more significant, consistent with as-measured J - V characteristics. For both of the two kinds of NRs, the fill factor (FF) shows a slightly increase when using a low doping concentration and then gradually declines as the doping concentration becomes optimal in the OPVs.

TABLE I. Summary of the photovoltaic parameters with and without NRs.

NR’s type	Rod concentration	V_{oc} (V)	J_{sc} (mA/cm ²)	FF	PCE (%)
	(v/v)				
W/O	0	0.600	7.48	0.684	3.07
NR ₁₁	30%	0.610	7.76	0.670	3.17
NR ₁₈	3%	0.610	8.39	0.676	3.46

Photocurrent density (J_{ph}) versus effective voltage (V_{eff}) characteristic curves have been calculated to observe photo-generated excitons.²¹ Here, J_{ph} is determined as $J_{ph} = J_L - J_D$, where J_L and J_D are the current density under illumination and in the dark, respectively. V_{eff} is determined as $V_{eff} = V_0 - V_a$, where V_0 is the voltage at which $J_{ph} = 0$ and V_a is the applied bias voltage. Figure 2 clearly shows that J_{ph} increases linearly at low V_{eff} values and saturates at a high V_{eff} (i.e., $V_{eff} > 0.6$ V). Assuming that all the photo-generated excitons are dissociated into free charge carriers and collected by electrodes afterward at a high V_{eff} region, saturation current density (J_{sat}) is then only limited by total amount of absorbed incident photons. G_{max} could be calculated from $J_{ph} = qG_{max}L$, where q is the electronic charge and L is the thickness of active layer (200 nm). The values of G_{max} for the control, NR₁₁- and NR₁₈-incorporated devices are $2.35 \times 10^{27} \text{ m}^{-3} \text{ s}^{-1}$ ($J_{sat} = 75.2 \text{ A/m}^2$), $2.45 \times 10^{27} \text{ m}^{-3} \text{ s}^{-1}$ ($J_{sat} = 78.3 \text{ A/m}^2$), and $2.56 \times 10^{27} \text{ m}^{-3} \text{ s}^{-1}$ ($J_{sat} = 82 \text{ A/m}^2$), respectively. Because the G_{max} value is only governed by the absorption of light,⁷ the enhanced values suggest that the incorporation of the Au NR₁₁ and NR₁₈ increases the degree of light harvesting in the devices, which is further testified with the significant enhancement in the absorption spectra (Figure 3(a)) for the multilayer films of PEDOT:PSS:NR₁₁ or NR₁₈/poly(3-hexylthiophene) (P3HT):[6, 6] phenyl C71-butyric acid methyl ester (PC₇₁BM) compared to the control PEDOT:PSS/P3HT:PC₇₁BM film around 300–650 nm. From Figure 3(a), we also observe that the enhanced magnitude from NR₁₈ is obviously higher than that from NR₁₁. To clearly explain this phenomenon, we simulate the absorption spectra of the NRs-doped PEDOT:PSS layer by using FDTD software. The calculation result shown in Figure 3(b) demonstrates that both Au NR₁₁ and NR₁₈ generate the same LSPR peaks with the longitudinal and

FIG. 2. Photocurrent density versus effective voltage for the OPVs with and without NRs.

FIG. 3. (a) and (c) are the measured absorption and PL spectra of the PEDOT:PSS:NR₁₁ or NR₁₈/P3HT:PC₇₁BM films and the control film without NRs, (b) and (d) are calculated absorption spectra (normalized) and scattering cross sections of Au NR₁₁ and NR₁₈. Inset of (a) and (b) are the enhancement factors of NRs' absorption and the calculated absolute absorption.

transverse axes peaks at 920 and 597 nm, respectively, but the absolute intensity from NR₁₈ is one order higher than that from NR₁₁, as shown in the inset of Figure 3(b), indicating a much stronger absorption ability from NR₁₈ and a larger local field intensity distribution around NR₁₈. From the simulation results of the field distribution around the NRs (Figure 4), one surprisingly observes that the largest electric field occurring at the surface of Au NR₁₈ is almost equal to that at the surface of Au NR₁₁ (excited with 597 nm, the resonance peak of transverse axis). Here, in order to obtain the above simulation results, it should be noted that we assumed that (1) the ideal distribution of NRs is in the layer center of the 50-nm thick PEDOT:PSS, (2) most of Au NRs lie but not stand in the PEDOT:PSS film, (3) x axis is along the longitudinal axis of Au NRs and z axis (the

incident direction of sun light is along with the backwards of z axis) is perpendicular to the PEDOT:PSS film, and (4) the periodic distribution of Au NRs is 200 nm × 200 nm. However, from careful comparison of the local field around NRs in Figure 4(c), we find that although the field quickly declines down to 1 for both NR₁₁ and NR₁₈ when far away from the surface of Au NR, the field intensity around NR₁₁ decreases more quickly than that around NR₁₈, with no more gain when the distance from the center of NR₁₁ is larger than 21 nm, indicating the active layer cannot absorb the additive energy generated by LSPR for a 50-nm thick PEDOT:PSS film if the NRs are mainly distributed in the center of the PEDOT:PSS film. In contrast, the field around NR₁₈ showing a slower damping can extend to 38 nm away from the center of the NR structure and maintain about 1.2 times of the

FIG. 4. The distribution of the electric field intensity around Au (a) NR₁₁ and (b) NR₁₈ along yz plane, and (c) is the comparison of the NR₁₁ and NR₁₈ electric field intensities along y axis under z = 0.

incident field intensity ($|E|^2$) even at the P3HT/PEDOT:PSS interface, thus resulting in the PL enhancement of the P3HT active layer considering of the overall increase in PL intensity proportional to $|1.2E|^2$ due to LSPR.²² This can be further proved with the measurement of the PL spectra for the PEDOT:PSS:NR₁₁ or NR₁₈/P3HT:PC₇₁BM films (Figure 3(c)). A slight enhancement for the PEDOT:PSS:NR₁₁/P3HT:PC₇₁BM film compared to the non-doped one in Figure 3(c) indicates the Au NRs are randomly distributed and not totally lied in the center of the PEDOT:PSS layer. From above measurement of the absorption and PL spectra and the simulation work on the local field around Au NRs, we can clearly explain the obvious J_{sc} and PCE improvement in the NR₁₈-doped OPVs.

Besides the magnified electric field generated by LSPR, the influence of scattering from Au NRs should be taken for granted to be considered. Our common sense tells us that a large-size NR, e.g., NR₁₈, will bring larger scattering intensity than the small one and result in lengthened light transport path, which further increases light absorption in OPV cells. The above idea has been identified by the simulated scattering cross section, as shown in Figure 3(d), from which one observes that the scattering cross section from NR₁₈ is one order higher than that from NR₁₁. As a conclusion, the OPVs doping NR₁₈ show a higher photon-to-electrical conversion performance due to both LSPR-induced field enhancement and the relatively large scattering cross section.

In addition to the absorbance and scattering enhancement in the NR₁₈-doped OPVs, other possible factors, such as the alteration of the hole extraction and transport ability induced by Au NRs₁₈ and the morphology changes of the PEDOT:PSS film by incorporating Au NRs, have been further investigated to observe their influences on solar cells. Hole- and electron-dominated single-carrier devices with the structures of ITO/PEDOT:PSS (~50 nm, with 3% or without Au NR₁₈)/Ag and ITO/LiF (1 nm)/PEDOT:PSS (~50 nm, with 3% or without Au NR₁₈)/Ca/Ag have been designed in order to observe the influence of NRs. The J - V curves (not shown here) indicate that the incorporation of Au NRs₁₈ brings no obvious alteration in injection and transport of the current, indicating a negligible influence of the shallow impurity energy level induced by Au on hole extraction and transport.²³

It has been suggested that a rough P3HT:PCBM surface creates defect sites that assist exciton dissociation.²⁴ Besides, increasing anode surface roughness will increase the interface area between the anode and the active layer, providing shorter routes for holes to travel to the anode and enhancing hole collection at the anode.²⁵ The increased interfacial area between PEDOT:PSS and P3HT:PCBM allows the collection of a larger number of holes in the P3HT:PCBM layer, thus increasing J_{sc} . Thus, the morphology changes of the PEDOT:PSS layer with 3% or with the absence of Au NRs₁₈ are measured by applying atomic force microscopy on the PEDOT:PSS or PEDOT:PSS:Au NRs₁₈ film. With introducing the Au NR₁₈, we observe a slight change in surface morphology of the rod-doped PEDOT:PSS film with an increase in surface roughness (R_a) from 1.53 to 1.63 nm. This result indicates that the doping of NRs₁₈ is beneficial to exciton

dissociation and the collection of a larger number of holes to some extent, resulting in the increase in J_{sc} , but we simultaneously infer that the roughness-induced increase in J_{sc} will not be significant due to a small alteration of R_a .

In conclusion, two types of Au NRs possessing longitudinal/transverse axes of 55/11 (NR₁₁) and 90/18 nm (NR₁₈) are, respectively, incorporated into PEDOT:PSS to improve the OPV performances. Totally different improvement factors in J_{sc} and PCE are obtained in the NR₁₁- and NR₁₈-doped cells, indicating the introduction of NR₁₁ and NR₁₈ into the PEDOT:PSS layer brings different influences on distribution and transport of light. To explore the origin of the improved performance, several characterizations including optical simulation, electrical transport performance, and film morphology have been investigated. Simulation results demonstrate that NR₁₈ generates a similar electric field intensity with NR₁₁ at the rods/PEDOT:PSS interface but a slower damping of field around NRs₁₈, which keeps an enhanced field when reaching the active layer in NR₁₈-doped cells. In addition, the scattering cross section from NR₁₈ is one order higher than that from NR₁₁. The incorporation of NRs₁₈ results in a slight increase in surface roughness of the PEDOT:PSS film, which is beneficial to exciton dissociation and the collection of a larger number of holes to some extent. Both the enhanced field intensity around rods and large scattering from NRs₁₈, together with a slight increase in surface roughness of the film contribute to the improved cell performances.

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