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2020

Lin, X., Liu, Z., Stauber, T., Gómez-Santos, G., Gao, F., Chen, H., . . . Low, T. (2020). Chiral plasmons with twisted atomic bilayers. *Physical Review Letters*, 125(7), 077401-.
doi:10.1103/PhysRevLett.125.077401

<https://hdl.handle.net/10356/145766>

<https://doi.org/10.1103/PhysRevLett.125.077401>

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Chiral Plasmons with Twisted Atomic Bilayers

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(Received 6 April 2020; accepted 14 July 2020; published 11 August 2020)

van der Waals heterostructures of atomically thin layers with rotational misalignments, such as twisted bilayer graphene, feature interesting structural moiré superlattices. Because of the quantum coupling between the twisted atomic layers, light-matter interaction is inherently chiral; as such, they provide a promising platform for chiral plasmons in the extreme nanoscale. However, while the interlayer quantum coupling can be significant, its influence on chiral plasmons still remains elusive. Here we present the general solutions from full Maxwell equations of chiral plasmons in twisted atomic bilayers, with the consideration of interlayer quantum coupling. We find twisted atomic bilayers have a direct correspondence to the chiral metasurface, which simultaneously possesses *chiral* and *magnetic* surface conductivities, besides the common *electric* surface conductivity. In other words, the interlayer quantum coupling in twisted van der Waals heterostructures may facilitate the construction of various (e.g., bi-anisotropic) atomically-thin metasurfaces. Moreover, the chiral surface conductivity, determined by the interlayer quantum coupling, determines the existence of chiral plasmons and leads to a unique phase relationship (i.e., $\pm\pi/2$ phase difference) between their transverse-electric (TE) and transverse-magnetic (TM) wave components. Importantly, such a unique phase relationship for chiral plasmons can be exploited to construct the missing *longitudinal* spin of plasmons, besides the common *transverse* spin of plasmons.

DOI: 10.1103/PhysRevLett.125.077401

Chiral materials [1–10], which have left- and right-handed counterparts connected by the mirror symmetry, are ubiquitous in nature. Generally, natural chiral materials have weak chiral light-matter interactions. The emerging field of chiral plasmonics [11–16] exploits strong light-matter interactions for chiral optical responses, including giant circular dichroism and optical activity. As such, it holds great promise for chiral optical spectroscopy with enhanced sensitivity. Chiral surface plasmons are thus of fundamental importance in physics [1,8–10,17], biology [13,18], stereochemistry [4,13], and drug development [13,15] for discriminating chiral molecules of different handedness.

van der Waals heterostructures with rotational misalignment [19–31] are a promising atomically thin platform for chiral plasmonics. The finite twist and interlayer coupling between the atomic bilayers imply all mirror symmetry is

broken, imparting the twisted van der Waals heterostructure with an inherent chirality [32–37]. Twisted van der Waals heterostructures also support the propagation of highly confined surface plasmons [38–47], thus providing an efficient way to strengthen chiral light-matter interactions in the extreme nanoscale [32–37]. Moreover, the active tunability of these atomic heterostructures is attractive for chiral plasmonics. First, the chemical potential of constituent two-dimensional (2D) materials [48] can be readily tuned, e.g., through electrostatic gating. As such, twisted van der Waals heterostructures can be an ideal platform for *active* chiral plasmonics [16]. Second, one can deterministically manipulate the interlayer twist angle, which dictates the electronic properties of van der Waals heterostructures [19–31], such as the recent discovery of superconducting and correlated insulating states in twisted bilayer graphene if the twist angle is close to the so-called “magic angle” [20–26].

Here we theoretically reveal the possibility to create the longitudinal spin of plasmons, in addition to their more well-known transverse spin, by exploiting the unique phase relationship (i.e., $\pm\pi/2$ phase difference) between the TE and TM wave components of chiral surface plasmons in twisted atomic bilayers. We highlight that while the longitudinal spin of photons and transverse spin of plasmons have been extensively studied [49–51], the transverse spin of photons was only recently reported [52], and the longitudinal spin of plasmons remains elusive. The longitudinal spin of plasmons might be of paramount importance to novel types of exotic spin-orbit interactions of light [50,53,54]. Moreover, we also show that stacked atomic bilayers with rotational misalignment can, in general, be effectively described by a chiral metasurface. The effective chiral metasurface simultaneously has chiral, magnetic, and electric surface conductivities, where the chiral surface conductivity is the key parameter that determines the existence of chiral plasmons and their unique phase relationship mentioned above, and its value depends on the interlayer quantum coupling. From a fundamental physical standpoint, the interlayer quantum coupling in twisted van der Waals heterostructures may facilitate the construction of various atomically thin metasurfaces, ranging from isotropic, anisotropic, bi-isotropic to bi-anisotropic. Our work therefore bridges the gap between two seemingly disparate but exciting fields, namely, metasurfaces and van der Waals heterostructures.

As a result of interlayer quantum coupling, their surface conductivity of twisted atomic bilayers can be expressed as a 4×4 matrix [34,35], namely,

$$\bar{\sigma}_s = \begin{bmatrix} \bar{\sigma}_0 & \bar{\sigma}_1 - i\sigma_{xy}\bar{\tau}_y \\ \bar{\sigma}_1 + i\sigma_{xy}\bar{\tau}_y & \bar{\sigma}_0 \end{bmatrix}, \quad (1)$$

where $\bar{\tau}_y$ is the 2×2 Pauli matrix; $\bar{\sigma}_0$, $\bar{\sigma}_1$, and σ_{xy} are the in-plane conductivity for each atomic layer, the covalent drag conductivity, and the Hall conductivity, respectively, which can be obtained, for example, via the continuum or tight-binding models [32–36]. Here, we restrict ourselves to the case where the atomic layer is isotropic; that is, $\bar{\sigma}_0 = \sigma_0 \bar{1}$ and $\bar{\sigma}_1 = \sigma_1 \bar{1}$ are diagonal. These conductivities, of course, depend on the twist angle θ [34,35]. In this work, we disregard any in-plane nonlocality. This is reasonable for cases where the wavelength of light or surface plasmons are much larger than the periodicity of moiré patterns. In other words, we restrict ourselves to the case where the interlayer twist angle is much larger than the magic angle. In order to consider the out-of-plane nonlocal response of twisted atomic bilayers [Fig. 1(a)], they should be separated by a nonzero distance a [34,35]. The interlayer quantum coupling or the out-of-plane nonlocal response is sensitive to a . For twisted bilayer graphene, $a \approx a_0$, where $a_0 = 0.35$ nm.

We now proceed to the discussion of electromagnetic boundary conditions for twisted atomic bilayers. The

FIG. 1. Simplified effective electromagnetic boundary conditions for twisted atomic bilayers. The twisted atomic bilayer is represented by twisted bilayer graphene. (a),(b) For twisted bilayer graphene, its interlayer distance a is comparable to $a_0 = 0.35$ nm. (a) Original boundary conditions with the out-of-plane nonlocal description. (b) Effective boundary conditions, where the twisted atomic bilayer is modeled by a chiral metasurface. (c),(d) For hypothetical twisted atomic bilayers, if their interlayer distance is relatively large, namely, $a \gg a_0$, the interlayer quantum coupling would disappear. Such hypothetical twisted atomic bilayers are equivalent to a nonchiral metasurface.

boundary conditions [55] at the two atomic layers [Fig. 1(a)] can be written as

$$\hat{n} \times (\bar{E}_{-}^{(1 \text{ or } 2)} - \bar{E}_{+}^{(1 \text{ or } 2)}) = 0, \quad (2)$$

$$\hat{n} \times (\bar{H}_{-}^{(1 \text{ or } 2)} - \bar{H}_{+}^{(1 \text{ or } 2)}) = \bar{J}_s^{(1 \text{ or } 2)} = \bar{\sigma}_s \begin{bmatrix} \bar{E}_{-}^{(1)} \\ \bar{E}_{+}^{(2)} \end{bmatrix}. \quad (3)$$

$\bar{E}_{\pm}^{(1 \text{ or } 2)}$ and $\bar{H}_{\pm}^{(1 \text{ or } 2)}$ stand for the components of electric and magnetic fields parallel to the interface [Fig. 1(a)], respectively. Their superscript 1 or 2 indicates whether the field is at the 1st and 2nd atomic layer, and their subscript – or + indicates whether the field is in the region above or below the corresponding interface. $\bar{J}_s^{(1 \text{ or } 2)}$ stands for the surface current. Equations (2)–(3) contain 8 coupled equations, since the off-diagonal terms of $\bar{\sigma}_s$ in Eq. (3) couples the fields of the two layers.

After some simplification, we find that the boundary conditions can be reorganized into a more intuitive way as follows [Fig. 1(b)]:

$$\hat{n} \times (\bar{E}_{-}^{(1)} - \bar{E}_{+}^{(2)}) = -\bar{\sigma}_m(\bar{H}_{-}^{(1)} + \bar{H}_{+}^{(2)}) + \bar{\sigma}_\chi(\bar{E}_{-}^{(1)} + \bar{E}_{+}^{(2)}), \quad (4)$$

$$\hat{n} \times (\bar{H}_{-}^{(1)} - \bar{H}_{+}^{(2)}) = +\bar{\sigma}_e(\bar{E}_{-}^{(1)} + \bar{E}_{+}^{(2)}) + \bar{\sigma}_\chi(\bar{H}_{-}^{(1)} + \bar{H}_{+}^{(2)}), \quad (5)$$

$$\bar{\bar{\sigma}}_m = \begin{bmatrix} \sigma_{m,x} & 0 \\ 0 & \sigma_{m,y} \end{bmatrix} = \begin{bmatrix} -\frac{f_{\text{TBG}}}{1-(\sigma_0-\sigma_1)f_{\text{TBG}}} & 0 \\ 0 & -\frac{f_{\text{TBG}}k_{z0}^2/k_0^2}{1-(\sigma_0-\sigma_1)f_{\text{TBG}}k_{z0}^2/k_0^2} \end{bmatrix}, \quad (6)$$

$$\bar{\bar{\sigma}}_\chi = \begin{bmatrix} \sigma_{\chi,x} & 0 \\ 0 & \sigma_{\chi,y} \end{bmatrix} = -\sigma_{xy}\bar{\bar{\sigma}}_m, \quad (7)$$

$$\bar{\bar{\sigma}}_e = \begin{bmatrix} \sigma_{e,x} & 0 \\ 0 & \sigma_{e,y} \end{bmatrix} = \begin{bmatrix} \sigma_0 + \sigma_1 - \sigma_{xy}^2\sigma_{m,x} - \frac{\epsilon_0}{\mu_0}f_{\text{TBG}} & 0 \\ 0 & \sigma_0 + \sigma_1 - \sigma_{xy}^2\sigma_{m,y} - \frac{\epsilon_0}{\mu_0}f_{\text{TBG}}\frac{k_{z0}^2}{k_0^2} \end{bmatrix}. \quad (8)$$

In these equations, the coefficient $f_{\text{TBG}} = (\omega\mu_0/k_{z0})(e^{ik_{z0}a/2} - e^{-ik_{z0}a/2}/e^{ik_{z0}a/2} + e^{-ik_{z0}a/2})$ originates from the electromagnetic response of the gap between the two atomic layers (i.e., region 3 in Fig. 1, which can be readily treated as free space), where $k_{z0} = \sqrt{k_0^2 - q^2}$, $k_0^2 = \omega^2\mu_0\epsilon_0$, μ_0 , and ϵ_0 are the permeability and permittivity of free space, respectively. Here we let the in-plane wave vector $\bar{q}$ be parallel to the $+\hat{x}$ direction, i.e., $\bar{q} = \hat{x}k_x$. There is a factor difference of (k_{z0}^2/k_0^2) between the x and y components of $\bar{\bar{\sigma}}_e$, $\bar{\bar{\sigma}}_m$, and $\bar{\bar{\sigma}}_\chi$ in Eqs. (6)–(8). Such a difference comes from the fact that we have $\hat{z}(\partial/\partial z) \times \hat{y}E_y = i\omega\mu_0\hat{x}H_x$ for TE (i.e., s -polarized) waves but $\hat{z}(\partial/\partial z) \times \hat{x}E_x = (k_{z0}^2/k_0^2)i\omega\mu_0\hat{y}H_y$ for TM (p -polarized) waves within the gap in Fig. 1.

Now the simplified effective boundary conditions in Eqs. (4) and (5) only contain 4 equations. To be specific, the effective boundary conditions [Fig. 1(b)] only relate to the fields outside the twisted bilayer (i.e., $|z| \geq a/2$). It is interesting to note that the effective boundary conditions satisfy the duality principle [55]. If we make the following replacements, namely, $\bar{E} \rightarrow \bar{H}$, $\bar{H} \rightarrow -\bar{E}$, $\bar{\bar{\sigma}}_m \rightarrow \bar{\bar{\sigma}}_e$, $\bar{\bar{\sigma}}_e \rightarrow \bar{\bar{\sigma}}_m$, and $\bar{\bar{\sigma}}_\chi \rightarrow \bar{\bar{\sigma}}_\chi$, Eq. (4) becomes Eq. (5), and Eq. (5) becomes Eq. (4).

The obtained expression for $\bar{\bar{\sigma}}_e$, $\bar{\bar{\sigma}}_m$, and $\bar{\bar{\sigma}}_\chi$ in Eqs. (4)–(8) holds for arbitrary propagation direction, since Eqs. (4)–(8) are obtained by defining the $+\hat{x}$ direction to be the direction of in-plane wave vector $\bar{q}$. Meanwhile, since we are considering atomic layers which are isotropic, $\bar{\bar{\sigma}}_e$, $\bar{\bar{\sigma}}_m$, and $\bar{\bar{\sigma}}_\chi$ are all 2×2 diagonal matrices. Moreover, due to the different electromagnetic responses of the twisted bilayer to different polarizations of light (i.e., TE and TM waves), we generally have $\sigma_{e,x} \neq \sigma_{e,y}$, $\sigma_{m,x} \neq \sigma_{m,y}$, and $\sigma_{\chi,x} \neq \sigma_{\chi,y}$. Such a situation also happens to an isotropic dielectric slab. To be specific, if there are no twisted atomic bilayers in Fig. 1, the thin isotropic dielectric slab (i.e., free space or region 3 in Fig. 1) has $\bar{\bar{\sigma}}_{m,\text{air}} = \begin{bmatrix} \sigma_{m,x,\text{air}} & 0 \\ 0 & \sigma_{m,y,\text{air}} \end{bmatrix}$, $\bar{\bar{\sigma}}_{e,\text{air}} = (\epsilon_0/\mu_0)\bar{\bar{\sigma}}_{m,\text{air}}$, and $\bar{\bar{\sigma}}_{\chi,\text{air}} = 0$, where $\sigma_{m,x,\text{air}} = -f_{\text{TBG}}$ and $\sigma_{m,y} = \sigma_{m,x,\text{air}}k_{z0}^2/k_0^2$. Accordingly, the effective boundary conditions in Eqs. (4) and (5) demonstrate that twisted atomic bilayers can be treated as

a 2D bi-isotropic chiral metasurface [Fig. 1(b)]. In contrast, we highlight that in the original boundary conditions in Eqs. (2) and (3), twisted atomic bilayers with the out-of-plane nonlocal response indeed shall be treated as a 3D material, due to its nonzero interlayer distance a . Without loss of generality, we denote $\bar{\bar{\sigma}}_e$, $\bar{\bar{\sigma}}_m$, and $\bar{\bar{\sigma}}_\chi$ in Eqs. (6)–(8) as the effective electric, magnetic, and chiral surface conductivities, respectively.

The dimensionless parameter $\bar{\bar{\sigma}}_\chi$ characterizes the magnetoelectric effect of the effective 2D chiral metasurfaces. Equation (7) shows that $\bar{\bar{\sigma}}_\chi$ depends on the Hall conductivity σ_{xy} . This way, the effective boundary conditions provide us a direct mapping of the interlayer quantum coupling of twisted atomic bilayers to the general constitutive parameters in Maxwell equations. If the interlayer distance for the two parallel atomic layers is relatively large [e.g., $a \gg a_0$ in Figs. 1(c) and 1(d)], the interlayer quantum coupling would diminish, which leads to $\sigma_{xy} = 0$ and thus $\bar{\bar{\sigma}}_\chi = 0$ from Eq. (7), even though the two atomic layers are rotationally misaligned. As such, our derived effective boundary conditions with $\bar{\bar{\sigma}}_\chi \neq 0$ are also an important extension of conventional boundary conditions with $\bar{\bar{\sigma}}_\chi = 0$ [55] for the electromagnetic wave theory itself.

We note that the forms of $\bar{\bar{\sigma}}_e$, $\bar{\bar{\sigma}}_m$, and $\bar{\bar{\sigma}}_\chi$, whose explicit expressions are given by Eqs. (4) and (5), were derived for the case of nonmagnetic and isotropic atomic bilayers. More general forms of $\bar{\bar{\sigma}}_e$, $\bar{\bar{\sigma}}_m$, and $\bar{\bar{\sigma}}_\chi$ can be realized by stacking other 2D atomic layers (e.g., in-plane anisotropic 2D materials, magnetic 2D materials) [28–30,48,56] or in conjunction with standard metasurface approaches such as nanopatterning [57–59]. With this in mind, below we explore surface plasmons governed by the effective boundary conditions in Eqs. (4) and (5), where $\bar{\bar{\sigma}}_e$, $\bar{\bar{\sigma}}_m$, and $\bar{\bar{\sigma}}_\chi$ are taken to be arbitrary values. For conceptual demonstration, we assume the bi-isotropic metasurface to be located inside a symmetric dielectric environment. That is, regions 1 and 2 [Figs. 1(a) and 1(b)] have a relative permittivity of $\epsilon_{1r} = \epsilon_{2r} = \epsilon_r > 0$.

For arbitrary values of $\bar{\bar{\sigma}}_\chi$, $\bar{\bar{\sigma}}_e$, and $\bar{\bar{\sigma}}_m$, the dispersions of surface plasmons is governed by

$$\frac{k_z^2}{\omega^2 \mu_0 \epsilon_0 \epsilon_r} \sigma_{\chi,x}^2 + \left(1 + \frac{k_z}{\epsilon_r} \frac{\sigma_{e,x}}{\omega \epsilon_0}\right) \left(1 + k_z \frac{\sigma_{m,x}}{\omega \mu_0}\right) = 0, \quad (9)$$

$$\sigma_{\chi,y}^2 + \left(\frac{k_z}{\omega \mu_0} + \sigma_{e,y}\right) \left(\frac{k_z}{\omega \epsilon_0} + \sigma_{m,y}\right) = 0, \quad (10)$$

where $k_z = \sqrt{\omega^2 \mu_0 \epsilon_0 \epsilon_r - q^2}$ is the component of wave vector perpendicular to the interface. Generally, the existence of surface plasmons including those in Eqs. (9) and (10) requires a nonzero carrier density at the Fermi level. It is useful to point out that there are also recent studies about exotic plasmons in systems with vanishing density of states at the Fermi level [60–64]. As a typical example, the enhanced interband correlation due to the band inversion with the Mexican-hat dispersion can give rise to plasmon excitations at zero temperature in the context of topological insulators such as V- or Cr-doped (Bi, Sb)₂Te₃ [64].

If $\bar{\sigma}_\chi = 0$, Eqs. (9) and (10) represent the dispersion for linearly polarized surface plasmons. Moreover, if $\text{Im}(\sigma_{e,x}) > 0$ [48] or $\text{Im}(\sigma_{m,y}) < 0$ in Eqs. (9) and (10), TM surface plasmons exist. Similarly, if $\text{Im}(\sigma_{e,y}) < 0$ [65] or $\text{Im}(\sigma_{m,x}) > 0$, TE surface plasmons can appear.

If $\bar{\sigma}_\chi \neq 0$, Eqs. (9) and (10) stand for the dispersion for chiral plasmons. Because of the magnetoelectric effect, these chiral plasmons are intrinsically hybrid TE-TM waves. As such, chiral plasmons with $\bar{\sigma}_\chi \neq 0$ are distinctly different from the linearly polarized surface plasmons with $\bar{\sigma}_\chi = 0$. On the other hand, the chiral plasmons in Eqs. (9) and (10) are reciprocal. They are different from the nonreciprocal chiral edge plasmons recently reported in a wide range of 2D metallic systems including gapped Dirac materials [66–68].

Particularly, if $\bar{\sigma}_e = 0$ and $\bar{\sigma}_m = 0$ in Eqs. (9) and (10), the dispersion of the two eigenmodes of chiral plasmons is reduced to

$$\frac{k_z^2}{\omega^2 \mu_0 \epsilon_0 \epsilon_r} \sigma_{\chi,x}^2 + 1 = 0, \quad (11)$$

$$\frac{k_z^2}{\omega^2 \mu_0 \epsilon_0 \epsilon_r} + \sigma_{\chi,y}^2 = 0. \quad (12)$$

Figure 2 shows the basic features of these chiral plasmons governed by Eqs. (11) and (12), including their dispersion (namely, the relation between q and $\sigma_{\chi,x}^2$ or $\sigma_{\chi,y}^2$) in Fig. 2(a) and their field distribution in Figs. 2(b) and 2(c). Figure 2(a) shows that we have $q/(\omega/c) \gg 1$ for one chiral eigenmode in Eq. (11) if $\sigma_{\chi,x} \rightarrow 0$, while we have $q/(\omega/c) \rightarrow 1$ for the other chiral eigenmode in Eq. (12) if $\sigma_{\chi,y} \rightarrow 0$. For the chiral eigenmodes in Eq. (11), Fig. 2(b) shows that their field distributions of both $H_z(\bar{r})$ and $E_z(\bar{r})$ are odd symmetric with respect to the interface (namely, the plane of $z = 0$). It is then straightforward to denote these modes in Eq. (11) as the chiral odd eigenmodes of surface

FIG. 2. Chiral surface plasmons supported by the chiral surface conductivity $\bar{\sigma}_\chi$. Here the chiral metasurface has $\bar{\sigma}_\chi \neq 0$, $\bar{\sigma}_m = 0$, and $\bar{\sigma}_e = 0$, and it is located at $z = 0$ in free space. (a) In-plane wave vector q of chiral surface plasmons as a function of $\sigma_{\chi,x}^2$ or $\sigma_{\chi,y}^2$. (b),(c) Field distribution of chiral surface plasmons at (b) $\sigma_{\chi,x} = +1$ and (c) $\sigma_{\chi,y} = +1$. Here the plasmonic wavelength λ_{spp} is equal to $2\pi/q$.

plasmons. Similarly, the modes in Eq. (12) are denoted as the chiral even eigenmodes of surface plasmons, since their field distribution of both $H_z(\bar{r})$ and $E_z(\bar{r})$ are even symmetric with respect to the interface [Fig. 2(c)].

Moreover, we find in Figs. 2(b) and 2(c) and Fig. S1 in the Supplemental Material [69] that there is a unique phase relationship between the TE and TM field components for chiral plasmons. The phase difference between the TE and TM field components, namely, $\text{Arg}[H_z(\bar{r})/E_z(\bar{r})]$, is dependent on the sign of $\sigma_{\chi,x}$ and $\sigma_{\chi,y}$. To be specific, we have $\text{Arg}\{[H_z(\bar{r})]/[E_z(\bar{r})]\} = -(\pi/2)\text{sgn}(\sigma_{\chi,y})$ for chiral even eigenmodes but $\text{Arg}\{[H_z(\bar{r})]/[E_z(\bar{r})]\} = +(\pi/2)\text{sgn}(\sigma_{\chi,x})$ for chiral odd eigenmodes.

Such unique phase relationships in chiral surface plasmons can be adopted to emulate the *longitudinal* spin of plasmons in Figs. 3(a) and 3(b), in addition to the common *transverse* spin of plasmons in Fig. 3(c) [49–51]. For the chiral surface plasmons in Fig. 2 in the $z < 0$ region, they have the electric field $\bar{E}_{1,\sigma_{\chi,y}} \propto \{\hat{x}(k_{z0}/k_0) + \hat{y}(-i)\text{sgn}(\sigma_{\chi,y}) + \hat{z}(k_x/k_0)\}e^{ik_x x - ik_{z0} z}$ for the eigenmodes related to $\sigma_{\chi,y}$, where $k_{z0} = i\text{Im}(k_{z0})$. Similarly, they have the electric field $\bar{E}_{1,\sigma_{\chi,x}} \propto [\hat{x}(k_{z0}/k_0) + \hat{y}(+i)\text{sgn}(\sigma_{\chi,x}) + \hat{z}(k_x/k_0)]e^{ik_x x - ik_{z0} z}$ for the eigenmode related to $\sigma_{\chi,x}$. Then the electric-field ellipticity $\varphi_E = \text{Im}(\bar{E}^* \times \bar{E})$ (or spin [70,71]) both in the $\hat{x}$ and $\hat{y}$ directions would not vanish for chiral surface plasmons, and its gradient would locally produce the spin energy flow [51]. In other words, the cycloidal rotation of electric fields in the y - z plane would

FIG. 3. Longitudinal spin in chiral surface plasmons. The surface plasmons propagate along the $+\hat{x}$ direction and decay exponentially away from the interface. The right-side panels show the instantaneous distribution of electric fields in the $z < 0$ region. (a),(b) Chiral surface plasmons. The structural setup in (a) and (b) are the same as Figs. 2(c) and 2(b), respectively. The cycloidal rotation of electric fields in the y - z plane generates the longitudinal spin $\bar{S}_x$ (parallel to $\bar{q} = \hat{x}k_x$), while the cycloidal rotation of electric fields in the x - z plane generates the transverse spin $\bar{S}_y$ (perpendicular to $\bar{q}$). (c) For comparison, we show the linearly polarized surface plasmons in (c), whose electric fields rotate only in the x - z plane and possess only the transverse spin.

generate the longitudinal spin $\bar{S}_x$ (parallel to $\bar{q}$), while the cycloidal rotation of electric fields in the x - z plane would generate the transverse spin $\bar{S}_y$ (perpendicular to $\bar{q}$), as shown in Figs. 3(a) and 3(b). Moreover, if $|(k_{z0}/k_0)| \ll 1$ (e.g., chiral surface plasmons with $|\sigma_{xy}| \ll 1$ in Fig. 2), we would have the cycloidal rotation of electric fields mainly in the y - z plane, inducing the almost pure longitudinal spin of plasmons. In contrast, if $|(k_{z0}/k_0)| \gg 1$ (e.g., chiral surface plasmons with $|\sigma_{xy}| \gg 1$ in Fig. 2), the cycloidal rotation of electric fields happens mainly in the x - z plane, giving rise to the almost pure transverse spin of plasmons; see also the pure transverse spin for linearly polarized plasmons in Fig. 3(c).

Regarding the twisted bilayer whose constituent atomic layers are isotropic and nonmagnetic, we generally have $\bar{\sigma}_x \neq 0$, $\bar{\sigma}_y \neq 0$, and $\bar{\sigma}_m \neq 0$. Then, their supported chiral plasmons have the dispersion governed by Eqs. (9) and (10). As a typical example, we show in Fig. 4 the dispersion of chiral plasmons for the case when the twisted atomic bilayers have $\sigma_0 = \sigma_1 = 0$ and $\sigma_{xy} \neq 0$. Under these specific conditions and if $\varepsilon_r = 1$, Eqs. (9) and (10) can be further reduced into the following simple form,

$$[t^{+1/2} + t^{-1/2}]^2 - \frac{\mu_0}{\varepsilon_0} \sigma_{xy}^2 = 0, \quad (13)$$

FIG. 4. Chiral surface plasmons supported by the twisted atomic bilayers. Here the frequency is 100 THz.

where $t = (-k_{z0}/\omega\mu_0)f_{\text{TBG}}$. Since $|t^{+1/2} + t^{-1/2}| \geq 2$, there is a critical existence condition for these chiral plasmons governed by Eq. (13), namely, $|\sigma_{xy}| \geq 4\varepsilon_0/\mu_0$. The in-plane wave vector of these chiral plasmons would go to infinity (i.e., extreme spatial confinement) if $|\sigma_{xy}|$ approaches to $\sqrt{4\varepsilon_0/\mu_0}$, and it would decrease to ω/c (poor spatial confinement) if $|\sigma_{xy}| \gg \sqrt{4\varepsilon_0/\mu_0}$, as shown in Fig. 4.

In addition, for realistic twisted atomic bilayers, σ_0 , σ_1 , σ_{xy} in Eq. (1) are generally complex numbers and have a nonzero real part, which characterizes the material loss and determines the propagation loss (or the lifetime) of chiral plasmons. A study of these plasmon damping mechanisms is beyond the scope of this work. However, the chiral plasmons such as the chiral even modes in Fig. 2 are most prominent for wave vectors of order to the free space wave vector ω/c . Hence, the chiral plasmons generally reside outside of the single particle excitation regime. Rather, due to the small wave vector, these plasmons are very weakly confined in the surrounding environment, and proper photonic engineering via cavity design might be necessary for future experimental observation.

In summary, we theoretically investigate basic features of chiral plasmons that can emerge in van der Waals heterostructures comprised of twisted atomic bilayers. As a unique emerging feature of chiral plasmons, we find that they possess the longitudinal spin of plasmons, besides to the common transverse spin of plasmons. The revealed longitudinal spin of plasmons may enable many other exotic spin-orbit interactions of light [49–54]. We have also directly mapped twisted atomic bilayers to the chiral metasurface, which simultaneously possesses the chiral, magnetic, and electric surface conductivities. Correspondingly, the derived effective boundary conditions for twisted atomic bilayers can further deepen our understanding of the influence of interlayer quantum coupling on

the chiral optical and plasmonic response. Meanwhile, the effective boundary conditions can enable a more intuitive and simplified way to treat light scattering problems in the new class of twisted atomic bilayers. Our work further indicates that chiral light-matter interactions in the extreme nanoscale can be efficiently tailored via the interlayer quantum coupling or the interlayer twisting. Considering a large library of atomically thin 2D materials, twisted van der Waals heterostructures can provide a fundamental building block to engineer various atomically-thin and actively tunable metasurfaces and/or metamaterials with their electromagnetic response ranging from isotropic, anisotropic, bi-isotropic to bi-anisotropic [55,72]. As such, twisted van der Waals heterostructures can also offer a fertile frontier for exploring the emerging field of chiral plasmonics.

This work was sponsored by NSF/EFRI-1741660 the Singapore Ministry of Education [Grants No. MOE2018-T2-1-022(S), No. MOE2016-T3-1-006], Spain's MINECO under Grants No. FIS2017-82260-P, No. PGC2018-096955-B-C42, No. CEX2018-000805-M as well as by the CSIC Research Platform on Quantum Technologies PTI-001, and Germany's Deutsche Forschungsgemeinschaft (DFG) via SFB 1277. This work at Zhejiang University was sponsored by the National Natural Science Foundation of China (NNSFC) under Grants No. 61801426, No. 61625502, No. 11961141010, and No. 61975176, the Top-Notch Young Talents Program of China, the Zhejiang Provincial Natural Science Foundation under Grants No. Z20F010018, and the Fundamental Research Funds for the Central Universities.

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- [1] J. B. Pendry, A chiral route to negative refraction, *Science* **306**, 1353 (2004).
- [2] A. V. Rogacheva, V. A. Fedotov, A. S. Schwanecke, and N. I. Zheludev, Giant Gyrotropy due to Electromagnetic-Field Coupling in a Bilayered Chiral Structure, *Phys. Rev. Lett.* **97**, 177401 (2006).
- [3] J. K. Gansell, M. Thiel, M. S. Rill, M. Decker, K. Bade, V. Saile, G. von Freymann, S. Linden, and M. Wegener, Gold helix photonic metamaterial as broadband circular polarizer, *Science* **325**, 1513 (2009).
- [4] N. Liu, H. Liu, S. Zhu, and H. Giessen, Stereometamaterials, *Nat. Photonics* **3**, 157 (2009).
- [5] Y. Zhao, M. A. Belkin, and A. Alù, Twisted optical metamaterials for planarized ultrathin broadband circular polarizers, *Nat. Commun.* **3**, 870 (2012).
- [6] S. Zhang, J. Zhou, Y. Park, J. Rho, R. Singh, S. Nam, A. K. Azad, H. Chen, X. Yin, A. J. Taylor, and X. Zhang, Photoinduced handedness switching in terahertz chiral metamolecules, *Nat. Commun.* **3**, 942 (2012).
- [7] J. Yeom, B. Yeom, H. Chan, K. W. Smith, S. Dominguez-Medina, J. H. Bahng, G. Zhao, W. Chang, S. Chang, A. Chuvilin, D. Melnikau, A. L. Rogach, P. Zhang, S. Link, P. Král, and N. A. Kotov, Chiral templating of self-assembling nanostructures by circularly polarized light, *Nat. Mater.* **14**, 66 (2015).
- [8] G. Hu, X. Hong, K. Wang, J. Wu, H. Xu, W. Zhao, W. Liu, S. Zhang, F. Garcia-Vidal, B. Wang, P. Lu, and C. Qiu, Coherent steering of nonlinear chiral valley photons with a synthetic Au-WS₂ metasurface, *Nat. Photonics* **13**, 467 (2019).
- [9] H. Jia, R. Zhang, W. Gao, Q. Guo, B. Yang, J. Hu, Y. Bi, Y. Xiang, C. Liu, and S. Zhang, Observation of chiral zero mode in inhomogeneous three-dimensional Weyl metamaterials, *Science* **363**, 148 (2019).
- [10] D. Ayuso, O. Neufeld, A. F. Ordóñez, P. Decleva, G. Lerner, O. Cohen, M. Ivanov, and O. Smirnova, Synthetic chiral light for efficient control of chiral light-matter interaction, *Nat. Photonics* **13**, 866 (2019).
- [11] A. Kuzyk, R. Schreiber, Z. Fan, G. Pardatscher, E. Roller, A. Högele, F. C. Simmel, A. O. Govorov, and T. Liedl, DNA-based self-assembly of chiral plasmonic nanostructures with tailored optical response, *Nature (London)* **483**, 311 (2012).
- [12] B. Yeom, H. Zhang, H. Zhang, J. I. Park, K. Kim, A. O. Govorov, and N. A. Kotov, Chiral plasmonic nanostructures on achiral nanopillars, *Nano Lett.* **13**, 5277 (2013).
- [13] M. Hentschel, M. Schäferling, X. Duan, H. Giessen, and N. Liu, Chiral plasmonics, *Sci. Adv.* **3**, e1602735 (2017).
- [14] H. Lee, H. Ahn, J. Mun, Y. Y. Lee, M. Kim, N. H. Cho, K. Chang, W. S. Kim, J. Rho, and K. T. Nam, Amino-acid- and peptide-directed synthesis of chiral plasmonic gold nanoparticles, *Nature (London)* **556**, 360 (2018).
- [15] Q. Zhang, T. Hernandez, K. W. Smith, S. A. Hosseini Jebeli, A. X. Dai, L. Warning, R. Baiyasi, L. A. McCarthy, H. Guo, D. Chen, J. A. Dionne, C. F. Landes, and S. Link, Unraveling the origin of chirality from plasmonic nanoparticle-protein complexes, *Science* **365**, 1475 (2019).
- [16] X. Yin, M. Schäferling, A. U. Michel, A. Tittl, M. Wuttig, T. Taubner, and H. Giessen, Active chiral plasmonics, *Nano Lett.* **15**, 4255 (2015).
- [17] B. Göhler, V. Hamelbeck, T. Z. Markus, M. Kettner, G. F. Hanne, Z. Vager, R. Naaman, and H. Zacharias, Spin selectivity in electron transmission through self-assembled monolayers of double-stranded DNA, *Science* **331**, 894 (2011).
- [18] L. Lin, S. Lepeshov, A. Krasnok, T. Jiang, X. Peng, B. A. Korgel, A. Alù, and Y. Zheng, All-optical reconfigurable chiral meta-molecules, *Mater. Today* **25**, 10 (2019).
- [19] R. Bistritzer and A. H. MacDonald, Moiré bands in twisted double-layer graphene, *Proc. Natl. Acad. Sci. U.S.A.* **108**, 12233 (2011).
- [20] Y. Cao, V. Fatemi, A. Demir, S. Fang, S. L. Tomarken, J. Y. Luo, J. D. Sanchez-Yamagishi, K. Watanabe, T. Taniguchi, E. Kaxiras, R. C. Ashoori, and P. Jarillo-Herrero, Correlated insulator behaviour at half-filling in magic-angle graphene superlattices, *Nature (London)* **556**, 80 (2018).
- [21] Y. Cao, V. Fatemi, S. Fang, K. Watanabe, T. Taniguchi, E. Kaxiras, and P. Jarillo-Herrero, Unconventional superconductivity in magic-angle graphene superlattices, *Nature (London)* **556**, 43 (2018).
- [22] Y. Choi, J. Kemmer, Y. Peng, A. Thomson, H. Arora, R. Polski, Y. Zhang, H. Ren, J. Alicea, G. Refael, F. von Oppen,

- K. Watanabe, T. Taniguchi, and S. Nadj-Perge, Electronic correlations in twisted bilayer graphene near the magic angle, *Nat. Phys.* **15**, 1174 (2019).
- [23] Y. Jiang, X. Lai, K. Watanabe, T. Taniguchi, K. Haule, J. Mao, and E. Y. Andrei, Charge order and broken rotational symmetry in magic-angle twisted bilayer graphene, *Nature (London)* **573**, 91 (2019).
- [24] A. Kerelsky, L. J. McGilly, D. M. Kennes, L. Xian, M. Yankowitz, S. Chen, K. Watanabe, T. Taniguchi, J. Hone, C. Dean, A. Rubio, and A. N. Pasupathy, Maximized electron interactions at the magic angle in twisted bilayer graphene, *Nature (London)* **572**, 95 (2019).
- [25] Y. Xie, B. Lian, B. Jäck, X. Liu, C. Chiu, K. Watanabe, T. Taniguchi, B. A. Bernevig, and A. Yazdani, Spectroscopic signatures of many-body correlations in magic-angle twisted bilayer graphene, *Nature (London)* **572**, 101 (2019).
- [26] A. L. Sharpe, E. J. Fox, A. W. Barnard, J. Finney, K. Watanabe, T. Taniguchi, M. A. Kastner, and D. Goldhaber-Gordon, Emergent ferromagnetism near three-quarters filling in twisted bilayer graphene, *Science* **365**, 605 (2019).
- [27] H. Yoo, R. Engelke, S. Carr, S. Fang, K. Zhang, P. Cazeaux, S. H. Sung, R. Hovden, A. W. Tsen, T. Taniguchi, K. Watanabe, G. Yi, M. Kim, M. Luskin, E. B. Tadmor, E. Kaxiras, and P. Kim, Atomic and electronic reconstruction at the van der Waals interface in twisted bilayer graphene, *Nat. Mater.* **18**, 448 (2019).
- [28] C. R. Dean, L. Wang, P. Maher, C. Forsythe, F. Ghahari, Y. Gao, J. Katoch, M. Ishigami, P. Moon, M. Koshino, T. Taniguchi, K. Watanabe, K. L. Shepard, J. Hone, and P. Kim, Hofstadter's butterfly and the fractal quantum Hall effect in moiré superlattices, *Nature (London)* **497**, 598 (2013).
- [29] J. Kunstmann, F. Mooshammer, P. Nagler, A. Chaves, F. Stein, N. Paradiso, G. Plechinger, C. Strunk, C. Schüller, G. Seifert, D. R. Reichman, and T. Korn, Momentum-space indirect interlayer excitons in transition-metal dichalcogenide van der Waals heterostructures, *Nat. Phys.* **14**, 801 (2018).
- [30] K. Tran *et al.*, Evidence for moiré excitons in van der Waals heterostructures, *Nature (London)* **567**, 71 (2019).
- [31] G. Chen, L. Jiang, S. Wu, B. Lyu, H. Li, B. L. Chittari, K. Watanabe, T. Taniguchi, Z. Shi, J. Jung, Y. Zhang, and F. Wang, Evidence of a gate-tunable Mott insulator in a trilayer graphene moiré superlattice, *Nat. Phys.* **15**, 237 (2019).
- [32] C. J. Tabert and E. J. Nicol, Optical conductivity of twisted bilayer graphene, *Phys. Rev. B* **87**, 121402 (R) (2013).
- [33] C. Kim, A. Sánchez-Castillo, Z. Ziegler, Y. Ogawa, C. Noguez, and J. Park, Chiral atomically thin films, *Nat. Nanotechnol.* **11**, 520 (2016).
- [34] T. Stauber, T. Low, and G. Gómez-Santos, Chiral Response of Twisted Bilayer Graphene, *Phys. Rev. Lett.* **120**, 046801 (2018).
- [35] T. Stauber, T. Low, and G. Gómez-Santos, Linear response of twisted bilayer graphene: Continuum versus tight-binding models, *Phys. Rev. B* **98**, 195414 (2018).
- [36] Z. Addison, J. Park, and E. J. Mele, Twist, slip, and circular dichroism in bilayer graphene, *Phys. Rev. B* **100**, 125418 (2019).
- [37] E. Suárez Morell, L. Chico, and L. Brey, Twisting dirac fermions: Circular dichroism in bilayer graphene, *2D Mater.* **4**, 035015 (2017).
- [38] G. X. Ni, H. Wang, J. S. Wu, Z. Fei, M. D. Goldflam, F. Keilmann, B. Özyilmaz, A. H. Castro Neto, X. M. Xie, M. M. Fogler, and D. N. Basov, Plasmons in graphene moiré superlattices, *Nat. Mater.* **14**, 1217 (2015).
- [39] F. Hu, S. R. Das, Y. Luan, T.-F. Chung, Y. P. Chen, and Z. Fei, Real-space imaging of the tailored plasmons in twisted bilayer graphene, *Phys. Rev. Lett.* **119**, 247402 (2017).
- [40] N. C. H. Hesp, I. Torre, D. Rodan-Legrain, P. Novelli, Y. Cao, S. Carr, S. Fang, P. Stepanov, D. Barcons-Ruiz, H. Herzig-Sheinfux, K. Watanabe, T. Taniguchi, D. K. Efetov, E. Kaxiras, P. Jarillo-Herrero, M. Polini, and F. H. L. Koppens, Collective excitations in twisted bilayer graphene close to the magic angle, [arXiv:1910.07893](https://arxiv.org/abs/1910.07893).
- [41] S. S. Sunku, G. X. Ni, B. Y. Jiang, H. Yoo, A. Sternbach, A. S. McLeod, T. Stauber, L. Xiong, T. Taniguchi, K. Watanabe, P. Kim, M. M. Fogler, and D. N. Basov, Photonic crystals for nano-light in moiré graphene superlattices, *Science* **363**, 1153 (2019).
- [42] T. Stauber and H. Kohler, Quasi-flat plasmonic bands in twisted bilayer graphene, *Nano Lett.* **16**, 6844 (2016).
- [43] C. Lewandowski and L. Levitov, Intrinsically undamped plasmon modes in narrow electron bands, *Proc. Natl. Acad. Sci. U.S.A.* **116**, 20869 (2019).
- [44] G. Sharma, M. Trushin, O. P. Sushkov, G. Vignale, and S. Adam, Superconductivity from collective excitations in magic angle twisted bilayer graphene, *Phys. Rev. Research* **2**, 022040 (2020).
- [45] G. Catarina, B. Amorim, Eduardo V. Castro, J. M. Viana Parente Lopes, and N. M. R. Peres, Twisted bilayer graphene: low-energy physics, electronic and optical properties, [arXiv:1908.01556](https://arxiv.org/abs/1908.01556).
- [46] H. Ochoa and A. Asenjo-Garcia, Flat Bands and Chiral Optical Response of Moiré Insulators, *Phys. Rev. Lett.* **125**, 037402 (2020).
- [47] P. Novelli, I. Torre, F. H. L. Koppens, F. Taddei, and M. Polini, Optical and plasmonic properties of twisted bilayer graphene: Impact of interlayer tunneling asymmetry and ground-state charge inhomogeneity, [arXiv:2005.09529](https://arxiv.org/abs/2005.09529).
- [48] T. Low, A. Chaves, J. D. Caldwell, A. Kumar, N. X. Fang, P. Avouris, T. F. Heinz, F. Guinea, L. Martin-Moreno, and F. Koppens, Polaritons in layered two-dimensional materials, *Nat. Mater.* **16**, 182 (2017).
- [49] K. Y. Bliokh, D. Smirnova, and F. Nori, Quantum spin Hall effect of light, *Science* **348**, 1448 (2015).
- [50] K. Y. Bliokh, F. J. Rodríguez-Fortuño, F. Nori, and A. V. Zayats, Spin-orbit interactions of light, *Nat. Photonics* **9**, 796 (2015).
- [51] K. Y. Bliokh and F. Nori, Transverse spin of a surface polariton, *Phys. Rev. A* **85**, 061801(R) (2012).
- [52] L. Peng, L. Duan, K. Wang, F. Gao, L. Zhang, G. Wang, Y. Yang, H. Chen, and S. Zhang, Transverse photon spin of bulk electromagnetic waves in bianisotropic media, *Nat. Photonics* **13**, 878 (2019).
- [53] X. Shi, X. Lin, I. Kaminer, F. Gao, Z. Yang, J. D. Joannopoulos, M. Soljačić, and B. Zhang, Superlight inverse Doppler effect, *Nat. Phys.* **14**, 1001 (2018).
- [54] X. Lin and B. Zhang, Normal Doppler frequency shift in negative refractive-index systems, *Laser Photonics Rev.* **13**, 1900081 (2019).

- [55] J. A. Kong, *Electromagnetic Wave Theory* (EMW Publishing, Cambridge, Massachusetts, USA, 2008).
- [56] T. Low, R. Roldán, H. Wang, F. Xia, P. Avouris, L. M. Moreno, and F. Guinea, Plasmons and Screening in Monolayer and Multilayer Black Phosphorus, *Phys. Rev. Lett.* **113**, 106802 (2014).
- [57] Y. Li, Y. Xu, M. Jiang, B. Li, T. Han, C. Chi, F. Lin, B. Shen, X. Zhu, L. Lai, and Z. Fang, Self-Learning Perfect Optical Chirality via a Deep Neural Network, *Phys. Rev. Lett.* **123**, 213902 (2019).
- [58] W. Ma, F. Cheng, and Y. Liu, Deep-learning enabled on-demand design of chiral metamaterials, *ACS Nano* **12**, 6326 (2018).
- [59] Y. Fan, N. Shen, F. Zhang, Q. Zhao, Z. Wei, P. Zhang, J. Dong, Q. Fu, H. Li, and C. M. Soukoulis, Photoexcited graphene metasurfaces: Significantly enhanced and tunable magnetic resonances, *ACS Photonics* **5**, 1612 (2018).
- [60] T. V. Shahbazyan and M. E. Raikh, Surface plasmon in a two-dimensional Anderson insulator with interactions, *Phys. Rev. B* **53**, 7299 (1996).
- [61] S. Gangadharaiah, A. M. Farid, and E. G. Mishchenko, Charge Response Function and a Novel Plasmon Mode in Graphene, *Phys. Rev. Lett.* **100**, 166802 (2008).
- [62] S. Juergens, P. Michetti, and B. Trauzettel, Plasmons due to the Interplay of Dirac and Schrödinger Fermions, *Phys. Rev. Lett.* **112**, 076804 (2014).
- [63] J. Zhou, H.-R. Chang, and D. Xiao, Plasmon mode as a detection of the chiral anomaly in Weyl semimetals, *Phys. Rev. B* **91**, 035114 (2015).
- [64] F. Zhang, J. Zhou, D. Xiao, and Y. Yao, Tunable Intrinsic Plasmons due to Band Inversion in Topological Materials, *Phys. Rev. Lett.* **119**, 266804 (2017).
- [65] S. A. Mikhailov and K. Ziegler, New Electromagnetic Mode in Graphene, *Phys. Rev. Lett.* **99**, 016803 (2007).
- [66] J. C. W. Song and M. S. Rudner, Chiral plasmons without magnetic field, *Proc. Natl. Acad. Sci. U.S.A.* **113**, 4658 (2016).
- [67] A. Kumar, A. Nemilentsau, K. H. Fung, G. Hanson, N. X. Fang, and T. Low, Chiral plasmon in gapped Dirac systems, *Phys. Rev. B* **93**, 041413(R) (2016).
- [68] S. S.-L. Zhang and G. Vignale, Chiral surface and edge plasmons in ferromagnetic conductors, *Phys. Rev. B* **97**, 224408 (2018).
- [69] See Supplemental Material at <http://link.aps.org/supplemental/10.1103/PhysRevLett.125.077401> for more discussion on the boundary conditions for twisted atomic bilayers and about the dispersion of chiral plasmons on the bi-isotropic chiral metasurface (e.g., twisted bilayer graphene).
- [70] C. Sayrin, C. Junge, R. Mitsch, B. Albrecht, D. O'Shea, P. Schneeweiss, J. Volz, and A. Rauschenbeutel, Nanophotonic Optical Isolator Controlled by the Internal State of Cold Atoms, *Phys. Rev. X* **5**, 041036 (2015).
- [71] D. L. Andrews and M. Babiker, *The Angular Momentum of Light* (Cambridge University Press, Cambridge, England, 2012).
- [72] W. Dorrell, H. Pirie, S. M. Gardezi, N. C. Drucker, and J. E. Hoffman, van der Waals metamaterials, *Phys. Rev. B* **101**, 121103(R) (2020).