Mechanics of materials characterization of lead-free solders

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2005

Xiong, B. S. (2005). Mechanics of materials characterization of lead-free solders. Doctoral thesis, Nanyang Technological University, Singapore.

<https://hdl.handle.net/10356/5423>

<https://doi.org/10.32657/10356/5423>

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Mechanics of Materials Characterization of Lead-Free Solders

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A thesis submitted to the Nanyang Technological University
in fulfillment of the requirement for the degree of
Doctor of Philosophy

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ABSTRACT

Lead-free solders will replace tin-lead solders in electronic products due to European Union laws to restrict the use of toxic materials like lead (Pb) in electronic equipment by July 1st, 2006. Legislation to ban the use of lead (Pb) is forcing the electronic industry to use lead-free solders. Solder interconnections serve as electrical connections and also as the mechanical support to hold the IC component in position on the printed circuit board (PCB). It is important to characterize the mechanical properties of lead-free solders. NEMI (National Electronic Manufacturing Initiative) recommends Sn-3.9Ag-0.6Cu($\pm 0.2\%$) for reflow soldering process and Sn-0.7Cu solder alloy for wave soldering. The scope of this study includes the two NEMI recommended Pb-free solder alloys, namely Sn-3.8Ag-0.7Cu and Sn-0.7Cu. A mechanics of materials characterization of the elastic-plastic-creep properties and low cycle fatigue behavior is reported. A new visco-plastic constitutive model and fatigue model is presented and used to model the thermal fatigue behavior of a Micro-BGA assembly.

A systematic mechanics of materials study of Sn-3.8Ag-0.7Cu and Sn-0.7Cu lead-free solders is reported in this thesis. Firstly, tensile tests at four different temperatures (-40°C , 25°C , 75°C and 125°C), and at each temperature, three different strain rates (5.6×10^{-4} , 5.6×10^{-3} and 5.6×10^{-2}) were conducted to study the temperature and strain rate effect on tensile properties of Sn-3.8Ag-0.7Cu and Sn-0.7Cu solder alloys. Empirical equations for temperature and strain rate dependent elastic modulus, yield stress and UTS were developed. Visco-plastic constitutive models for both lead-free solders were also presented.

Secondly, creep tests were conducted at four different temperatures (-40°C , 25°C , 75°C and 125°C), and at each temperature, several different stress levels were tested to study the effect of temperature and stress level on the steady state creep strain rate behavior. Creep constitutive models were developed for Sn-3.8Ag-0.7Cu and Sn-0.7Cu.

Thirdly, low cycle fatigue tests were conducted at three different temperatures (25°C , 75°C and 125°C), and at each temperature, different strain range and frequencies were tested to study the effect of temperature and frequency on the fatigue behavior. Both strain-based and energy-based low cycle fatigue life prediction models were developed.

Fourthly, new research contributions have been achieved in the following areas,

- (a) A new visco-plastic constitutive model was developed. The new model can accurately simulate strain-stress response with temperature, strain rate and hardening-softening effects.
- (b) A new fatigue model was developed, which makes the fatigue lives at different temperatures and frequencies have a master curve with the load drop rate.
- (c) Impact tests at three different strain rates (7×10^2 , 9×10^2 and $1.3 \times 10^3 \text{ s}^{-1}$) were conducted to study the strain rate effect on impact properties of lead-free solder alloys at room temperature. Yield stress equations over a wide strain rate range (from 10^{-4} to 10^3 s^{-1}) were developed based on impact test results.

Finally, micro-deformation analysis of a Micro-BGA assembly with Sn-3.8Ag-0.7Cu was investigated using in-situ Digital Image Correlation (DIC) measurement. FEA simulation based on the new visco-plastic model was investigated. The measured test data compared well with the FEA results.

Acknowledgement

The author would like to acknowledge and express his sincere appreciation and gratitude to the following people:

A/P Pang Hock Lye, John, the project supervisor, for his invaluable advice and constant encouragement during this project.

Dr. Zhang Xueren, Dr. Liu Qingjun, Dr. Kithva Prakash Hariram, Mr. Mao Xiaohai and Mr. Low Tse Hoong, for their helpful discussion.

All technicians in the Strength of Materials Lab for providing technical support.

Finally, the author would like to express his gratitude to his parents, for their support and encouragement.

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NOMENCLATURE

Sn	Tin
Ag	Silver
Cu	Copper
Pb	Lead
SMT	Surface mount technology
EPA	Environmental Protection Agency
NEMI	National Electronic Manufacturing Initiative
PCB	Printed circuit board
DFR	Design for reliability
FEA	Finite element analysis
WLCSP	Wafer-level chip-scale package
UTS	Ultimate tensile strength
SHPB	Split Hopkinson pressure bar
BGA	Ball grid array
DISC	Digital image speckle correlation
$\frac{d\Phi}{dN}$	Load drop rate
T_m	Melting temperature (K)
σ	Normal stress (MPa)
ϵ_{ij}	Total normal strain
ϵ_{ij}^e	Elastic normal strain
ϵ_{ij}^p	Plastic normal strain
ϵ_{ij}^c	Creep normal strain
γ	Shear strain
τ	Shear stress (MPa)
E	Elastic modulus (GPa)
G	Shear modulus (GPa)
$d\epsilon_{in}/dt$	Inelastic strain rate
Q	Activation energy
R	Universal gas constant
b	Burgers vector
k	Boltzmann's constant (J/K)
d	Grain size
D_0	Diffusion constant
T	Absolute temperature (K)
ΔH_{GB}	Activation energy for grain boundary,
ΔH_{MC}	Activation energy for matrix creep
Q_c	Activation energy for the core-diffusion
Q_l	Activation energy for lattice-diffusion
$\Delta\epsilon_p$	Plastic strain range

g	Equilibrium or back stress
c	Fatigue exponent
ϵ'_f	Fatigue ductility coefficient
N_f	Fatigue life
σ'_f	Fatigue strength coefficient
b	Fatigue strength exponent
$\Delta\gamma_{mc}$	Strain range due to matrix creep
TSOP	Thin small outline package
N_p	Number of cycles to failure due to plastic fatigue
N_c	Number of cycles to failure due to the creep fatigue
SRP	Strain range partitioning method
f	Frequency (Hz)
$\Delta\overline{W}_{total}$	Total strain energy (J)
ν	Poisson's ratio
J	J integral
LCF	Low cycle fatigue
ASTM	American society for testing and materials
σ_{dr}	Dynamic recovery parameter
σ_{ss}	Saturation stress
$h'(\epsilon)$	Strain hardening function
ϵ_i	Initial strain
σ_{h-s}	Hardening-softening parameter
TEC	Thermoelectric coolers
DNP	Displacement from neutral point

Chapter 1. Introduction

Electronic packaging is a challenging research area due to the introduction of new materials, development of packaging design, minimization of structures, and many challenges driven by technological, environmental and economic considerations. For electronic products, reliable fatigue design is required for long-term reliability, especially when dealing with lead-free solder materials, where constitutive models and fatigue analysis are needed.

1.1 Background

Interest in advanced solder alloys arises from the increase use of surface mount technology (SMT) in electronic assemblies. Surface mount technology was developed to overcome the limitations of pin-through-hole (PTH) assembly technology. SMT can achieve more Input/Output (I/Os) and lower volumes compared to PTH technology. Development of surface mount devices moves from SMT-peripheral (such as QFP) to SMT- Area Array (such as BGA), and onto chip scale packaging (CSP) due to industry tends to minimize package size and increase solder joint I/Os. Hence, the electronics industry focused their attention on research and development of solder based manufacturing technologies [1]. In Singapore, the electronics sector is one of the most important industries and the production of high-quality and reliable electronic products are dependent on the advances in electronic packaging technology. As this industry advances, the demand in manufacturing efficiency, increased device

function and reliability is expected. Solder joint reliability research for lead-free solder alloys is urgently needed as the industry will have to adjust to lead-free electronic manufacturing in the coming years.

1.2 Lead-Free Solder

Tin-lead solders are the primary materials used for interconnecting electronic components for many reasons, such as low cost, good soldering properties, known metallurgical and fatigue resistance properties. However, lead (Pb) in solders has been cited by the Environmental Protection Agency (EPA) in the USA as one of the materials posing a health and environment problem. Untreated or inadequately treated water containing lead from waste dumping is a major health concern. The European Commission introduced two legislations, WEEE (Waste Electrical and Electronic Equipment) and ROHS (Reduction of Hazardous Substances) to minimize the risks and impact that the production, use, treatment and disposal of waste electrical and electronic equipment has on human health and the environment. The European Parliament has approved the ban on hazardous substances including lead (Pb) to take effect on July 1st, 2006.

The main substitutes for traditional tin-lead (Sn-Pb) solders are Sn-Ag-Cu, Sn-Cu, and Sn-Ag lead-free solder alloys [2-3]. The National Electronic Manufacturing Initiative (NEMI) recommends using Sn-3.9Ag-0.6Cu($\pm 0.2\%$) solder for reflow soldering and Sn-0.7Cu solder alloy for wave soldering [4]. Tin-lead solders have been studied for more than 40 years, while research on lead-free or Pb-free solders is

active in recent years. Mechanics of materials characterization of lead-free solders are needed for understanding and developing reliable SMT assemblies with lead-free solders.

1.3 Reliability Problem of Soldered Assemblies

In SMT soldered assemblies, solder joints provide electrical connections and function as structural members to join the IC components to the printed circuit boards (PCBs). That means the solder alloys serve not only as an interconnect material for electrical connections but also as the mechanical support to hold the component in position on the PCBs. The assemblies contain materials with different coefficients of thermal expansion and generate high cyclic strain in the solder joints when subjected to cyclic thermal loading. The thermal loadings may be caused by either changes in the external temperature or internal heat generation and dissipation by operating devices. The temperature fluctuation may be large, for example, from -55°C to 125°C for automotive electronic components; or small, for computers in climate-controlled environment. Even small temperature fluctuations can have a large effect, depending upon the size of the package and solder joint, and the difference in the thermal expansion of the materials.

The majority of current reliability test methodologies are based on empirical analysis of reliability test data [5]. That means, the solder joints on an actual product are exposed to conditions of accelerated thermo-mechanical fatigue, the lifetime prediction will be extrapolated based on the accelerated fatigue data. Such test

methods for thermal cycling are time consuming and expensive to use for extensive parametric studies. In order to study the reliability problem of solder in SMT assemblies more fundamentally, a fatigue life prediction method employing a Design For Reliability (DFR) approach is needed. The schematic illustration of the DFR methodology is shown in Fig. 1-1. The stress-strain relationship and creep properties highlighted in the figure must be obtained from tensile and creep tests and expressed as mechanics models in Finite Element Analysis (FEA) to calculate the plastic strain range or strain energy density in the solder material. These failure parameters can then be used in fatigue models, which are developed based on low cycle fatigue tests of solder alloys, to predict the fatigue life of solder joints.

Fig. 1-1 Schematic illustration of Design for Reliability Methodology

1.4 Objective of the Study

The objective of this study is to characterize the mechanical properties of two lead-free solder alloys (Sn-3.8Ag-0.7Cu and Sn-0.7Cu) and develop new constitutive and fatigue models for these lead-free solder alloys. Mechanics of materials characterization of the elastic-plastic-creep properties and low cycle fatigue behavior were investigated. A new visco-plastic constitutive model was developed and applied to FEA simulation of a Micro-BGA assembly subjected to thermal loading. A new load-drop fatigue model was developed to improve on the existing low cycle fatigue analysis of solder materials.

The specific research objectives are:

- (i) Develop temperature and strain rate dependent tensile properties and stress-strain relations for Pb-free solders.
- (ii) Develop creep constitutive model for Pb-free solders.
- (iii) Develop low cycle fatigue model for Pb-free solders, study the effects of temperature and frequency.
- (iv) Develop new visco-plastic constitutive model for Pb-free solders.
- (v) Develop new fatigue model based on a load-drop parameter.
- (vi) Application of developed constitutive models to a Micro-BGA packaging assembly subject to thermal loading.

1.5 Dissertation Outline

The dissertation is organized into nine chapters. The structure of each chapter is summarized in the following.

Chapter one introduces the need for mechanics of materials research of lead-free solders.

Chapter two review and categorize the published constitutive and fatigue models of solder alloys.

Chapter three introduces the experimental procedure in this study. The specimen geometry, test machine and test conditions for tensile, impact, creep and fatigue tests are described.

Chapter four investigates the mechanical properties at different temperature and strain rate for the two lead-free solders (Sn-3.8Ag-0.7Cu and Sn-0.7Cu), and the data were compared with other reported results. The apparent elastic modulus, yield stress and ultimate tensile strength (UTS) will be presented as function of temperature and strain rate. The test data were applied to the Anand visco-plastic model for both lead-free solders.

Chapter five studies the creep behavior at different temperature and stress level for the two lead-free solders (Sn-3.8Ag-0.7Cu and Sn-0.7Cu). The creep data are compared with other reported results. The steady state creep strain rate of lead-free solders is characterized by the established hyperbolic sine creep model.

Chapter six studies the low cycle fatigue behavior for the two lead-free solders (Sn-3.8Ag-0.7Cu and Sn-0.7Cu), and the fatigue data are compared with other

reported results. The fatigue test results for the two lead-free solders are described by low cycle fatigue models, where temperature and frequency dependent constants were determined. Frequency-modified low cycle fatigue models are developed to characterize the fatigue behavior of the lead-free solders over wide range of frequencies.

Chapter seven focus on new research contributions for Sn-3.8Ag-0.7Cu solder. Firstly, a new visco-plastic constitutive model is formulated and applied to model the tensile test results and shows good agreement. Secondly, a new fatigue parameter (load drop rate, $\frac{d\Phi}{dN}$) is introduced to overcome the difficulties encountered in conventional low cycle fatigue models employed earlier. Thirdly, high strain rate impact tests on Sn-3.8Ag-0.7Cu lead-free solder are investigated. The yield stress equation over a wide range of strain rate (from 10^{-4} to 10^3) is developed.

Chapter eight applies the developed models in Finite Element Analysis (FEA) to simulate a Micro-BGA assembly with Sn-3.8Ag-0.7Cu lead-free solder subject to thermal loading. The thermal loading was applied to Micro-BGA assembly from 25°C to 125°C. In-situ measurement is conducted by a Micro-DISC (Digital Image Speckle Correlation) system. The displacement and strain field of the solder joint at 75°C and 125°C were measured. The results from the in-situ measurements are compared to the FEA results. The FEA simulation employed the new constitutive visco-plastic model. A subroutine code was programmed and integrated into the ANSYS finite element analysis software. The comparison between the in-situ measurement strain and FEA simulated strain are made.

Chapter nine concludes with the key results, contributions made and suggestions for future research study.

Chapter 2. Literature Review

Solder materials are usually subjected to thermo-mechanical loadings at the high operating temperatures, 0.5 to 0.8 times T_m of the alloy, and deformation induced are non-linear and consist of plastic and creep effects. The stress, strain or strain energy density during the thermal-mechanical loading will not be directly measured or controlled in the field situation. However, these quantities are quite important for fatigue life prediction and estimated by calculations or simulations. Therefore, the constitutive models to calculate these quantities are the basis of the solder fatigue life prediction methodology. In this chapter, constitutive and fatigue models for solder alloys will be reviewed.

2.1 Constitutive Models

Due to the low melting temperature, solders have complex mechanical phenomena, both the time-independent plastic strain and time-dependent creep strain are significant parts of the solder deformation. The published constitutive models for solder alloys behavior can be categorized into elastic-plastic-creep approach and visco-plastic approach.

2.1.1 Elastic-plastic-creep approach

Elastic-plastic-creep approach treats the total strain as the sum of the phenomenological components of elastic strain, time independent plastic strain and time dependent creep strain as shown below,

$$\varepsilon_{ij} = \varepsilon_{ij}^e + \varepsilon_{ij}^p + \varepsilon_{ij}^c \quad (2.1.1)$$

where ε_{ij} , ε_{ij}^e , ε_{ij}^p and ε_{ij}^c are total, elastic, time-independent plastic and time-dependent creep strain tensors, respectively. The formation of elastic and plastic strain is the same for all models. While the formulation for creep strain differs depending on the creep mechanism model used as shown in Fig. 2-1. Depending on temperature and applied stress, dislocation glide, dislocation recovery, Nabarro-Herring creep and dislocation glide-climb mechanisms may be the dominant creep deformation mechanism. At low temperature and high stress level, dislocation glide is the dominant mechanism; however, at high temperature and low stress level, Nabarro-Herring creep mechanism occurs by diffusional mass transport will dominate the creep deformation.

Fig. 2-1 Schematic of deformation mechanism map

Some of the creep and plastic strain forms will be discussed in the following parts:

Knecht and Fox [6] proposed a constitutive relation based on total shear strain rate.

For time dependent creep strain rate, the Integrated Matrix Creep (IMC) model was introduced, accounts for the effects of equivalent grain boundary creep and the equivalent matrix creep by utilizing a creep strain rate equation in the form of two power laws:

$$\dot{\gamma}_{cr} = C_1 \exp\left(\frac{-\Delta H_{GB}}{kT}\right) \tau^{n_{GB}} + C_2 \exp\left(\frac{-\Delta H_{MC}}{kT}\right) \tau^{n_{MC}} \quad (2.1.2a)$$

where C_1 and C_2 are material constants, ΔH_{GB} is the activation energy for grain boundary, ΔH_{MC} is the activation energy for matrix creep, k is Boltzmann's constant, T is absolute temperature, τ is the shear stress, n_{GB} and n_{MC} are grain boundary creep

and matrix creep exponents, respectively. The time-independent elastic and plastic strain part is,

$$\gamma_{e+p} = \frac{\tau}{G} + \left(\frac{\tau}{\tau_p} \right)^n \quad (2.1.2b)$$

where γ_{e+p} is the time-independent elastic and creep strain, G is the shear modulus and τ_p is plasticity parameter.

Darveaux [7] proposed a model based on inelastic strain, which neglected the time independent elastic strain, shown in the following equations below.

$$\varepsilon_{in} = \varepsilon_c + \varepsilon_p \quad (2.1.3a)$$

$$\varepsilon_c = \frac{d\varepsilon_s}{dt}t + \varepsilon_T \left(1 - \exp \left(-B \frac{d\varepsilon_s}{dt} \right) \right) \quad (2.1.3b)$$

$$\varepsilon_p = C_p \left(\frac{\sigma}{G} \right)^{m_p} \quad (2.1.3c)$$

where ε_c and ε_p are the creep and plastic strain, respectively. For creep strain, Darveaux included the transient creep strain (ε_T) in the model. The transient creep strain will occur immediately after the stress is applied and before a steady state creep stage is reached, the transient creep strain will be more dominant when the stress level is low. While $d\varepsilon_s/dt$ is the steady creep rate, B is the transient creep coefficient, ε_p is the time-independent plastic strain, G is shear modulus, and C_p and m_p are material constants.

Akay, et al [8-9] used only the creep part to represent the total inelastic strain, the creep law is shown as,

$$\frac{d\gamma_s}{dt} = \frac{CGb}{kT} \left(\frac{b}{d} \right)^p \left(\frac{\tau}{G} \right)^n D_0 \exp \left(\frac{-\Delta H}{kT} \right) \quad (2.1.4)$$

where $d\gamma/dt$ is steady-state shear strain rate, G is shear modulus, b is Burgers vector. k is Boltzmann's constant, d is grain size, τ is applied stress, D_0 is diffusion constant, ΔH is activation energy for the deformation process, p is grain size exponent, C is a constant characteristic of the underlying micro-mechanism. Akay's model correlates the macro material behavior with microstructure. The stress exponent, n , is dependent on the rate controlling mechanism. At low stresses, $n=1$ for diffusion creep, $n=2$ for grain boundary sliding. At intermediate stresses, $n=3$ to 4 dislocation glide controlled kinetics, and $n=5$ to 7 for dislocation climb process. At high stresses, the strain rate is an exponential function of stress. The intermediate-to-high stress power law breakdown region can be described by a hyperbolic-sine expression [10]:

$$\frac{d\gamma_s}{dt} = C_1 \frac{G}{kT} \left[\sinh \left(\alpha \frac{\tau}{G} \right) \right]^n \exp \left(\frac{-\Delta H}{kT} \right) \quad (2.1.5)$$

where α prescribes the stress level at which the power dependence break down and C_1 is a constant.

Shi et al [11] also proposed a creep model to describe the creep flow of the solder and the model is capable of explaining the issues of stress and temperature dependent stress exponent and activation energy in the Arrhenius power-law model, shown as

$$\dot{\gamma} = C_1 \frac{G}{T} \left(\frac{\tau}{G} \right)^n \left[1 + C_2 \exp \left(- \frac{(Q_c - Q_l) - (\alpha - \beta)(\tau/G)}{RT} \right) \right] \exp \left(- \frac{Q_l - \alpha(\tau/G)}{RT} \right) \quad (2.1.6)$$

where C_1 , C_2 , α , β are material constants, Q_c and Q_l are the activation energy for the core-diffusion and that for lattice-diffusion, respectively. τ is shear stress, G is shear modulus, T is absolute temperature, R is gas constant.

Elastic-plastic-creep approach is a phenomenological way to describe the constitutive behavior of solder alloy, since the elastic, plastic and creep strains represent different deformation stages. All types of strain have been studied very well, for example, many creep models for high temperature metals can be used for solder creep modeling. However, during the thermal-mechanical loading, the time-independent plastic strain and time-dependent creep strain is difficult to distinguish. From the non-linear deformation modeling point of view, the mechanism of the creep and plastic strain may be related to dislocation motion. In order to study the constitutive behavior from a state variable visco-plastic approach, the creep and plastic strain may be combined into inelastic strain, accumulated over a deformation history.

2.1.2 Visco-plastic approach

The visco-plastic approach follows the materials science perspective that dislocation motion is the cause of both creep and plastic deformation, and combined them into a state variable inelastic strain. The total strain is expressed as,

$$\boldsymbol{\varepsilon}_{ij} = \boldsymbol{\varepsilon}_{ij}^e + \boldsymbol{\varepsilon}_{ij}^{in} \quad (2.1.7)$$

where $\boldsymbol{\varepsilon}_{ij}^{in}$ is the inelastic strain tensor. Some of the visco-plastic models will be described next.

One visco-plastic model commonly used for solder is the Anand model, which was reported by Anand [12]. The Anand model [13] consists of two coupled differential equations that relate the inelastic strain rate to the rate of deformation resistance. The strain rate equation is represented by,

$$\frac{d\epsilon_{in}}{dt} = A \left[\sinh \left(\xi \frac{\sigma}{s} \right) \right]^{\frac{1}{m}} \exp(-Q/RT) \quad (2.1.8a)$$

and the rate of deformation resistance equation by

$$\dot{s} = \left\{ h_0 (|B|)^{\alpha} \frac{B}{|B|} \right\} \frac{d\epsilon_p}{dt} \quad (2.1.8b)$$

$$B = 1 - \frac{s}{s^*} \quad (2.1.8c)$$

$$s^* = \hat{s} \left[\frac{1}{A} \frac{d\epsilon_p}{dt} \exp(-Q/RT) \right] \quad (2.1.8d)$$

where $d\epsilon_{in}/dt$ is the effective inelastic strain rate, σ is effective true stress, s is the deformation resistance, T is the absolute temperature, A is the pre-exponential factor, ξ is the stress multiplier, m is the strain rate sensitivity of stress, Q is the activation energy, R is the universal gas constant, h_0 is the hardening/softening constant, $\hat{s}$ is the coefficient for deformation resistance saturation value, n is the strain rate sensitivity of saturation value, and α is strain rate sensitivity of hardening or softening. In order to curve-fit the nine material constants in the Anand model, the incremental form shown in Eq. (2.1.8) should be integrated into integral form, which is shown in Eq. (2.1.9).

$$\sigma^* = \frac{\hat{s}}{\xi} \left(\frac{\dot{\epsilon}_p}{A} e^{Q/RT} \right)^n \sinh^{-1} \left[\left(\frac{\dot{\epsilon}_p}{A} e^{Q/RT} \right)^m \right] \quad (2.1.9a)$$

$$\sigma = \sigma^* - [(\sigma^* - c s_0)^{(1-a)} + (a-1) c h_0 \sigma^{*(-a)} \epsilon_p]^{1/(1-a)} \quad (2.1.9b)$$

The creep test results can be used to curve-fit the constants in Eq.(2.1.9a), which is the flow equation; while stress-strain curves from tensile tests are used to fit the material constants in Eq.(2.1.9b). The Anand model has been coded into the ANSYS Finite Element software and has been widely used for simulation of the solder joint deformation under thermal-mechanical loading.

Other visco-plastic models were also developed for solder alloys. Tachibana Y. and Krempl E. [14-16] proposed their visco-plastic model based on overstress, called VBO model. VBO model contains a state variable called the equilibrium (back) stress. Bor [17] modified VBO model and applied it into Sn-Pb solder. Unified creep-plasticity (UCP) models are also proven to be successful methods to model the solder material at high homologous temperatures. McDowell D.L. [18] introduced a thermo-viscoplastic internal state variable model to simulate the solder alloys. Wen et al [19] incorporated the damage effect into UCP model, and applied it to Sn-Ag lead-free solder. Busso et al [20] proposed another UCP model, which assumes that the inelastic strain is the result from the release of the dislocations. Other constitutive models were also developed to describe the stress-strain behavior for high temperature metals and other materials. Yaguchi M. [21-23] proposed the model for nickel-base super alloy.

Although the Anand model is widely used for solder joint reliability analysis, its dynamic hardening term h combines the dynamic recovery and strain hardening effects and loses the physical meaning of h . New visco-plastic constitutive model is needed to overcome this concern.

2.2 Low Cycle Fatigue Models

Low cycle fatigue behavior of solders is an important property for fatigue life prediction analysis of thermal cycling tests for soldered assemblies. Typically, thermal cycling test failures fall between 1000 to 10,000 cycles, which is related to low cycle fatigue behavior. Over the years, generally there are two types of approaches to model the fatigue life of structures. They are the total life approach, and the crack initiation and propagation approach. For total life approach, some fatigue parameters, such as strain or strain energy density are used to predict the total fatigue life. However, the crack initiation and propagation approach will predict the fatigue life with a pre-existing crack, the fatigue life is the number of cycles to propagate this crack to a critical size.

2.2.1 Total life approach

Total life approach can be divided into three major methods, based on the fatigue driving force parameter used to characterize the fatigue damage process. These three parameters are (a) plastic strain range, (b) creep strain range and, (c) inelastic energy density or plastic work. In the strain range based fatigue approach, strain controlled loading have been reported by many researchers [24-37]. The strain range based fatigue approach can be further divided into plastic strain range and creep strain range methods. Plastic strain deformation focuses on the time-independent plastic effect, while creep strain accounts for the time-dependent effects. The energy-based fatigue models employ the stress-strain hysteresis energy density of the solder specimen.

2.2.1.1 Plastic Strain Range Fatigue Models

The Coffin-Manson fatigue model [38-39] is perhaps the best-known and most widely used approach. The total number of cycles to failure, N_f , is depicted as being dependent on the plastic strain range, $\Delta\epsilon_p$, the fatigue ductility coefficient, ϵ'_f , and the fatigue ductility exponent, c , given in the expression below:

$$\frac{\Delta\epsilon_p}{2} = \epsilon'_f (2N_f)^c \quad (2.2.1)$$

The fatigue ductility coefficient, ϵ'_f , is approximately equal to the true fracture ductility, ϵ_f . The fatigue ductility exponent, c , varies between -0.5 and -0.7 for tin-lead solder (Dieter, 1986 [40]; Kilinski, 1991 [41]), and experimental data are required to determine the constants. Actual solder joint fatigue tests, however, are often time consuming and the results are usually applicable only to the specific geometry of the solder joint. For small solder joints, FEA modeling can be used to determine the plastic strain, which is then used to predict the fatigue life. This version of the Coffin-Manson relation assumes that fatigue failure is strictly due to plastic deformation and that elastic strains contribute only a small portion to fatigue failure. Because the Coffin-Manson equation considers only plastic deformations, it is commonly combined with the Basquin's equation to account for elastic deformation as well [41]. The resulting equation is known as the total strain equation, and is given below:

$$\frac{\Delta\epsilon}{2} = \frac{\sigma'_f}{E} (2N_f)^b + \epsilon'_f (2N_f)^c \quad (2.2.2)$$

where $\Delta\varepsilon$ is the strain gauge, σ'_f is the fatigue strength coefficient, E is the elastic modulus, ε'_f is the fatigue ductility, b is the fatigue strength exponent (Basquin's exponent), and c is the fatigue ductility exponent. This fatigue model is an improvement over the Coffin-Manson equation in that it also accounts for the elastic contribution to fatigue failure.

Solomon's low cycle fatigue model [42] relates the plastic shear strain range to fatigue life cycles is given below:

$$\Delta\gamma_p N_p^\alpha = \theta \quad (2.2.3)$$

$\Delta\gamma_p$ is the plastic shear strain range. N_p is the number of cycles to failure, θ is the inverse of the fatigue ductility coefficient, and α is a material constant. Typical hysteresis loop is shown in Fig. 2-2.

Fig. 2-2 Typical hysteresis loop

2.2.1.2 Creep Strain Range Fatigue Models

Creep strain range fatigue models account strictly for the cyclic creep deformation in the solder joints. Early attempts at modeling creep were made by isolating the elastic and plastic deformation mechanisms. Creep, as mentioned previously, can be separated into two possible mechanisms, matrix and grain boundary creep. Knecht and Fox [43] proposed a simple matrix creep fatigue model relating the solder microstructure and the matrix creep shear strain range given below,

$$N_f = \frac{C}{\Delta\gamma_{mc}} \quad (2.2.4)$$

The number of cycles to failure, N_f , is related to a constant C , which is dependent on failure criteria and solder microstructure. $\Delta\gamma_{mc}$ is the strain range due to matrix creep.

The second creep mechanism, grain boundary sliding, is incorporated with matrix creep into a fatigue model presented by Syed [44-45]. In this model, creep strain is partitioned into two parts as shown [44],

$$N_f = \left([0.022D_{gbs}] + [0.063D_{mc}] \right)^{-1} \quad (2.2.5)$$

Here, D_{gbs} and D_{mc} are the accumulated equivalent creep strain per cycle for grain boundary sliding and the matrix creep, respectively. Results published by Syed on thin small outline package (TSOP) parts indicated that the dominant mechanism changes from grain boundary sliding to matrix creep for faster ramp rates, stiffer assemblies, and lower temperature controlling the lower temperature ranges.

2.2.1.3 Creep-Fatigue Interaction Model

By applying Miner's linear superposition principal, both plastic and creep strain can be accounted for in strain-based fatigue model. This model combines the Solomon fatigue model with the Knecht and Fox creep model, and is given below:

$$\frac{1}{N_f} = \frac{1}{N_p} + \frac{1}{N_c} \quad (2.2.6)$$

where N_p refers to the number of cycles to failure due to plastic fatigue and is obtained directly from the Solomon's fatigue model. N_c refers to the number of cycles to failure due to the creep fatigue and is obtained from the Knecht and Fox's creep fatigue model. This fatigue model relates the fatigue behavior to the plastic shear strain imposed on the specimen, and requires data collection or determination of the experimental plastic strain range. The model has been applied to ceramic BGA and underfilled flip chip assemblies subjected to thermal cycling loading [46-49]. However, this model does not account for frequency effects.

A similar approach is the Strain Range Partitioning (SRP) approach [41]. In SRP, a typical hysteresis loop can be separated into four components, the plastic strain in tension and compression (PP), the creep strain in tension and compression (CC), the creep strain in tension-plastic strain in compression (CP) and the plastic strain in tension-creep strain in compression (PC), as shown in Fig. 2-3. The SRP equation is given below:

$$\frac{1}{N_f} = \frac{F_{pp}}{N_{pp}} + \frac{F_{cc}}{N_{cc}} + \frac{F_{cp}}{N_{cp}} + \frac{F_{pc}}{N_{pc}} \quad (2.2.7)$$

where F_{ij} is the fraction of the total inelastic strain range of the hysteresis loop. The

contributions to each part are determined from other fatigue models and from cyclic stress-strain test. Though the SRP model is a good approach to study the creep-fatigue interaction, it may be difficult for application.

Fig. 2-3 Schematic of the Strain Range Partitioning Method

2.2.1.4 Total Strain Range Fatigue Model

The Engelmaier fatigue model [50] is shown in Eq. (2.2.8), the total number of cycles to failure is related to the total shear strain, $\Delta\gamma_t$, the fatigue ductility coefficient, ϵ'_f , and the variable, c , which is a function of frequency and temperature.

$$N_f = \frac{1}{2} \left[\frac{\Delta\gamma_t}{2\epsilon'_f} \right]^{1/c} \quad (2.2.8)$$

where $c = -0.442 - 6 \times 10^{-4} T_s + 1.74 \times 10^{-2} \ln(1+f)$ for Sn-Pb solders. T_s is the mean cyclic solder joint temperature in °C, and f is the cyclic frequency in cycles/day. This fatigue model improves on Soloman's and Coffin-Manson by including cyclic frequency and temperature effects.

2.2.1.5 Frequency Modified Plastic Strain Range Method

The constants in the Coffin-Manson model are dependent on temperature and cyclic frequency. Shi et al. [51] proposed a modified Coffin-Manson model for eutectic tin-lead solder given below:

$$\left[N_f \nu^{(k-1)} \right]^m \Delta \epsilon_p = C \quad (2.2.9)$$

where $\nu^{(k-1)} =$

$$\begin{cases} \nu^{(k_1-1)} & \text{for } 1\text{Hz} \geq \nu \geq 10^{-3} \text{ Hz} \\ \left[\frac{\nu}{10^{-3}} \right]^{(k_2-1)} (10^{-3})^{(k_1-1)} & \text{for } 10^{-3} \text{ Hz} > \nu \geq 10^{-4} \text{ Hz} \end{cases}$$

where k_1 , k_2 , m and C are dependent on temperature. The frequency effect was compensated by this frequency-modified model. However, the temperature effect of low cycle fatigue behavior is still a problem.

2.2.1.6 Energy-Based Models

Energy-based fatigue models are used to predict fatigue failure based on measured hysteresis energy volume-weighted average strain energy density history. Fatigue energy is typically calculated using some correlation to the energy under the stress-strain hysteresis loop. Akay et al [8-9] has proposed the following fatigue model, based on the total strain energy,

$$N_f = \left(\frac{\Delta \bar{W}_{total}}{W_0} \right)^{1/k} \quad (2.2.10)$$

where N_f is the mean cycles to failure, $\Delta \bar{W}_{total}$ is the total strain energy, W_0 and k are fatigue coefficients. They used this model on an LLCC leaded package fatigue

behavior.

Darveaux et. al [10] used strain energy to predict crack initiation and crack growth, the equations are given below:

$$N_0 = K_1 \Delta W^{K_2} \quad (2.2.11)$$

$$\frac{da}{dN} = K_3 \Delta W^{K_4} \quad (2.2.12)$$

where ΔW is strain energy, K_1 , K_2 , K_3 , and K_4 are material constants. When this model was used in finite element analysis, the strain energy ΔW is normalized by the volume of the element:

$$\Delta W_{ave} = \frac{\sum \Delta W \cdot V}{\sum V} \quad (2.2.13)$$

where ΔW_{ave} is the average strain energy, V is the volume of each element.

Shi et al. [52] proposed a modified energy-based low cycle fatigue model, given below:

$$\left[N_f \nu^{(k-1)} \right]^m \frac{W_p}{2\sigma_f} = C \quad (2.2.14)$$

where $\nu^{(k-1)} =$

$$\begin{cases} \nu^{(k_1-1)} & \text{for } 1\text{Hz} \geq \nu \geq 10^{-3} \text{ Hz} \\ \left[\frac{\nu}{10^{-3}} \right]^{(k_2-1)} (10^{-3})^{(k_1-1)} & \text{for } 10^{-3} \text{ Hz} > \nu \geq 10^{-4} \text{ Hz} \end{cases}$$

where k_1 , k_2 , m and C are dependent on temperature. This model has been used for fatigue life prediction of PBGA and flip chip solder joint reliability evaluations [47].

2.2.2 Crack initiation and propagation approach

Crack initiation and propagation approach characterizes the fatigue crack growth phases during the fatigue life. Some research work on applying fracture mechanics to tin-lead solder had been reported by Pao [53] and Lau [54]. Fatigue crack growth behavior under creep-fatigue conditions have been reported for solders and other metals (Bernstein, 1982 [55]; Kordisch, 1996 [56]; Mcdowell, 1996 [57]; Pidaparti, 1996 [58]; Nguyen, 2000 [59]; Liu, 2000 [60]; Mutoh, 2001 [61]; Zhao 2002 [62]). Because of the low melting point of solder, the material is at high homologous temperature. Under low cycle fatigue (LCF) condition, it is known that the time-dependent creep deformation is likely to occur together with cyclic fatigue crack growth under creep-fatigue interaction conditions. Creep failure is characterized by intergranular cracking due to grain boundary sliding, while fatigue failure occurs due to formation of surface cracks and then propagation. The creep-fatigue failure can be viewed as interaction of grain boundary cracks with the fatigue cracks. Therefore, failure would be transgranular at high frequencies and become intergranular at low frequencies due to transition from fatigue to creep controlled mechanisms (See Fig. 2-4). Hence, the fatigue crack growth behavior can be separated as: fatigue dominated region and creep-dominated region.

Fig. 2-4 Transgranular and Intergranular Fracture

For fatigue-dominated region, the crack growth is cycle dependent, the failure mechanism is transgranular, and many researchers [61-62] use ΔJ to predict fatigue crack growth rate in this region, given below:

$$da / dN = A(\Delta J)^m \quad (2.2.15)$$

where a is crack length, N is cycle, A and m are material constants, and ΔJ -value can be calculated according to the following equation:

$$\Delta J = \frac{S_p}{B(W-a)} f(a, W) \quad (2.2.16)$$

where S_p is the area under the load verses load-line displacement curve with consideration of crack closure. B , W and a are the thickness, the width and the crack length, respectively. $f(a, W)$ is the function of geometry determined by a and W .

For creep dominated region, the crack growth is time dependent, the failure mechanism is intergranular, and C^* can be used to predict the crack growth in this region, shown as:

$$da/dt = B(C^*)^n \quad (2.2.17)$$

where a is crack length, B and n are material constants, and C^* -value is estimated by using the following equation:

$$C^* = \frac{P\dot{V}_c}{BW} \left[\frac{n}{n+1} \left(\frac{2}{1-a/W} + 0.522 \right) \right] \quad (2.2.18)$$

where P is the applied load ($P_{\max}$ was used in cyclic loading condition), $\dot{V}_c$ is the load-line displacement rate, B , W and a are the specimen thickness, width and crack length, respectively. n is the creep exponent. However, there are some practical difficulties in applying this approach to thermal fatigue problems.

The total life approach is most widely used. However, its fatigue exponent m and ductility coefficient C will dependent on test temperatures and frequencies. Shi et al [51-52] proposed the frequency-modified Coffin-Manson and Morrow's model, and solved the frequency dependent problem, it is still difficult to characterize the temperature and frequency dependent low cycle fatigue behavior of solder alloys in the thermal-mechanical loading conditions. Furthermore, the plastic strain range or inelastic strain energy density used in Coffin-Manson or Morrow's model is derived at a representative "stable" hysteresis loop. Kanchanomai [35] noted that there is no

“stable” hysteresis loop during the fatigue tests of lead-free solder alloys. The plastic strain range will increase, while the stress range will decrease with the cycles. It may not be reasonable to use only one representative “stable” loop information to characterize the long period of fatigue life. Hence, new fatigue model is needed to overcome this problem.

Chapter 3. Experimental Procedure

To characterize the mechanical and creep properties of lead-free solder alloys, tensile and creep tests over a wide range of test conditions were conducted. Low cycle fatigue tests were conducted to characterize the fatigue resistances at different temperatures and frequencies. Thermal cycling loading is the major concern of solder alloys; however, drop impact loading is also very important. Hence, impact tests were conducted to characterize the mechanical properties of solder alloys at high strain rate. In this chapter, the experimental procedure and details for a comprehensive mechanics test program is described. This includes the specimen geometry, test conditions and matrix, test machine and procedure used.

3.1 Tensile test

The tensile test method was employed to measure the mechanical properties of 95.5Sn-3.8Ag-0.7Cu and 99.3Sn-0.7Cu solder alloys. Dog bone-shaped bulk solder specimens for uni-axial tensile test were machined from solder bar. The specimen has a total length of 65mm, a gage length of 15mm, and a diameter of 3mm (See Fig.3-1), which is following the ASTM standard [63]. The specimens were annealed for 24 hours at 60°C in vacuum to eliminate the surface residual stresses.

Fig.3-1 Geometry of tensile and creep specimen (in mm)

The tensile tests were carried out on a universal testing machine, Instron model 5569, at four different temperatures (-40°C , 25°C , 75°C and 125°C). At each temperature, three different displacement rates were used (0.5mm/min, 5mm/min and 50mm/min). The test matrix for Sn-3.8Ag-0.7Cu and Sn-0.7Cu are shown in Table 3-1 and 3-2. In order to perform the test over the range from -40°C to 125°C , it was conducted within a thermally insulated chamber. A non-contact video extensometer was employed in the specimen gauge section to measure the true extension of the specimen. Two lines were marked on the gauge length of the specimen as shown in Fig. 3-2(a), and are detected by the system as shown in Fig. 3-2(b). When test is in progress, the distance between these two points can be measured and the strain of the specimen can be calculated. A computer with the data acquisition software was used to collect the data.

Fig. 3-2(a) Image of video extensometer

Fig. 3-2(b) Detected points

Table 3-1 Tensile test matrix for Sn-3.8Ag-0.7Cu

	-40°C	25°C	75°C	125°C
0.5mm/min	×1	×3	×3	×3
5mm/min	×1	×3	×3	×3
50mm/min	×1	×3	×3	×3

Table 3-2 Tensile test matrix for Sn-0.7Cu

	-40°C	25°C	75°C	125°C
0.5mm/min	-	×3	×2	×2
5mm/min	-	×2	×2	×2
50mm/min	-	×2	×2	×2

After the specimen grips and environmental chamber reached thermal equilibrium, the specimen was fixed in grips within the chamber for a minimum of half an hour prior to testing. The specimen temperature was monitored by a thermal-couple. A feed back control was used to regulate the test temperature. An example of the specimen for Sn-3.8Ag-0.7Cu solder before and after testing (at 125°C and 0.5mm/min) is shown in Fig. 3-3. The load and displacement curves for three repeated tests at 125°C and 0.5mm/min are given in Fig. 3-4. In order to calculate the modulus and yield stress accurately, initial parts of the load and displacement curves are plotted in Fig. 3-5. Using Fig. 3-5 and following the method in ASTM standard, the Elastic modulus, yield stress at certain condition can be calculated.

Fig. 3-3 Tensile specimen before and after testing

Fig. 3-4 Load-displacement curves at 125°C and 0.5mm/min

Fig. 3-5 Initial parts of load and displacement curves at 125°C and 0.5mm/min

3.2 Creep Test

The specimen used for tensile test for 95.5Sn-3.8Ag-0.7Cu and 99.3Sn-0.7Cu solder alloy was also used for the creep test program. The specimens were also annealed for 24 hours at 60°C in vacuum to eliminate the surface residual stresses. The creep tests were carried out on a universal testing machine, Instron model 5569, the machine has the capability to hold the load constant. A thermal chamber was used for creep test over a wide range of test temperatures. In the creep test, specimen was deformed in tension at constant load. The non-contact video extensometer was employed to measure the strain. Creep tests were carried out at four different temperatures (-40°C, 25°C, 75°C and 125°C), with constant stress set at different values (3, 4, 5, 7, 10, 15, 20, 25, 30, 35, 40, 50, 60 and 70 MPa). The test matrix for Sn-3.8Ag-0.7Cu and Sn-0.7Cu are shown in Table 3-3 and 3-4. After the specimen grips and chamber reached thermal equilibrium, the specimen was placed into the chamber for a minimum of half an hour prior to testing. The specimen temperature was monitored by a thermal-couple, which is used to regulate the testing temperature in the chamber. For example, specimen for Sn-3.8Ag-0.7Cu solder, before and after testing (at 125°C and 10MPa) is shown in Fig. 3-6.

Table 3-3 Creep test matrix for Sn-3.8Ag-0.7Cu

	-40°C	25°C	75°C	125°C
2MPa	-	-	-	×1
3MPa	-	-	-	×1
5MPa	-	×1	×1	×2
7MPa	-	-	×1	×1
10MPa	-	×1	×1	×2
15MPa	-	×2	×1	×1
20MPa	-	×1	×1	×2
25MPa	×1	×2	×2	-
30MPa	×1	×1	-	-
35MPa	-	×2	×1	
40MPa	×1	×1	-	-
50MPa	×1	-	-	-
60MPa	×1	-	-	-
70MPa	×1	-	--	-

Table 3-4 Creep test matrix for Sn-0.7Cu

	25°C	75°C	125°C
3MPa	-	×1	×1
4MPa	-	-	×1
5MPa	×1	×1	×2
7MPa	×1	×1	×1
10MPa	×2	×2	×2
15MPa	×1	×1	×1
20MPa	×2	×1	×2
25MPa	×1	×1	-
30MPa	×2	×1	-
35MPa	×1	-	-

Fig. 3-6 Creep specimen before and after testing

3.3 Low Cycle Fatigue Test

The low cycle fatigue test specimens for 95.5Sn-3.8Ag-0.7Cu and 99.3Sn-0.7Cu solder alloy were machined from the solder bar as well. The configuration of the fatigue specimens has a diameter of 6mm at the two grip ends, a center diameter of 3mm, and a gauge length of 4.5mm with a radius of curvature of 50mm. The geometry of the specimen follows the ASTM standard [64] and is shown in Fig. 3-7.

The low cycle fatigue tests were conducted on a micro-force materials test system. Chuck grips were used to fix the solder specimen for tension-compression fatigue test. The tests were run under a symmetrical uni-axial tension-compression loading with

total displacement control over a range of test frequencies. The sine waveform was employed for all fatigue tests. The total strain was calculated from the crosshead displacement divided by the gauge length. The tests were carried out at three different frequencies (10^{-3} , 10^{-2} and 1Hz) and at three different temperatures (25, 75 and 125°C) with total strain set at four different values (2, 3.5, 5 and 7.5%). The test matrix of fatigue test for Sn-3.8Ag-0.7Cu and Sn-0.7Cu are shown in Table 3-5 and 3-6. The fatigue failure was defined as 50% reduction of maximum tensile load. The specimen of Sn-3.8Ag-0.7Cu solder before and after testing at 75°C, 1Hz and 3.5% total strain is shown in Fig. 3-8.

Fig. 3-7 Geometry of fatigue specimen(in mm)

Fig. 3-8 Fatigue specimen before and after testing

Table 3-5 Fatigue test matrix for Sn-3.8Ag-0.7Cu

		25°C	75°C	125°C
2%	1Hz	×2	×1	×2
	0.01Hz	×2	×1	×2
	0.001Hz	×1	×1	×1
3.5%	1Hz	×1	×1	×1
	0.01Hz	×1	×1	×1
	0.001Hz	×1	×1	×1

5%	1Hz	×1	×1	×1
	0.01Hz	×1	×1	×1
	0.001Hz	×1	×1	×1
7.5%	1Hz	×2	×1	×2
	0.01Hz	×2	×1	×2
	0.001Hz	×1	×1	×1

Table 3-6 Fatigue test matrix for Sn-0.7Cu

		25°C	75°C	125°C
2%	1Hz	×1	×1	×1
	0.01Hz	×1	×1	×1
	0.001Hz	-	-	×1
3.5%	1Hz	×1	×1	×1
	0.01Hz	×1	×1	×1
	0.001Hz	-	-	×1
5%	1Hz	×1	×1	×1
	0.01Hz	×1	×1	×1
	0.001Hz	-	-	×1
7.5%	1Hz	×1	×1	×1
	0.01Hz	×1	×1	×1
	0.001Hz	-	-	×1

3.4 Split Hopkinson Pressure Bar Impact Test

Impact test method was employed to determine the mechanical properties of 95.5Sn-3.8Ag-0.7Cu solder alloys at high strain rate. Dog bone-shaped bulk solder specimens for impact tensile test were machining from solder bars. The specimen has a total length of 50mm, a gage length of 10 mm, and a diameter of 4mm (See Fig. 3-9). The specimen was threaded at both ends and screwed to the test system.

Impact tests were conducted with a Split Hopkinson pressure bar (SHPB). The Hopkinson bar test system commonly used to study the dynamic response of materials. The basic theory of the SHPB is based on the theory of stress wave propagation in elastic bar and interaction between a stress pulse and the specimen of different impedance. The data acquisition system collects and analyzes the output waveforms from the SHPB tests. A schematic illustration of the SHPB and recording system is shown in Fig. 3-10. The solder specimen was assembled between the incident and transmitted bars (ie: input and output bars). Strain gages at the mid-span of both the incident and transmitted bars were used to measure the dynamic response. The strain gages used on the bars are 120Ω and connected in a full bridge circuitry arrangement. Data acquisition is performed with a TML DC-92D dynamic strain meter and a DL 1540 digital oscilloscope. The strain meter will amplify the pulse signals and the oscilloscope will display the input and output waveforms.

The pressure pulse was initiated by axial impact from the striker bar that was accelerated to the desired impact velocity by the pressure chamber. The striker bar impacts on the anvil bar, which was connected to the input bar, so the pulse can travel via the input bar to the specimen. This manner of loading produces a loading pulse in the input bar with an amplitude that is proportional to the impact velocity of the striker. The impact mechanical properties can be calculated from the strain gauge readings. The test matrix is shown in Table 3-7.

Fig. 3-9 Geometry of impact specimen (in mm)

Table 3-7 Impact test matrix for Sn-3.8Ag-0.7Cu

Strain rate	25°C
$7 \times 10^2 \text{ s}^{-1}$	×3
$9 \times 10^2 \text{ s}^{-1}$	×2
$1.3 \times 10^3 \text{ s}^{-1}$	×3

Fig. 3-10 Dynamic tensile test using SHPB testing system

Chapter 4. Tensile Test Data & Analysis

In this chapter, mechanical properties will be presented for different temperatures and strain rates for the two NEMI recommended lead-free solder alloys. Temperature and strain rate dependent expression for stress-strain properties was developed and non-linear curve-fitting to use Anand model will also be presented.

4.1 Tensile test result

4.1.1 95.5Sn-3.8Ag-0.7Cu solder alloy results

The effects of strain rate and temperature on the 95.5Sn-3.8Ag-0.7Cu tensile properties were evaluated and the stress-strain curves for the three different strain rates at a constant temperature of 25°C are shown in Fig 4.1-1. The test result for the three strain rate conditions at temperature of 125°C is given in Fig 4.1-2. The strain rate was calculated using displacement rate of machine divided by the gauge length of specimen. It can be seen that the mechanical properties of 95.5Sn-3.8Ag-0.7Cu is strongly dependent on the test temperature and strain rate parameters [65-67]. For the same temperature, strength of the material will increase with strain rate, ultimate strength increase from about 40MPa for strain rate of $5.6 \times 10^{-4} \text{ s}^{-1}$ to 60MPa for $5.6 \times 10^{-2} \text{ s}^{-1}$ at 25°C (See Fig. 4.1-1); However, at the same strain rate, the strength will decrease with temperature, for example, in Fig. 4.1-1 and 4.1-2, both line (c) indicate the strain rate of $5.6 \times 10^{-4} \text{ s}^{-1}$, while the strength will decrease from 40MPa at 25°C to 20MPa at 125°C.

Fig. 4.1-1 Tensile test results at constant temperature of 25°C

Fig. 4.1-2 Tensile test results at constant temperature of 125°C

Based on the stress-strain curves obtained from tensile test, the Elastic modulus, yield stress and UTS can be derived. Fig. 4.1-3 illustrate the calculation method.

Fig. 4.1-3 Illustration of calculating elastic modulus, yield stress and UTS

The result of the effect of temperature on elastic modulus is shown in Fig. 4.1-4. It can be seen that the curves demonstrate linear relationship between the elastic modulus and the temperature and elastic modulus decrease with the increase of temperature. The effect of strain rate on elastic modulus was presented by plotting the graph of elastic modulus versus strain rate as shown in Fig. 4.1-5. The plot shows approximately straight lines with a constant slope for any given temperature. This is expected as the elastic modulus has a linear function of logarithmic strain rate and elastic modulus increase with increase in strain rate.

Fig.4.1-4 Effect of temperature on elastic modulus

Fig.4.1-5 Effect of strain rate on elastic modulus

The yield stress was computed from the stress-strain curve at 0.2 percent plastic strain. The effects of test temperature and strain rate on the yield stress are given in Figs 4.1-6 and 4.1-7, respectively. There is a linear relationship between the yield stress versus temperature plot, and Yield Stress versus logarithmic strain rate. The yield stress increases with faster strain rate, and decreases with increase in temperature.

The corresponding results for the ultimate tensile stress (UTS) are given in Figs 4.1-8 and 4.1-9, respectively. The UTS results follow a similar trend as the yield stress results. UTS increases with increase in strain rate, and decreases with increase in temperature.

Fig. 4.1-6 Effect of temperature on yield stress

Fig. 4.1-7 Effect of strain rate on yield stress

Fig.4.1-8 Effect of temperature on UTS

Fig.4.1-9 Effect of strain rate on UTS

The temperature and strain rate dependent elastic modulus, yield stress and UTS for the bulk 95.5Sn-3.8Ag-0.7Cu solder tensile test results are summarized in Table 4.1-1. The variance range of test data was also shown to evaluate the repeatability of test results.

Table 4.1-1: Summary of Tensile Test Results for Sn-Ag-Cu Solder

	E (GPa)	Yield (MPa)	UTS (MPa)
25°C			
5.6 x10 ⁻⁴	41.8 ± 3.0	35.1 ± 0.5	40.6 ± 1.4
5.6 x10 ⁻³	48.3 ± 2.1	42.9 ± 2.1	49.0 ± 0.9
5.6 x10 ⁻²	55.1 ± 2.4	52.8 ± 1.5	58.0 ± 2.5
75°C			
5.6 x10 ⁻⁴	30.7 ± 1.9	25.6 ± 2.5	29.0 ± 3.2
5.6 x10 ⁻³	36.0 ± 0.6	33.5 ± 0.7	38.8 ± 3.3
5.6 x10 ⁻²	42.4 ± 3.5	41.5 ± 1.2	47.0 ± 3.5
125°C			
5.6 x10 ⁻⁴	18.8 ± 3.8	16.7 ± 0.5	19.7 ± 0.4
5.6 x10 ⁻³	26.1 ± 0.8	23.9 ± 1.6	27.2 ± 1.8
5.6 x10 ⁻²	32.5 ± 1.2	34.0 ± 1.0	39.7 ± 0.5

-40°C			
5.6×10^{-4}	51	58.4	67.9
5.6×10^{-3}	57	68.7	76.6
5.6×10^{-2}	63	76.5	83.3

4.1.2 99.3Sn-0.7Cu solder alloy results

The mechanical properties of Sn-0.7Cu lead-free solder alloy show similar trend but with low magnitude compared to Sn-3.8Ag-0.7Cu solder alloy. The elastic modulus, yield stress and UTS increases with strain rate and decreases with temperature. Sn-0.7Cu solder has lower mechanical properties than Sn-3.8Ag-0.7Cu solder alloy, but higher than Sn-37Pb solder.

The temperature and strain rate dependent elastic modulus, yield stress and UTS for the bulk 99.3Sn-0.7Cu solder tensile test results are given in Table 4.1-2. The variance range of test data was also shown to evaluate the repeatability of test results.

Table 4.1-2: Summary of Tensile Test Results for Sn-Cu Solder

	E (GPa)	Yield (MPa)	UTS (MPa)
25°C			
5.6×10^{-4}	20.2 ± 3.7	31.1 ± 1.7	35.8 ± 2.6
5.6×10^{-3}	25.6 ± 1.2	36.5 ± 2.4	45.0 ± 1.5
5.6×10^{-2}	32.0 ± 2.1	47.8 ± 2.8	52.0 ± 1.6
75°C			
5.6×10^{-4}	15.6 ± 1.6	22.8 ± 1.1	26.1 ± 0.6
5.6×10^{-3}	18.9 ± 2.1	30.4 ± 1.8	34.2 ± 2.1
5.6×10^{-2}	23.3 ± 2.4	35.8 ± 1.4	42.0 ± 0.8
125°C			
5.6×10^{-4}	11.6 ± 2.6	16.5 ± 2.6	18.2 ± 1.5
5.6×10^{-3}	15.0 ± 1.8	21.4 ± 4.4	26.1 ± 2.8
5.6×10^{-2}	18.9 ± 1.7	29.5 ± 3.8	38.2 ± 4.1

4.1.3 Comparison with other reported results

4.1.3.1 Comparison with tin-lead solder

Shi [68] reported the mechanical properties for 63Sn-37Pb solder at different temperatures and strain rates. The comparison of elastic modulus, yield stress and UTS for Sn-3.8Ag-0.7Cu, Sn-0.7Cu and 63Sn-37Pb [68] at room temperature and high temperature are shown in Figs 4.1-10, 4.1-11 and 4.1-12, respectively. It can be noted that Sn-Ag-Cu has the highest mechanical properties of the three solders. While Sn-Cu solder has similar mechanical properties with Sn-37Pb solder. The differences in elastic modulus are significant for three solders. At room temperature, the Sn-Ag-Cu has a modulus of 50GPa, compared with about 30GPa for Sn-Cu and Sn-Pb solders. However, the difference in yield stress and UTS is not as large as elastic modulus.

Fig. 4.1-10(a) Comparison of Elastic modulus at room temperature

Fig. 4.1-10(b) Comparison of Elastic modulus at high temperature (125°C)

Fig. 4.1-11(a) Comparison of yield stress at room temperature

Fig. 4.1-11(b) Comparison of yield stress at high temperature (125°C)

Fig. 4.1-12(a) Comparison of UTS at room temperature

Fig. 4.1-12(b) Comparison of UTS at high temperature (125°C)

4.1.3.2 Comparison with other lead-free solders data

The reported mechanical properties for other lead-free solder data will be summarized and compared with the author’s data.

Some reported test data [69-81] were reviewed for Sn-Ag-Cu and Sn-Cu lead-free solders. Harrison et al [73] and Kanchanomai et al [35] reported elastic modulus of Sn-Ag-Cu at different temperatures, data comparison with author’s result is shown in Fig. 4.1-13. Tensile strength for Sn-Ag-Cu and Sn-Cu lead-free solders at different temperatures were also reported (NCMS, 1998 [69]; Lin, 2001 [72]; Kim, 2002 [77]; Kanchanomai, 2002 [37]; Plumbridge, 2001 [74]), the comparison is shown in Fig. 4.1-14 and 15. Temperature and strain effect on tensile strength reported by author and other researchers (Foley, 2000 [70]; Amagai, 2002 [76]; Hirose, 2004 [80];

Shohji, 2004 [81]) for Sn-Ag-Cu solder is shown in Fig. 4.1-16, it was found that the author's test results were compared well with other researchers' results.

Fig. 4.1-13 Comparison of elastic modulus at different temperatures for Sn-Ag-Cu

Fig. 4.1-14 Comparison of tensile strength at different temperatures for Sn-Ag-Cu

Fig. 4.1-15 Comparison of tensile strength at different temperatures for Sn-Cu

Fig. 4.1-16 (a) Temperature effects of UTS for Sn-Ag-Cu at strain rate of $1E-3 \text{ s}^{-1}$

Fig. 4.1-16 (b) Strain rate effect of UTS for Sn-Ag-Cu at room temperature

4.2 Analysis of tensile test result

4.2.1 Strain rate and temperature dependent tensile properties

In section 4.1, it had been found that the mechanical properties of Sn-3.8Ag-0.7Cu and Sn-0.7Cu are dependent on temperature and strain rate. Hence, a statistical method incorporating linear regression was employed to quantify the temperature and strain rate dependent mechanical properties of 95.5Sn-3.8Ag-0.7Cu and 99.3Sn-0.7Cu lead-free solders.

The elastic modulus of 95.5Sn-3.8Ag-0.7Cu and 99.3Sn-0.7Cu is as follows:

$$E(T, \dot{\epsilon})_{SnAgCu} = (0.00074T + 6.44) \log(\dot{\epsilon}) + (-0.1932T + 65.935) \quad (4.2.1)$$

$$E(T, \dot{\epsilon})_{SnCu} = (-0.0235T + 6.396) \log(\dot{\epsilon}) + (-0.157T + 42.1) \quad (4.2.2)$$

The yield stress and UTS were established and expressed individually as follows:

$$\sigma_y(T, \dot{\epsilon})_{SnAgCu} = (-0.2053T + 76.61)(\dot{\epsilon})^{(6.54 \times 10^{-4}T + 0.074)} \quad (4.2.3)$$

$$\sigma_y(T, \dot{\epsilon})_{SnCu} = (-0.199T + 65.1)(\dot{\epsilon})^{(2.87 \times 10^{-4}T + 0.08254)} \quad (4.2.4)$$

$$UTS(T, \dot{\epsilon})_{SnAgCu} = (-0.2161T + 81.32)(\dot{\epsilon})^{(6.27 \times 10^{-4}T + 0.0619)} \quad (4.2.5)$$

$$UTS(T, \dot{\epsilon})_{SnCu} = (-0.062T + 65.8)(\dot{\epsilon})^{(7.9 \times 10^{-4}T + 0.0545)} \quad (4.2.6)$$

The calculated values and percentage error of the predicted elastic modulus, yield stress and UTS compared to the test results for Sn-3.8Ag-0.7Cu and Sn-0.7Cu lead-free solders are given in Table 4.2-1 and 4.2-2, respectively. The equations of elastic modulus, yield stress and UTS are within 5% of the test results. That means the curve-fitted equations (4.2.1) to (4.2.6) gave satisfactory estimation of the temperature and strain rate dependant mechanical properties compared to the tensile test result of 95.5Sn-3.8Ag-0.7Cu and 99.3Sn-0.7Cu lead-free solders.

Table 4.2-1: Calculated Values From Equations and Percentage Error for Sn-Ag-Cu

Test Conditions	Elastic Modulus (% error)	Yield Stress (% error)	UTS (% error)
25°C			
5.6 x10 ⁻⁴	40.1(4)	36.3(3.5)	42.5(4.7)
5.6 x10 ⁻³	46.6(3.5)	44.7(4.2)	50.8(3.6)
5.6 x10 ⁻²	53(3.8)	55.1(2.5)	60.7(4.7)
75°C			
5.6 x10 ⁻⁴	30.3(1.3)	24.4(4.7)	28.8(0.63)
5.6 x10 ⁻³	36.8(2.3)	32.3(3.5)	37(4.6)
5.6 x10 ⁻²	43.3(2.1)	42.9(3.4)	47.6(1.2)
125°C			
5.6 x10 ⁻⁴	20.5(0.6)	15.9(3.7)	19(3.6)
5.6 x10 ⁻³	27.1(4.1)	22.7(5.0)	26.3(3.3)
5.6 x10 ⁻²	33.6(3.4)	32.5(4.4)	36.3(1.2)
-40°C			
5.6 x10 ⁻⁴	52.8(3.5)	59.3(1.5)	68.3(0.58)
5.6 x10 ⁻³	59.2(3.9)	66.2(3.7)	74.3(2.9)
5.6 x10 ⁻²	65.6(4.2)	73.9(3.4)	80.9(2.9)

Table 4.2-2: Calculated Values From Equations and Percentage Error for Sn-Cu

Test Conditions	Elastic Modulus (% error)	Yield Stress (% error)	UTS (% error)
25°C			
5.6 x10 ⁻⁴	19.2(4.8)	30.7(1.3)	36.8(2.7)
5.6 x10 ⁻³	25.0(2.3)	37.7(3.4)	43.6(3.1)
5.6 x10 ⁻²	30.9(3.6)	46.4(2.9)	51.8(0.46)
75°C			
5.6 x10 ⁻⁴	15.2(2.7)	22.9(0.7)	26.0(0.33)
5.6 x10 ⁻³	19.8(4.8)	29.2(3.9)	33.8(1.1)
5.6 x10 ⁻²	24.4(4.7)	37.1(3.6)	43.9(4.6)
125°C			
5.6 x10 ⁻⁴	11.1(4.2)	16.5(0.09)	18.4(0.86)
5.6 x10 ⁻³	14.6(3.3)	21.7(1.4)	26.1(0.13)
5.6 x10 ⁻²	18.0(4.6)	28.5(3.4)	37.2(2.6)

Apparent elastic modulus, yield stress and UTS can be calculated from equations (4.2.1) to (4.2.6) for different temperatures and strain rates. By using these properties, bi-linear stress-strain curves can be generated for Finite Element Analysis (FEA) application, as shown in Fig. 4.2-1. However, bi-linear curve is only an approximate analysis; actual stress strain curves (See Fig. 4.2-2) should be modeled for more accurate application. Hence, curve-fitting of Anand model will be discussed next.

Fig. 4.2-1 Schematic illustration of bi-linear strain curves

Fig. 4.2-2 Schematic illustration of actual stress strain curves

4.2.2 Application to Anand visco-plastic model

The Anand visco-plastic model is widely used in thermo-mechanical analysis of solder joint reliability. It includes two kinds of equations, the first one deal with relationship between saturation stress and strain rate under certain temperature, while the second one deal with the relationship between strain and stress under certain strain rate and temperature. They are given in Eqs. (4.2.7) and (4.2.8):

$$\sigma^* = \frac{\hat{s}}{\xi} \left(\frac{\dot{\epsilon}_p}{A} e^{Q/RT} \right)^n \sinh^{-1} \left[\left(\frac{\dot{\epsilon}_p}{A} e^{Q/RT} \right)^m \right] \quad (4.2.7)$$

where variables $\dot{\epsilon}_p$ and T denote strain rate and temperature respectively. And parameters Q/R , A , $\hat{s}/\xi$, m and n can be determined by a nonlinear fitting method.

$$\sigma = \sigma^* - [(\sigma^* - c s_0)^{(1-a)} + (a-1) c h_0 \sigma^{*(-a)} \epsilon_p]^{1/(1-a)} \quad (4.2.8)$$

where variable ϵ_p denote the nonlinear strain, and a , s_0 and h_0 are parameters to be determined. And c is a function of strain rate and temperature:

$$c \equiv \frac{1}{\xi} \sinh^{-1} \left[\left(\frac{\dot{\epsilon}_p}{A} e^{Q/RT} \right)^m \right] \quad c < 1 \quad (4.2.9)$$

All variables and parameters involved in Eq. (4.2.9) have been used in Eq. (4.2.7). Even though, ξ in Eq. (4.2.9) is used independently and it is used as a part of parameter $\hat{s}/\xi$. If ξ is regarded as an independent parameter, there will be 9 parameters involved in Anand model. But ξ and $\hat{s}$ could not be determined by curve fitting of Eq. (4.2.7) and Eq. (4.2.8). However, the Anand model has been implemented with nine parameters in the ANSYS Finite Element software. Hence, the user needs to "guess" the value of ξ by the condition of $c < 1$. The procedure to determine all nine parameters is as follows:

- 1) Determination of the saturation stress σ^* under a series of strain rate and temperature by creep test.
- 2) Curve fitting of parameters Q/R , A , $\hat{s}/\xi$, m and n in Eq. (4.2.7).

- 3) Determination of ξ and $\hat{s}$. For value of $\hat{s}/\xi$ has been determined in step (2), value of ξ should be “guessed” such that the value of c will match condition: $c < 1$. And then value of $\hat{s}$ can be derived from $\hat{s}/\xi$ and guessed ξ .
- 4) Curve fitting of a , s_0 and h_0 by Eq. (4.2.8).

Based on the tensile and creep test of Sn-3.8Ag-0.7Cu and Sn-0.7Cu solder at different temperatures, strain rates or stress levels, nine constants in Anand model can be determined, as shown in Table 4.2-3. Commercial curve-fitting software Datafit 8.0 from Oakdale Engineering was used in curve-fitting of Anand model.

Table 4.2-3 Parameters in Anand model for Sn-3.8Ag-0.7Cu and Sn-0.7Cu

	A	Q/R	ξ	m	$\hat{s}$	n	h_0	a	s_0
Sn-3.8Ag-0.7Cu	65.92	6656	8	0.346	80.8	n1	h1	1.29	37.1
Sn-0.7Cu	9875	5276	2	0.176	65.2	n2	h2	1.03	33.8

The comparison of model prediction and the raw test data for Sn-3.8Ag-0.7Cu lead-free solder is shown in Fig. 4.2-3, 4.2-4 and 4.2-5. The separated points in the figures express the experimental results obtained in this study; the solid lines in the figures denote the calculated stress-strain curves with the values of parameters obtained in Anand model curve-fitting. It is recognized that calculated results can predict the tensile stress-strain curves very well. The curve-fit result for Sn-0.7Cu also gave good agreement with test data.

Fig. 4.2-3 Anand model curvefitting at strain rate of $5.6 \times 10^{-4} \text{ s}^{-1}$

Fig. 4.2-4 Anand model curvefitting at strain rate of $5.6 \times 10^{-3} \text{ s}^{-1}$

Fig. 4.2-5 Anand model curvefitting at strain rate of $5.6 \times 10^{-2} \text{ s}^{-1}$

Chapter 5. Creep Test Data & Analysis

In this chapter, the creep behavior for different temperatures and stress levels for the two lead-free solders were investigated. The steady state creep strain rate results were characterized by a hyperbolic sine creep constitutive model.

5.1 Creep test result

5.1.1 Creep behavior of lead-free solders

Creep tests of Sn-3.8Ag-0.7Cu and Sn-0.7Cu lead-free solders were carried out at several different temperatures with constant load set at several different stress levels. In all creep tests, the creep-time displays three stages, namely primary, secondary and tertiary creep. A typical curve is shown in Fig. 5.1-1. A typical strain rate versus time curve is shown in Fig. 5.1-2. Attention was focused on steady-state (secondary) creep since it dominates the creep rupture life of solder. Based on the curve, the creep rate can be determined for any given time by taking the derivative of the creep strain time. The minimum rate was taken as the creep strain rate of the steady-state stage.

Fig.5.1-1 Creep-time curve obtained at 25MPa, 25°C (Sn-0.7Cu)

Fig.5.1-2 Strain rate- time curve obtained at 5MPa, 25°C (Sn-0.7Cu)

By plotting all the strain-time curves under each condition into one graph, the effect of stress and temperature on the steady strain rate of lead-free solder alloy could be evaluated. The typical strain-time curves for Sn-0.7Cu solder, at a constant temperature of 125°C is shown in Fig. 5.1-3, and at a constant stress level of 7MPa is given in Fig. 5.1-4. It is noted that the steady strain rate of Sn-0.7Cu lead-free solders is strongly dependent on the test temperature and stress level. For Sn-3.8Ag-0.7Cu, the same trend can be found.

Fig.5.1-3 Creep-time curve at constant temperature of 125°C (Sn-0.7Cu)

Fig.5.1-4 Creep-time curve at constant stress level of 7MPa (Sn-0.7Cu)

5.1.2 95.5Sn-3.8Ag-0.7Cu solder alloy results

Table 5.1-1 summarizes the steady state creep test result which has been reported by Pang and Xiong et al [82-85]. The steady state creep strain rate against its applied normal stress data is plotted in Fig. 5.1-5. For Sn-3.8Ag-0.7Cu solder, it can be seen that when the temperature and applied normal stress increases, the steady state creep strain rate also increases.

Table 5.1-1 Summary of 95.5Sn-3.8Ag-0.7Cu creep test result

Stress	-40°C	25°C	75°C	125°C
2MPa	-	-	-	6.58E-8
3MPa	-	-	-	2.14E-7
5MPa	-	1.15E-9	3.2E-8	1.83E-6
7MPa	-	-	1.0E-7	1.07E-5
10MPa	-	1.0E-8	2.4E-7	3.37E-5
15MPa	-	8.91E-8	6.4E-6	1.57E-4
20MPa	-	1.4E-6	3.8E-5	3.2E-3
25MPa	1.92E-8	4.1E-6	1.58E-4	-
30MPa	1.74E-7	3.2E-5	-	-
35MPa	-	9.1E-5	1.04E-3	-
40MPa	5.5E-7	3.4E-4	-	-
50MPa	3.24E-6	-	-	-
60MPa	1.3E-5	-	-	-
70MPa	1.3E-4	-	-	-

Fig. 5.1-5 Steady-state creep behavior of 95.5Sn-3.8Ag-0.7Cu solder alloy

5.1.3 99.3Sn-0.7Cu solder alloy results

Creep properties of Sn-0.7Cu solder alloy has similar trend with Sn-3.8Ag-0.7Cu solder. The steady state creep strain rate increases with increase in temperature and stress level. The creep properties of Sn-0.7Cu solder is lower than those of the Sn-3.8Ag-0.7Cu solder alloy. The steady state creep strain rates of Sn-0.7Cu solder at different temperatures and stress levels are plotted in Fig. 5.1-6, and the results were summarized in Table 5.1-2.

Fig. 5.1-6 Steady-state creep behavior of 99.3Sn-0.7Cu solder alloy

Table 5.1-2 Summary of 99.3Sn-0.7Cu creep test result

<div>Strain Rate</div> <div>Stress</div>	25°C	75°C	125°C
3MPa	-	2.5E-8	5.21E-7
4MPa	-	-	1.56E-6
5MPa	8.91E-9	1.74E-7	4.07E-6
7MPa	6.03E-8	9.88E-7	1.35E-5
10MPa	3.27E-7	4.47E-6	7.59E-5
15MPa	2.95E-6	3.72E-5	5.6E-4
20MPa	2.96E-5	2.88E-4	1.09E-2
25MPa	1.86E-4	2.04E-3	-
30MPa	9.8E-4	1.35E-2	-
35MPa	7.94E-3	-	-

5.1.4 Comparison with other reported results

5.1.4.1 Comparison with tin-lead solder

Shi [11] reported the creep properties of 63Sn-37Pb solder at different temperatures and stress levels. The comparison of steady state creep strain rate for Sn-3.8Ag-0.7Cu, Sn-0.7Cu and 63Sn-37Pb [11] at room temperature and high temperature are shown in Fig. 5.1-7, and 5.1-8, respectively. It can be noticed that lead-free solder has the better creep resistance than tin-lead solder, while the creep property of Sn-Ag-Cu is better than Sn-Cu solder.

Fig. 5.1-7 Comparison of creep resistance at room temperature (25°C)

Fig. 5.1-8 Comparison of creep resistance at high temperature (125°C)

5.1.4.2. Comparison with other lead-free data

Some reported creep data [86-100] for Sn-3.8Ag-0.7Cu and other lead-free solder alloys were reviewed. Fig. 5.1-9 and 5.1-10 summarized creep data for Sn-Ag-Cu at room temperature (25°C) and high temperature (125°C). It was found that there is a order variances (1X) for different reported results (Morris, 2003 [96]; Lau, 2003 [101]; Schubert, 2001 [91]; Wiese. 2003 [97]; Pang and Xiong, 2004 [101-102]). Fig. 5.1-11 shows the comparison between the author's creep data with Morris's creep data [96]. The solder joint specimens were used in Morris's tests. The solder thickness is 160 microns and the samples were cooled at two cooling rates of 2.7°C/s and 3.5°C/s, respectively. It was found that the steady state creep strain rates for the

author's bulk solder data were comparable to the solder joint data of Morris [96] at 125-130°C [101-102]. Fig. 5.1-12 shows the author's Sn-Ag-Cu bulk creep data comparison with the NPL [98] solder joint creep data at room temperature and it was noted the result is also acceptable. The creep properties obtained from bulk specimens compares satisfactory with the solder joint creep results for Sn-Ag-Cu solder. However, few creep data for Sn-Cu solder was reported, the author's Sn-Cu data was compared with the data from Plumbridge [93] at 75°C in Fig. 5.1-13 and shows the similar trend.

Fig. 5.1-9 Sn-Ag-Cu steady state creep strain rate at 25°C

Fig. 5.1-10 Sn-Ag-Cu steady state creep strain rate at 125°C

Fig.5.1-11 Comparison of creep properties between author and Morris for Sn-Ag-Cu

Fig.5.1-12 Comparison of creep properties between author and NPL for Sn-Ag-Cu

Fig.5.1-13 Comparison of creep properties between author and Plumbridge for Sn-Cu

5.2 Creep models

Creep behavior is often characterized by its steady state creep strain rate, $\dot{\epsilon}_{ss}$, which can be simply expressed as power law relationship,

$$\dot{\epsilon} = A\sigma^n e^{\frac{-Q}{kT}} \quad (5.2.1)$$

where A is material constant, σ is applied stress, n is stress exponent, Q is creep activation energy, k is Boltzmann's constant, and T is absolute temperature. The activation energy, Q, and the stress exponent, n, changes with the dominant creep mechanism, and may have different values at different regimes of the applied stress. To describe the steady state creep strain rate at different regimes of stress and temperature, the hyperbolic-sine model is often used. The expressions of the models is,

$$\dot{\epsilon} = C[\sinh(\alpha\sigma)]^n \exp\left(-\frac{Q}{kT}\right) \quad (5.2.2)$$

The results of steady state creep strain rate depend on the normal stress and temperature for 95.5Sn-3.8Ag-0.7Cu and 99.3Sn-0.7Cu lead-free solders were used to curve fit to Eq. (5.2.2). Figs. 5.2-1 and 5.2-2 show the comparison of calculated steady state creep strain rates with the experimental data at different temperatures. The separated points in the figures express the experimental results obtained in this study; the solid lines in the figure denote the steady state creep strain rate curves with the values obtained in curve-fitting. It is recognized that calculated results based on Eq. (5.2.2) show fairly good agreement with experimental results.

After curve-fitting, the parameters for Sn-3.8Ag-0.7Cu and Sn-0.7Cu solder can be

determined, and were shown as,

Hyperbolic-sine model:

$$\dot{\epsilon}_{SnAgCu} = 501.3[\sinh(0.0316\sigma)]^{4.96} \exp\left(-\frac{5433.5}{T}\right) \tag{5.2.3}$$

$$\dot{\epsilon}_{SnCu} = 4.35[\sinh(0.096\sigma)]^{3.7} \exp\left(-\frac{4835.2}{T}\right) \tag{5.2.4}$$

Fig. 5.2-1Hyperbolic-sine model of 95.5Sn-3.8Ag-0.7Cu solder alloy

Fig. 5.2-2 Hyperbolic-sine model of 99.3Sn-0.7Cu solder alloy

Lau [99], Schubert and Pang [100] also reported their creep test data for Sn-Ag-Cu solder. Their curve-fitted results for the hyperbolic-sine creep model is shown below [83],

Lau (95.5Sn-3.9Ag-0.6Cu) $\dot{\epsilon} = 4.41 \times 10^5 [\sinh(0.005\sigma)]^{4.2} \exp(-5412/T)$ (5.2.5)

Schubert (95.5Sn-3.8Ag-0.7Cu) $\dot{\epsilon} = 2.78 \times 10^5 [\sinh(0.02447\sigma)]^{6.41} \exp(-6496/T)$ (5.2.6)

A comparison of the Sn-Ag-Cu solder material, specimen type, stress exponent and activation energy from Lau, Schubert and the author' s creep test result is given in Table 5.2-1. It is noted that the stress exponent n varies from 4.2 to 6.4, while the activation energy, Q, varies from 45KJ/mol - 54KJ/mol. A comparison of the steady state creep model using the equations (5.2.3), (5.2.5) and (5.2.6) are shown in Fig.

5.2-3. From the figure, it can be seen that the author’s creep data agree well with data reported by Lau. Satisfactory agreement with Schubert’s data was seen at low stresses, but some difference is noted at higher stresses above 10 MPa.

Table 5.2-1 Comparison of different reported creep test data for Sn-Ag-Cu

	Material	Specimen	Stress exponent n	Active energy Q (KJ/mol)
Author	95.5Sn3.8Ag0.7Cu	Cylindrical bulk specimen with gauge diameter of 3mm and gauge length of 15mm	4.96	45.2
Lau	95.5Sn3.9Ag0.6Cu	Compression specimen with diameter of 10mm and length of 19mm	4.2	45
Schubert	95.5Sn3.8Ag0.7Cu	Flat bulk specimen with 3×3mm cross section and gauge length of 30mm	6.4	54

Fig. 5.2-3 Comparison of steady-state creep behavior of different researchers for Sn-Ag-Cu

Chapter 6. Low Cycle Fatigue Test Data & Analysis

In this chapter, low cycle fatigue behaviors for the two lead-free solders tested over the range of temperatures, frequencies and strain levels were analyzed. Coffin-Manson and Morrow's models were used to characterize the low cycle fatigue behavior of the Sn-3.8Ag-0.7Cu and Sn-0.7Cu solder alloys.

6.1 Low Cycle Fatigue test result

6.1.1 Cyclic stress-strain behavior

After calculating cyclic stress and strain in each cycle, stress-strain hysteresis loop of Sn-0.7Cu and Sn-3.8Ag-0.7Cu solders at the tenth cycle for 2% total strain range at temperature of 125°C and frequency of 1Hz are shown in Fig. 6.1-1.

Fig. 6.1-1 Cyclic stress-strain hysteresis loops at the tenth cycle of fatigue test

For the same total strain range, Sn-0.7Cu solder has larger plastic range and smaller stress range than Sn-3.8Ag-0.7Cu solder. The results correspond to a greater tensile strength for Sn-3.8Ag-0.7Cu solder alloy as shown in Chapter 4. The plastic range

increased with the applied total strain range, and will increase slightly with the number of cycles, as shown in Fig. 6.1-2.

Fig. 6.1-2 Hysteresis loop at various cycles at 25°C, 7.5% and 0.01Hz of Sn-0.7Cu solder

The relationship between stress amplitude (one-half of the stress range) and number of cycles for Sn-0.7Cu and Sn-3.8Ag-0.7Cu solders for different total strain ranges at 125°C and 1Hz are shown in Fig. 6.1-3. Cyclic softening was observed for both lead-free solders. At the beginning of the fatigue test, stress amplitude reduces rapidly; after the first stage, stress amplitude shows slower reduction, which was defined as the second stage of the fatigue test; and finally, at the third stage, the stress reduction rate increases again and leads to final fracture. It is also can be noticed that the decrease rate of stress amplitude at secondary stage increases with the total strain range increases, which can be compared between Figs. 6.1-3 (a) and (b).

Fig. 6.1-3(a) Relationship between stress amplitude and number of cycles at 2% total strain range, 125°C and 1Hz

Fig. 6.1-3(b) Relationship between stress amplitude and number of cycles at 7.5% total strain range, 125°C and 1Hz

6.1.2 Effect of temperature on low cycle fatigue behavior

Test result of Sn-0.7Cu solder at different temperatures will show the effect of temperature on low cycle fatigue. Hysteresis loops at beginning of the second stage were selected to plot at different temperatures at strain range of 3.5% and frequency of 1Hz. The material response at different temperature can be evaluated and compared as shown in Fig.6.1-4. While the Sn-3.8Ag-0.7Cu solder has the similar trends with Sn-0.7Cu solder [103-104].

Fig. 6.1-4 Hysteresis loop at 1Hz and strain range of 3.5% for Sn-0.7Cu

The relationship between the fatigue life and plastic strain obtained from tests of 0.01Hz at three different temperatures (25, 75 and 125°C) is presented in Fig. 6.1-5. The fatigue life versus inelastic strain energy density plot is given in Fig. 6.1-6.

Fig. 6.1-5 Plastic strain versus fatigue life at 0.01Hz for different temperatures

Fig. 6.1-6 Inelastic strain energy density versus fatigue life at 0.01Hz for different temperatures

From Fig. 6.1-5 and 6.1-6, the values of constants for Coffin-Manson model and Morrow's energy-based model can be determined for different temperatures by taking the slope and the interception the plastic strain (inelastic strain energy density) axis. It was found that the value of m and C in Coffin-Manson model decreases with increasing temperature. For energy-based model, the same trend can be found.

6.1.3 Effect of Frequency on low cycle fatigue behavior

The fatigue test result of Sn-0.7Cu solder will show the frequency on low cycle fatigue. By plotting the hysteresis loop of different frequency at 125°C and strain range of 7.5%, the material response at different temperature can be evaluated and compared (Fig. 6.1-7). Sn-3.8Ag-0.7Cu solder has the similar trend.

Fig. 6.1-7 Hysteresis loop at 125°C and strain range of 7.5% for Sn-0.7Cu

After conducting the tests at the same temperature and total strain but at different frequencies, the fatigue life of lead-free solder was found to decrease with decreasing frequency. This characteristic of fatigue life can be attributed to accumulate creep damage during fatigue testing. As the frequency decreases, the time for each cycle increases, and this allow more time for creep to develop and thus leads to lower fatigue life in terms of cycles to failure.

As can be seen from Fig. 6.1-8 and 6.1-9, the Coffin-Manson model and energy-based model can be used to describe the fatigue behavior of lead-free solder for any given frequency. However, the fatigue results have some difference at different frequencies, the value of fatigue exponent m and ductility coefficient C changes as frequency changes. It was found that, for both models, the m value decrease with frequency, but the frequency dependent is small. However, the C value decreases significantly as the frequency decreases, and is strongly frequency dependent.

Fig. 6.1-8 Plastic strain versus fatigue life at 125°C for different frequencies

Fig.6.1-9 Inelastic strain energy density versus fatigue life at 125°C for different frequencies

6.1.4 Comparison with other reported results

6.1.4.1 Comparison with tin-lead solder

Shi [51-52] reported the fatigue properties for 63Sn-37Pb solder at different temperatures and frequencies. The comparison of fatigue resistance for Sn-3.8Ag-0.7Cu, Sn-0.7Cu and 63Sn-37Pb [51-52] at room temperature & high frequency and high temperature & low frequency are shown in Fig 6.1-10, and 6.1-11, respectively. It can be noticed that lead-free solder has the better fatigue resistance than tin-lead solder, while the fatigue property of Sn-Ag-Cu is better than Sn-Cu solder.

Fig. 6.1-10 Comparison of fatigue resistance at room temperature and 1Hz

Fig. 6.1-11 Comparison of fatigue resistance at high temperature (125°C) and 10³Hz

6.1.4.2 Comparison with other lead-free data

Reported studies (Mavoori, 1994 [26]; Kariya, 1998 [28]; Kanchanomai, 2002 [33-35]) have studied that the low cycle fatigue behavior of lead-free and lead-bearing solder alloys. Fig. 6.1-12 shows the fatigue test result at room temperature and 1Hz of different reported data of lead-free and lead-bearing solder alloys. The fatigue failure was defined as 50% reduction of maximum tensile load. From Fig. 6.1-12, it can be noticed that the conventional tin-lead solder has the lowest fatigue life at the same test condition, three types of lead-free solder: 99.3Sn-0.7Cu, 97Sn-3Ag and 95.5Sn-3.8Ag-0.7Cu solder all have better fatigue property than 63Sn-37Pb solder at room temperature and 1Hz. However, for lead-free solder alloys, the fatigue life of 99.3Sn-0.7Cu is lower than the other two lead-free solder alloys,

while 97Sn-3Ag and 95.5Sn-3.8Ag-0.7Cu solder have similar fatigue life [103-104].

Fig. 6.1-12 Comparison of LCF data for solder alloys at room temperature and 1Hz

Isothermal LCF test data for Sn-Ag, Sn-Ag-Cu lead-free solders at 0.1Hz and room temperature were reported by Kanchanomai et al [33-35]. Their failure criteria were defined at the 25% load drop of the stress amplitude. Comparison with other LCF data by Mavoori, and Kariya, at 1Hz and room temperature, is shown in Fig. 6.1-13. It can be seen that at the same test condition, Sn-Ag and Sn-Ag-Cu have comparable fatigue life. However, the fatigue life data from Kanchanomai [35], at 0.1Hz and with a failure definition of 25% load drop, is lower than the result by Mavoori [26] and Kariya [28] and the author's data. Fatigue ductility exponent (m) and fatigue ductility coefficient (C) in the Coffin-Manson model for these solder alloys at room temperature are summarized in Table 6-1.

Fig. 6.1-13 Comparison of LCF data for lead-free solders for different fatigue criterions

Table 6-1 Coffin-Manson parameters of lead-free solders at room temperature

	m	C
SnAg [Kanchanomai] (25°C and 0.1Hz)	0.93	21.9
SnAgCu [Kanchanomai] (25°C and 0.1Hz)	0.73	3.7
SnAgCu [Kariya] (25°C and 1Hz)	0.75	6.4
SnAg [Mavoori] (25°C and 1Hz)	0.45	0.57

In recent years, some researchers also conducted the isothermal fatigue tests for real solder joints (Kariya, 2004 [106]; Lau, 2004 [107] ; Lin, 2004 [108]). Kariya et al [106] conducted shear fatigue tests of Sn-1Ag-0.5Cu, Sn-3Ag-0.5Cu and Sn-1.2Ag-0.5Cu-0.05Ni lead-free solder for flip chip interconnections. The Coffin-Manson relations for each alloy are,

$$\text{For Sn-1Ag-0.5Cu:} \quad \Delta \varepsilon_{in} N_f^{0.62} = 1.4 \quad (6.1.1)$$

$$\text{For Sn-3Ag-0.5Cu:} \quad \Delta \varepsilon_{in} N_f^{0.45} = 0.78 \quad (6.1.2)$$

$$\text{For Sn-1.2Ag-0.5Cu-0.05Ni:} \quad \Delta \varepsilon_{in} N_f^{0.44} = 0.78 \quad (6.1.3)$$

Lin et al [108] also investigated Sn-3.5Ag, Sn-0.7Cu and Sn-3.8Ag-0.7Cu solder for flip chip applications. It was found that the fatigue life is dependent on failure mode. The life is longer when the failure was through the bulk of solder; however, fatigue life will be very short if failure occurred in the interface.

Lau et al [107] studied 95.5Sn-3.9Ag-0.5Cu lead-free solder for a solder-bumped WLCSP, load control was used in isothermal fatigue tests. The relationship between the fatigue life and strain energy density is shown as,

$$N_f = 18.15(\Delta W)^{-1.96} \quad (6.1.4)$$

Fig. 6.1-14 shows the strain control fatigue behavior comparison of author's bulk specimen and other solder joint specimens (Kariya, 2004 [106]; Lin, 2004 [108]). It was found that author's bulk data has fairly good comparison with other solder joints data from real packaging assembly.

Fig. 6.1-14 Fatigue behavior comparison of bulk solder and solder joint

6.2 Low cycle fatigue models

The Coffin-Manson model [38-39] has been widely used to relate low cycle fatigue life (N_f) of metallic materials with the plastic strain range ($\Delta\epsilon_p$), as shown below:

$$N_f^m \Delta\epsilon_p = C \quad (6.2.1)$$

where m and C are material constants.

The Morrow's energy-based model [105] was also used to predict low cycle fatigue lives. The model predicts fatigue life in terms of inelastic strain energy density (W_p), given below:

$$N_f^n W_p = A \quad (6.2.2)$$

where n is fatigue exponent, and A is material ductility coefficient. The inelastic strain energy density was determined from the area surrounded by a stable hysteresis loop.

Based on the low cycle fatigue test result at different temperatures and frequencies,

the m , C , n and A at different conditions can be determined for 95.5Sn-3.8Ag-0.7Cu and 99.3Sn-0.7Cu lead-free solders. The results are summarized in Table 6.2-1 and 6.2-2.

Table 6.2-1(a) m and C for Coffin-Manson model of Sn-3.8Ag-0.7Cu

	m			C		
	25°C	75°C	125°C	25°C	75°C	125°C
1Hz	0.913	0.896	0.889	26.3	19.8	16.0
0.01Hz	0.904	0.889	0.871	20.7	16.0	12.1
0.001Hz	0.891	0.876	0.853	13.9	11.5	9.2

Table 6.2-1(b) n and A for Morrow's model of Sn-3.8Ag-0.7Cu

	n			A		
	25°C	75°C	125°C	25°C	75°C	125°C
1Hz	1.103	1.079	0.953	14865	6208.3	1492.8
0.01Hz	0.973	0.944	0.926	1426.2	1144.3	578.9
0.001Hz	0.935	0.914	0.897	1144.4	666.9	311.7

Table 6.2-2(a) m and C for Coffin-Manson model of Sn-0.7Cu

	m			C		
	25°C	75°C	125°C	25°C	75°C	125°C
1Hz	0.9734	0.9227	0.9022	21.27	12.51	9.98
0.01Hz	0.8067	0.7938	0.7825	5.89	4.46	3.33
0.001Hz	–	–	0.7192	–	–	1.98

Table 6.2-2(b) n and A for Morrow’s model of Sn-0.7Cu

	n			A		
	25°C	75°C	125°C	25°C	75°C	125°C
1Hz	1.2157	1.1406	1.1064	9542.9	2864.8	1387.8
0.01Hz	1.1396	1.0084	0.8379	1524.8	559.46	143.71
0.001Hz	–	–	0.7328	–	–	38.64

To model frequency dependent low cycle fatigue behavior of Sn-3.8Ag-0.7Cu and Sn-0.7Cu lead-free solders, the frequency-modified Coffin-Manson relationship [51] can be introduced to describe the low cycle fatigue behavior of Sn-0.7Cu solder, given below.

$$\left[N_f \nu^{(k-1)}\right]^m \Delta \epsilon_p = C \tag{6.2.3}$$

where ν is frequency, k , is frequency exponent. Based on the fatigue test results at different frequencies at 125°C, the frequency exponent, k , can be determined to be 0.95 and 0.91 for Sn-3.8Ag-0.7Cu and Sn-0.7Cu solder, respectively. Then the frequency modified fatigue life $N_f \nu^{(k-1)}$ can be calculated. When the plastic strain was plotted against the frequency-modified fatigue life, all the fatigue life data obtained at different frequencies were found to fit well into a single line, as shown in Fig. 6.2-1 and 6.2-2. This means that the frequency-modified Coffin-Manson model can be used to model the effect of frequency for the low cycle fatigue behavior of Sn-3.8Ag-0.7Cu and Sn-0.7Cu solder.

Similarly, the frequency-modified Morrow model can be used to model the frequency effect, as given below:

$$\left[N_f \nu^{(h-1)} \right]^n W_p = A \quad (6.2.4)$$

where ν is the frequency, h is frequency exponent. Based on fatigue test of Sn-3.8Ag-0.7Cu and Sn-0.7Cu solder at different frequencies, the frequency exponent, h , can be determined to be 0.82 and 0.762, respectively. Figures 6.2-3 and 6.2-4 show the inelastic strain energy density plotted against the frequency-modified fatigue life at 125°C. It can be seen that all fatigue life data at different frequencies falls on a single line. Hence, the frequency-modified Morrow model can be used to model the effect of frequency for the low cycle fatigue behavior of lead-free Sn-3.8Ag-0.7Cu and Sn-0.7Cu solder.

Fig. 6.2-1 Plastic strain versus frequency-modified fatigue life at 125°C for Sn-Ag-Cu (k=0.95)

Fig. 6.2-2 Plastic strain versus frequency-modified fatigue life at 125°C for Sn-Cu (k=0.91)

6.2-3 Inelastic strain energy density versus frequency-modified fatigue life at 125°C for Sn-Ag-Cu (h=0.82)

Fig. 6.2-4 Inelastic strain energy density versus frequency-modified fatigue life at 125°C for Sn-Cu (h=0.762)

Chapter 7. Research on New Visco-plastic Model, Fatigue Model and Impact Yield Stress for 95.5Sn-3.8Ag-0.7Cu Solder

This chapter reports on new developments in (i) A visco-plastic constitutive model, which deals with the hardening-softening behavior; (ii) A fatigue model based on a damage parameter (load drop rate, $\frac{d\Phi}{dN}$), which compensates for temperature and frequency effects; (iii) Yield stress equation combining impact and tensile test results, covering a wide range of strain rate from 10^{-4} to 10^3 s^{-1} .

7.1 New visco-plastic model for 95.5Sn-3.8Ag-0.7Cu solder

A new visco-plastic constitutive model has been developed in this study, and applied to predict the visco-plastic behavior of Sn-3.8Ag-0.7Cu lead-free solder. This model can deal with both hardening and softening effect.

7.1.1 Model Formulation

Based on the theory of plasticity [109-110], under isothermal, constant strain rate condition, for fully developed flows where $\dot{\epsilon} \approx \dot{\epsilon}_p$, the expression of incremental plastic flow hardening (or softening) form can be expressed as,

$$\frac{d\sigma}{d\epsilon} = H \quad (7.1.1)$$

where H consists all the physical mechanisms that affect the hardening (or softening) of the plastic flow, such as strain hardening, dynamic recovery, static recovery and internal damage, etc. However, for solder materials, the most two important mechanisms are dynamic recovery and strain hardening [12-13], then Eq. (7.1.1) can be represented as,

$$\frac{d\sigma}{d\varepsilon} = H(\sigma_{dr}, \varepsilon) \quad (7.1.2)$$

where σ_{dr} is an internal variable, with dimension of stress to represent the dynamic recovery stress; and ε is the effect of strain hardening.

Though the strain hardening and dynamic recovery can be modeled by a combined dynamic hardening term, it will be more appropriate to study the visco-plastic behavior of solder material if these two effects can be studied separately. Then the hardening formulation in this model can be expressed as,

$$\frac{d\left(\frac{\sigma}{\sigma_{dr}}\right)}{d\varepsilon} = h(\varepsilon) \quad (7.1.3)$$

In Eq. (7.1.3), $h(\varepsilon)$ was associated with strain hardening only, because the dynamic recovery effect in former function H has been described by σ_{dr} and moved to the left side of the formula. It is also interesting to find that, σ_{dr} has the dimension of stress, and then $\frac{\sigma}{\sigma_{dr}}$ is dimensionless. It is reasonable to consider h as the function of ε , which is also dimensionless, at the right of the expression.

7.1.1.1 Evaluation of dynamic recovery stress σ_{dr}

Dynamic recovery can be viewed as creep occurring at the high strain rates. The true stress-strain behavior of a material experiencing only dynamic recovery is illustrated in Fig. 7.1-1. It can be seen that the overall level of the flow stress curve increases with increase in strain rate and decrease with increase in temperature. The stress increases with further strain, eventually obtaining a steady-state value (σ_{ss}). During the transient period, a steady-state microstructure is developing in much the same way it does during steady-state creep [111]. This means the flow stress equation can be used to describe the saturation stress, σ_{ss} . The flow stress equation can be expressed from the steady state creep strain rate expression,

$$\dot{\epsilon} = A e^{-Q/RT} \left[\sinh\left(\frac{\sigma}{B}\right) \right]^{1/m} \quad (7.1.4)$$

The static stress is taken as the saturation stress, σ_{ss} , which is the function of strain rate and absolute temperature,

$$\sigma_{ss} = B \sinh^{-1} \left[\left(\frac{\dot{\epsilon}}{A} e^{Q/RT} \right)^m \right] \quad (7.1.5)$$

The dynamics recovery stress is assumed to be equal to the saturation stress,

$$\sigma_{dr} = \sigma_{ss} = B \sinh^{-1} \left[\left(\frac{\dot{\epsilon}}{A} e^{Q/RT} \right)^m \right] \quad (7.1.6)$$

where A, B are material constants, Q is activation energy, m is creep exponent.

Fig.7.1-1 Schematic of the stress-strain behavior under dynamic recovery

7.1.1.2 Evaluation of hardening-softening parameter σ_{h-s}

In section 7.1.1.1, the dynamic recovery stress, σ_{dr} , was assumed to be equal to the creep constant stress or saturation stress, σ_{ss} . It is true only if the ultimate tensile strength (UTS) is not reached and no softening behavior is noted. That means the constitutive model only can predict the small strain part of the stress-strain curves. As we know, though the stress will increase with strain in hardening part, it will reach its maximum limit at ultimate tensile strength (UTS). After that, the stress-strain behavior goes into the softening part as it curves downwards. In order to represent the complete hardening-softening behavior, the dynamic recovery stress, σ_{dr} should be extended to model both hardening and softening effects, denoted by the parameter, σ_{h-s} , and expressed as,

$$\sigma_{h-s} = \sigma_{h-s}(\sigma_{ss}, \varepsilon) \quad (7.1.7)$$

Eq. (7.1.7) shows that the hardening-softening parameter is not only dependent on saturation stress, but the strain as well. The formation of $\sigma_{h-s}(\sigma_{ss}, \varepsilon)$ which is adopted to represent the hardening-softening behavior is,

$$\sigma_{h-s} = \sigma_{ss} - \sigma_{ss} \frac{|\varepsilon - b|}{\varepsilon + c} \quad (7.1.8)$$

In physical terms, the hardening-softening parameter σ_{h-s} denotes the maximum stress the material can bear at a given strain rate, temperature and strain. In the hardening part, it will increase with strain and go to the maximum value till $\varepsilon = b$. When $\varepsilon > b$, it goes into the softening part, σ_{h-s} will decrease with strain.

7.1.1.3 Evaluation of strain hardening function $h(\varepsilon)$

The increase in the stress because of previous deformation is known as strain hardening, or work hardening. A power law relationship was used to describe the strain hardening, as shown in Eq. (7.1.9),

$$\sigma = K\varepsilon^n \quad (7.1.9)$$

where n is the strain-hardening exponent and K is the strength coefficient. While in this study, a new relationship that considers the initial strain is proposed. The form of $h(\varepsilon)$ which is adopted to represent the strain hardening behavior with the initial strain effect is,

$$h(\varepsilon) = \frac{a}{(a + \varepsilon - \varepsilon_i)^2} \quad (7.1.10)$$

where a is the strain hardening parameter, ε_i is the initial strain, which describe the strain history of the material.

7.1.1.4. Summary of model formulation

Combining Eqs. (7.1.3), (7.1.6), (7.1.8) and (7.1.10), the new model can be summarized as:

Hardening-softening equation:

$$\frac{d\left(\frac{\sigma}{\sigma_{h-s}}\right)}{d\varepsilon} = \frac{a}{(a + \varepsilon - \varepsilon_i)^2} \quad (7.1.11)$$

Hardening-softening parameter:

$$\sigma_{h-s} = \sigma_{ss} - \sigma_{ss} \frac{|\varepsilon - b|}{\varepsilon + c} \quad (7.1.12)$$

where $\sigma_{dr} = \sigma_{ss} = B \sinh^{-1} \left[\left(\frac{\dot{\varepsilon}}{A} e^{Q/RT} \right)^m \right]$

Integrated form of Eq. (7.1.11) is:

$$\sigma = \sigma_{ss} \left(1 - \frac{|\varepsilon - b|}{\varepsilon + c} \right) \frac{\varepsilon - \varepsilon_i}{a + \varepsilon - \varepsilon_i} \quad (7.1.13)$$

where ε_i is the initial strain at the point $\sigma = 0$.

If only hardening effect was considered, Eq. (7.1.13) can be simplified to the form as,

$$\sigma = \sigma_{dr} \frac{\varepsilon - \varepsilon_i}{a + \varepsilon - \varepsilon_i} \quad (7.1.14)$$

7.1.2 Parameter determination

There are four parameters involved in formulation of saturation stress and three parameters involved in strain-stress formulation. Therefore, there are seven material parameters, A , B , Q/R , m , a , b and c to be determined for this model.

Stress-strain curves can be built from tensile test data with zero initialized stress state. However, if only tensile data is used for curve fitting, loading-unloading behavior could not be represented by the model. Therefore, some load-unload-reload test results were used to show the stress-strain behavior where initial strain need not be zero ($\varepsilon_i \neq 0$). The normal step to determine the seven parameters of this model is as follows,

- 1) Determination of saturation stress from steady state creep relation.
- 2) Nonlinear curve fitting of A , B , Q/R , m in Eq. 7.1.6.
- 3) Nonlinear curve fitting of a , b and c in Eq. 7.1.13. At least one non-zero initialized strain curve must be used. In step 3), parameters determined in step 1) will be used. Similarly, if only hardening effect was considered, parameter a can be fitted from nonlinear fitting of Eq. 7.1.14.

Based on the test result of Sn-3.8Ag-0.7Cu, seven material constants for hardening-softening model and five material constants for hardening model were determined, shown in Table 7.1-1.

Table 7.1-1: Material constants for Sn-3.8Ag-0.7Cu

	A	Q/R	B	m	a	b	c
Hardening-softening	18.59	5645	13.1	0.3	a1	7.4×10^{-3}	0.778
Hardening	18.59	5645	13.1	0.3	a2	-	-

The comparison of model prediction and the raw data for Sn-3.8Ag-0.7Cu is shown in Fig. 7.1-2 and 7.1-3. Fig. 7.1-2 shows the results of simple tensile tests, while Fig. 7.1-3 shows load-unload test results. The separated points in the figures express the experimental results obtained in this study; the solid lines in the figures denote the calculated stress-strain curves with the values obtained in curve-fitting. From Fig. 7.1-2, it is recognized that calculated results show fairly good agreement with experimental results in both hardening and softening parts; however, from Fig. 7.1-3, it can be seen that new developed model can predict not only the simple tensile stress-strain curves, but also the load-unload curves.

Fig. 7.1-2(a) Hardening-softening stress-strain behavior at strain rate of $5.6 \times 10^{-4} \text{ s}^{-1}$

Fig. 7.1-2(b) Hardening-softening stress-strain behavior at strain rate of $5.6 \times 10^{-3} \text{ s}^{-1}$

Fig. 7.1-2(c) Hardening-softening stress-strain behavior at strain rate of $5.6 \times 10^{-2} \text{ s}^{-1}$

Fig. 7.1-3(a) Load-unload test at 25°C and $5.6 \times 10^{-4} \text{ s}^{-1}$

Fig. 7.1-3(b) Load-unload test at 25°C and $5.6 \times 10^{-2} \text{ s}^{-1}$

Fig. 7.1-3(c) Load-unload test at 125°C and $5.6 \times 10^{-4} \text{ s}^{-1}$

Fig. 7.1-3(d) Load-unload test at 125°C and $5.6 \times 10^{-3} \text{ s}^{-1}$

7.2 New load drop rate fatigue model for 95.5Sn-3.8Ag-0.7Cu solder

From Chapter 6, it was found that the fatigue exponent m (or n) and ductility coefficient C (or A) are dependent on temperature and frequency in the traditional Coffin-Manson or Morrow fatigue models. Although the frequency modified model solves the frequency dependent effect, it is still difficult to characterize the temperature and frequency dependent low cycle fatigue behavior of solder alloys in the thermal-mechanical loading conditions. Furthermore, the plastic strain range or inelastic strain energy density used in Coffin-Manson or Morrow's model is based on an approximated "stable" hysteresis loop. However, from Fig. 6.1-2 and 6.1-3, it is noted that there is no "stable" hysteresis loop during the fatigue test of Pb-free solder alloys. The cyclic properties will change during the fatigue period, it may not be reasonable to use the initial cyclic properties to characterize the long-term fatigue life. In this study, a new fatigue model based on load drop rate was developed to characterize the low cycle fatigue behavior of Sn-3.8Ag-0.7Cu lead-free solder alloy.

7.2.1 Strain range, temperature and frequency dependent load drop rate

During the fatigue test, the amplitude of the stress will decrease as shown in Fig. 7.2-1. It was observed that the total fatigue life could be divided into three stages based on the change of the load drop rate. At the beginning of the fatigue test, stress amplitude reduces rapidly, which may be due to cyclic softening and crack initiation process. After crack initiation, stable cracks propagation will increase with fatigue cycles. This propagation mechanism causes a linear reduction of the stress amplitude,

defined as the second stage of the fatigue failure process. Thirdly, final failure occurs as the load drop rate increases rapidly leading to fatigue fracture. In Fig. 7.2-1, it can be noted that the second stage is the dominated stage during the fatigue life. It was also found that the load drop rate at this stage depends on total strain range, temperature and frequency as shown in Figs. 7.2-2 to 7.2-4. For example, Fig. 7.2-2 shows the Sn-3.8Ag-0.7Cu solder results tested at 25°C and 0.01Hz for different strain ranges (from 2%-7.5%).

The load drop rate at the second stage is defined as $\frac{d\Phi}{dN}$, where $\Phi = \sigma / \sigma_0$, σ_0 is the peak stress at the beginning of the 2nd stage of the fatigue process (See Fig. 7.2-1).

Fig. 7.2-1 Definition of load drop rate

Fig. 7.2-2 Effect of total strain range on load drop rate

Fig. 7.2-3 Effect of temperature on load drop rate

Fig. 7.2-4 Effect of frequency on load drop rate

By plotting the load drop rate $\frac{d\Phi}{dN}$ with the strain range, temperature and frequency, it was found that the load drop rate at the second stage has a power law relationship with total strain range, a linear relationship with temperature and logarithmic relationship with frequency, as seen in Figs. 7.2-5 to 7.2-7.

Fig. 7.2-5 Power law relationship of total strain range and load drop rate at 0.01Hz

Fig. 7.2-6 Linear relationship of temperature and load drop rate at 1Hz

Fig. 7.2-7 Logarithmic relationship of frequency and load drop rate at 75°C

7.2.2 Load drop rate damage model

From the damage mechanics point of view, load drop is due to accumulated damage in the material during the fatigue test duration. The total damage consists of two major parts, fatigue damage and creep damage. The time-dependent creep-fatigue damage model [112-113] can be expressed as,

$$\dot{D}_{total} = D_f |\dot{\sigma}| + \dot{D}_c \quad (7.2.1)$$

For fatigue damage, D_f , can be written as

$$D_f = C_f |\sigma|^{m_f} (1 - D)^{-k} \quad (7.2.2)$$

where $D = 1 - \Phi$, C_f and m_f are material constants.

For creep damage rate, $\dot{D}_c$, can be written as

$$\dot{D}_c = C_c |\sigma|^{m_c} (1 - D)^{-k} \quad (7.2.3)$$

where C_c and m_c are material constants.

So Eq. (7.2.1) can be rewritten as

$$\dot{D}_{total} = (C_f |\sigma|^{m_f} |\dot{\sigma}| + C_c |\sigma|^{m_c}) (1 - D)^{-k} \quad (7.2.4)$$

where $\dot{D}_{total}$ is the total damage rate.

While the stress-strain relation during the low cycle fatigue test can be assumed as

$$\sigma = (aT + b) \dot{\epsilon}^{n_1} (\Delta \epsilon)^{n_2} \quad (7.2.5)$$

where a, b, n_1 and n_2 are material constants, T is temperature in $^{\circ}\text{C}$, $\dot{\epsilon}$ is strain rate, $\Delta \epsilon$ is the strain range.

Integrating Eq. (7.2.4) with respect to time t , for simplification, let $k=0$,

$$\oint_{cycle} dD_{total} = \oint_{cycle} C_f |\sigma|^{m_f} d|\sigma| + \oint_{cycle} C_c |\sigma|^{m_c} dt \quad (7.2.6)$$

$$\oint_{cycle} C_f |\sigma|^{m_f} d|\sigma| = \frac{4C_f (aT + b)^{m_f+1}}{m_f + 1} \dot{\epsilon}^{n_1(m_f+1)} (\Delta \epsilon)^{n_2(m_f+1)} \quad (7.2.7)$$

$$\begin{aligned} \oint_{cycle} C_c |\sigma|^{m_c} dt &= 2C_c \int_0^{\Delta \epsilon} (aT + b)^{m_c} [\dot{\epsilon}^{n_1} (\Delta \epsilon_{current})^{n_2}]^{m_c} dt \\ &= 2C_c (aT + b)^{m_c} \dot{\epsilon}^{n_1 m_c} \int_0^{\Delta \epsilon} (\dot{\epsilon})^{n_2 m_c} dt \\ &= \frac{2C_c (aT + b)^{m_c}}{n_2 m_c + 1} \dot{\epsilon}^{n_1 m_c - 1} (\Delta \epsilon)^{n_2 m_c + 1} \end{aligned} \quad (7.2.8)$$

$$\oint_{\text{cycle}} dD_{\text{total}} = \frac{\Delta D_{\text{total}}}{\Delta N} \quad (7.2.9)$$

So Eq. (7.2.6) can be rewritten as

$$\begin{aligned} \frac{\Delta D_{\text{total}}}{\Delta N} = & \frac{4C_f (aT + b)^{m_f+1}}{m_f + 1} \dot{\epsilon}^{n_1(m_f+1)} (\Delta \epsilon)^{n_2(m_f+1)} \\ & + \frac{2C_c (aT + b)^{m_c}}{n_2 m_c + 1} \dot{\epsilon}^{n_1 m_c - 1} (\Delta \epsilon)^{n_2 m_c + 1} \end{aligned} \quad (7.2.10)$$

In damage mechanics, $D = 1 - \Phi$, which means

$$\frac{\Delta D}{\Delta N} = -\frac{d\Phi}{dN} \quad (7.2.11)$$

Then the simplification of Eq. (7.2.10) can be expressed as

$$-\frac{d\Phi}{dN} = \frac{\Delta D}{\Delta N} = (-a_f T + b_f) \nu^{m_f} (\Delta \epsilon)^{n_f} + (a_c T + b_c) \nu^{-m_c} (\Delta \epsilon)^{n_c} \quad (7.2.12)$$

In Eq. (7.2.12), the first term on the right side is the contribution of fatigue damage, the second term is the contribution of the creep damage. It can be found that if frequency decrease, ν^{m_f} in the first term will be smaller, while ν^{-m_c} in the second term will increase. Similarly, when temperature increase, the first term will also decrease because of negative value of $-a_f$, the second term will increase with the increase with temperature. That means the creep damage will be more dominant at the low frequency and high temperature, while the fatigue damage will be more important at high frequency and low temperature.

Based on the decrease rate at different strain range, temperature and frequency, the load drop model for Sn-3.8Ag-0.7Cu solder alloy is,

$$-\left(\frac{d\Phi}{dN}\right)_{SnAgCu} = (-2.4 \times 10^{-4}T + 9.13)\nu^{0.179}(\Delta\epsilon)^{4.14} + (8.8 \times 10^{-5}T + 0.0055)\nu^{-0.126}(\Delta\epsilon)^{1.29} \quad (7.2.13)$$

Based on the fatigue test result of Sn-3.8Ag-0.7Cu solder alloy, it was found that decrease rate of peak stress, $\frac{d\Phi}{dN}$, has a power law relationship with fatigue life.

$$N_f^m \left(-\frac{d\Phi}{dN} \right) = C \quad (7.2.14)$$

Fig. 7.2-8 shows the log-log plot of decrease rate of peak stress and fatigue life, it can be found that fatigue lives at different temperatures and frequencies all follow to a master curve, which means the fatigue exponent m and ductility coefficient C in decrease rate model is independent on temperature and frequency. The m and C in load drop model for Sn-3.8Ag-0.7Cu solder alloy is 0.818 and 0.121, respectively.

Fig. 7.2-8 Load drop rate model for low fatigue life of Sn-3.8Ag-0.7Cu

7.3 Impact properties and high strain rate model for 95.5Sn-3.8Ag-0.7Cu solder

Impact test were conducted with a Split Hopkinson pressure bar (SHPB) to study the Sn-3.8Ag-0.7Cu lead-free solder behavior under high strain rates. The stress and strain could be measured and calculated based on stress wave theory [114]. Upon the incident pulse hitting the specimen, it is split into reflected and transmitted pulse. Based on the strain gauge readings of incident, reflected and transmitted pulses, stress and strain during the impact tests can be determined. Typical pulse shape and relationship among incident, reflected and transmitted pulses are shown in Fig. 7.3-1 and 7.3-2.

Fig.7.3-1 Typical pulse shape of SHPB test

Fig.7.3-2 Typical relationship among incident, reflected and transmitted pulse

By plotting all stress-strain curves into one graph, the effect of strain rate on the Sn-3.8Ag-0.7Cu solders tensile properties of impact tests could be evaluated and compared. The stress-strain curves of Sn-3.8Ag-0.7Cu at room temperature and different strain rates (7×10^2 , 9×10^2 and $1.3 \times 10^3 \text{ s}^{-1}$) are shown at Fig. 7.3-3. The Elastic modulus and Yield stress at different strain rate are summarized in Table 7.3-1.

Table 7.3-1 Impact results of Sn-3.8Ag-0.7Cu lead-free solders

Strain rate	Sn-3.8Ag-0.7Cu	
	E (GPa)	Yield (MPa)
$7 \times 10^2 \text{ s}^{-1}$	52.8	129
$9 \times 10^2 \text{ s}^{-1}$	53.3	175
$1.3 \times 10^3 \text{ s}^{-1}$	54.0	300

Fig. 7.3-3 Impact stress-strain curves for Sn-3.8Ag-0.7Cu

The temperature and strain rate dependent yield stress equations for Sn-3.8Ag-0.7Cu lead-free solder alloys at normal tensile tests have been described in Eq. (4.2.3). From impact test results, it was also found the mechanical properties of solders at high strain rates (such as impact tests) are dependent on strain rates as well. However, the yield stress equations for normal tensile tests only can predict the yield stress at low

strain rate, if the strain rate is as high as in the impact test (10^2 s^{-1} to 10^3 s^{-1}), the equations are not valid any longer. There is a big difference between the test data and predicted values. The reason is, for most materials, the yield stress will have the dramatic increase at high strain rates ($10^2 \text{ s}^{-1} \sim 10^4 \text{ s}^{-1}$) [115]. The strain rate dependence of yield stress at constant temperature is shown in Fig. 7.3-4.

Fig. 7.3-4 Schematic of strain rate dependent yield stress

From Fig. 7.3-4, it can be found that the yield stress have a linear relationship with logarithmic strain rate at low strain rate, so Eqs (4.2.3) can predict the yield stress quite well for normal tensile test. But this linear relationship could not be used to describe the yield stress over the wide range ($10^{-4} \text{ s}^{-1} \sim 10^4 \text{ s}^{-1}$), because the yield stress will increase dramatically when the strain rate reaches the higher level ($10^2 \text{ s}^{-1} \sim 10^4 \text{ s}^{-1}$). The dramatic increase part should be added into the constitutive model to predict the strain rate dependent yield stress over a wide range. The increase part can be described as Eq. (7.3.1),

$$\sigma_{increase} = B\dot{\epsilon}^m \quad \dot{\epsilon} \geq 10^2 \quad (7.3.1)$$

Based on the impact result at room temperature and three different strain rates, the values of constant B and exponent m can be decided. Combining with the Eqs. (4.2.3), the strain rate dependent yield stress at room temperature over a wide strain rate range ($10^{-4} \text{ s}^{-1} \sim 10^4 \text{ s}^{-1}$) for Sn-3.8Ag-0.7Cu can be described as Eq. (7.3.2).

$$\sigma_y(\dot{\epsilon})_{SnAgCu} = \begin{cases} 64.1\dot{\epsilon}^{0.082} & 10^{-4} \leq \dot{\epsilon} < 10^2 \\ 64.1\dot{\epsilon}^{0.082} + 1.44 \times 10^{-5} \dot{\epsilon}^{2.22} & \dot{\epsilon} \geq 10^2 \end{cases} \quad (7.3.2)$$

The experimental value and model value are compared in Figs. 7.3-5.

Fig. 7.3-5 Strain rate dependent yield stress for Sn-3.8Ag-0.7Cu

Chapter 8. Application of 95.5Sn-3.8Ag-0.7Cu Visco-plastic Model to Micro-Deformation Analysis of Micro-BGA Assembly

In this chapter, both the in-situ Digital Image Correlation (DIC) measurement and Finite Element Analysis (FEA) of a Micro-BGA assembly under thermal loading were investigated. In FEA, Sn-Ag-Cu solder properties were characterized by the new constitutive model. The FEA simulation is from 25°C to 125°C and the computed deformation is compared to in-situ DIC measurement subject thermal ramp loading.

8.1 In-situ measurements under thermal loading

8.1.1 Test vehicle

The test vehicle used for in-situ measurement is a Micro-BGA assembly that consists of Polyimide, HDI, Silicon (Si), Cu Pads, Sn-3.8Ag-0.7Cu solder joints and a BT board. The package is cross-sectioned and the internal structure was measured. There are 14 by 14 rows, depopulated, 179 solder interconnect I/Os. The die size is 3.49 by 3.49 mm with a height of 0.25 mm. The solder bump height is 0.4 mm, a diameter of 0.54 mm and a pitch of 0.8 mm. The image of the assembly is shown in Fig. 8.1-1. The micro-speckle technique was used to measure the in-situ deformation of Sn-3.8Ag-0.7Cu solder joint under thermal loading. The equipment named Micro-DISC (Digital Image Speckle Correlation) system used for in-situ measurement is described in the next section.

Fig. 8.1-1 Micro-BGA test Vehicle for thermal loading

8.1.2 Micro-DISC system

The Micro-DISC system is shown in Fig. 8.1-2. The system consists of five main parts: a working table; XYZ motorized translation stages; a long-working distance microscope; a miniature thermal cycling chamber; and a computer. The chamber was fixed on the table. Two resistance heaters and three thermoelectric coolers (TECs) were arranged on the walls of the inner chamber to heat and cool the chamber, respectively. A temperature controller was designed to activate the heaters and coolers in order to produce the required temperature in the inner chamber. The microscope was mounted onto the table via the XYZ stages. A positioning controller was provided to drive the stages and further locate the microscope at any desired point in the XY plane and any desired height over the chamber. The microscope included a zoom module, a focus module, a TV tube and an objective lens. The one-time-focus feature made the microscope able to zoom-in and zoom-out the sample without losing

focus for the measurement of macro- and micro-deformation of packages at the same test. A ring-type white light source was mounted to the objective lens to illuminate the sample through the glass window on the top of the inner chamber. A CCD camera was connected to the TV tube to acquire images of the sample under any loading condition. A main software was developed to control all hardware, generate temperature profile, and acquire the images of the specimen. An image correlation software was implemented into the system to correlate a pair of captured images, calculate the displacement fields, then differentiate the displacement fields to get the strain fields, and visualize the results.

Fig. 8.1-2 Schematic diagram of micro-digital image correlation system (upper left corner: real image of the system): 1 -- objective lens; 2 -- focus module; 3 -- TV tube; 4 -- zoom module; 5, 7 -- position sensors; 6, 8 -- stepper motors; 9 -- ring light source; 10 -- inner

8.1.3 In-situ thermal deformation measurement

Micro-DISC measurements and digital image correlation (DIC) were carried out on the Micro-BGA assembly subjected to thermal loading. The assembly was sectioned along the symmetric plane. Attention should be paid on the sectioned surface to make sure that the surface has a random speckle pattern for digital image correlation (DIC) analysis. The sectioned plane of the Micro-BGA is shown in Fig. 8.1-3. The outmost solder joint located underneath the corner of the silicon die was chosen for analysis. Measurements were taken at different temperatures of 25°C, 75°C and 125°C. These images for three different temperatures shown in Fig. 8.1-4 were selected for analysis.

Fig. 8.1-3 Digital images of sectioned surface

Fig. 8.1-4 Digital images of outmost solder joint during thermal loading

The image at 25°C was at the stress free state and used as the base image. Only the solder joint area was processed for image correlation analysis. The correlated displacement fields in the solder joint at 75°C and 125°C are shown in Fig. 8.1-5 and 8.1-6. The U and V fields are deformations in horizontal (x) and vertical (y) directions respectively. For both temperatures, it is shown that for the largest displacement for U field is located at the bottom right corner of the solder joint. The largest displacement for V field is located at the top right corner of the solder joint. The displacement patterns show that when temperature rise from 25°C to 75°C or 125°C, the deformation of the solder joint has horizontal translation and super-imposed with a

small bending rotation. This observation coincides with the common understanding of the deformation of packaging assembly. Fig. 8.1-7 and 8.1-8 shows the derived shear strain fields from the correlated displacement fields. As indicated in Fig. 8.1-7, the largest shear strain (in absolute value) at 75°C is about -0.63% , and located near the bottom left corner of the solder ball. The overall shear strain is around -0.1% . While for the shear strain at 125°C shown in Fig. 8.1-8, the largest shear strain (in absolute value) is about -1.7% , and the overall strain is around -0.4% . These results agree with those from FEA, which will be described in the following section.

(a) U field (b) V field

Fig.8.1-5 Displacement fields of solder ball at 75°C from correlation (unit: mm)

(a) U field (b) V field

Fig.8.1-6 Displacement fields of solder ball at 125°C from correlation (unit: mm)

Fig. 8.1-7 Shear strain field of solder ball at 75°C from correlation

Fig. 8.1-8 Shear strain field of solder ball at 125°C from correlation

8.2 FEA application of new visco-plastic model

Finite Element Analysis (FEA) is a computer-based numerical technique for calculating the strength and behavior of engineering structures. This technique is used extensively in solving thermal-mechanical problems in the electronic package due to the inability to calculate the displacement using close form equations.

In this work, a commercial FEA program, ANSYS 6.1 is used to solve this thermal-mechanical problem. A 2-Dimension plane strain model was used to model the Micro-BGA. Fig. 8.2-1 shows the 2-D model with the materials defined. The elements of the solder ball with the furthest distance from the neutral point (DNP) were refined as it will experience the largest deformation. For nodes along a plane of symmetry, movement perpendicular to its plane must be restricted. A node was restricted in the y-direction to prevent free body translation and rotation in the space during simulation. The finite element modeling employed the visco-plastic equations for solder and the visco-elastic equations for molding compound. The constitutive models used for various materials in the Micro-BGA assembly are summarized in Table 8.2-1.

Fig. 8.2-1 2-D Finite Element Model for Micro-BGA

Table 8.2-1 Thermo-mechanical constitutive models of Micro-BGA assembly materials

<i>Material</i>	<i>Constitutive model</i>	<i>Source</i>
Silicon Die	Elastic-isotropic	[116]
Polyimide	Elastic-isotropic	Vendors data
Mould	Viscoelastic-isotropic	[116]
Copper Pad	Elastic-isotropic	[116]
HDI	Elastic-isotropic	Vendors data
PCB	Temp-dependent elastic, isotropic	[116]
Die Adhesive	Temp-dependent elastic, isotropic	[116]
Sn-3.8Ag-0.7Cu Solder	Viscoplastic	Curve-fitted

In Chapter 7, a new constitutive visco-plastic model was developed to characterize the stress-strain behavior of solder alloys. Hence, based on the incremental form of the new model, a subroutine code was programmed and implemented into the commercial ANSYS FEA software (See Appendix A), to characterize the visco-plastic behavior of Sn-3.8Ag-0.7Cu solder joint in Micro-BGA assembly. Before applying the new model subroutine to real Micro-BGA assembly, a simple tensile test simulation was

conducted to verify the source code. It was found that the calculated stress results from new model simulation compares satisfactory to the Anand model results within 12%. (See Appendix B)

In Micro-BGA assembly simulation, PLANE183 element based on the user defined material subroutine was used for Sn-3.8Ag-0.7Cu lead-free solder. The constants used in the new hardening model were curve fitted in the previous section and they are $C1 = 18.59$ MPa, $C2 = 5645$ (1/K), $C3 = 13.1$, $C4 = 0.3$, $C5 = 5.5 \times 10^{-4}$, respectively.

The FEA output for the U and V displacement fields for the selected solder joint at 75°C and 125°C are shown in Fig. 8.2-2 and 8.2-3. The maximum and minimum values are located at the corners. By comparison to Fig. 8.1-5 and 8.1-6, it can be noticed that the U and V displacement field pattern from the Micro-DISC and FEA results gave similar trend. For 75°C, the largest relative displacements between the diagonal corners are 1.3 mm (for U displacement) and 0.99 mm (for V) from FEA results, and 1.5 mm (for U) and 1.1 mm (for V) from correlation results respectively; at 125°C, displacements are 2.9 mm (for U) and 2.3 mm (for V) for FEA results, and 2.6 mm (for U) and 2.8 mm (for V) for correlation results. This means that the displacement differences which cause the deformation of the solder ball obtained from FEA and correlation are in satisfactory agreement.

Fig. 8.2-2 Displacement fields of the outmost solder ball by FEA (new model) (T=75°C, unit: mm)

Fig. 8.2-3 Displacement fields of the outmost solder ball by FEA (new model) (T=125°C, unit: mm)

The shear strain fields for the solder joint at 75°C and 125°C are illustrated in Fig. 8.2-4 and 8.2-5. As indicated in Fig. 8.2-4, the largest shear strain (in absolute value) at 75°C is about -0.46%, and also located near the bottom left corner of the solder ball compared to the correlation result. The overall shear strain is around -0.1%, which is exactly matched with the correlation value. While for the shear strain at 125°C shown in Fig. 8.2-5, the similar trend can be found. The largest shear strain (in absolute value) is about -1.4%, and the overall strain is around -0.4%. It can be concluded that the overall results from FEA and correlation are in satisfactory agreement. That means the new constitutive model is also a useful tool to characterize the visco-plastic behavior of solder joints in electronic packaging assembly.

Fig. 8.2-4 Shear strain field of solder ball at 75°C from FEA (new model)

Fig. 8.2-5 Shear strain field of solder ball at 125°C from FEA (new model)

Chapter 9. Conclusion & Recommendation

Mechanics of materials characterization of 95.5Sn-3.8Ag-0.7Cu and 99.3Sn-0.7Cu lead-free solder alloys have been investigated for the mechanical properties, creep and low cycle fatigue behavior. New developments in a visco-plastic constitutive model and a load-drop fatigue model have been documented in detail. Based on the systematic tests and analysis program conducted, the following conclusions can be made.

9.1 Mechanical properties

With reference to the specific research objective (i), the temperature and strain rate dependent tensile properties and stress-strain relations for the two Pb-free solders were investigated and the following conclusions can be made,

1. The values of the mechanical properties of Sn-3.8Ag-0.7Cu and Sn-0.7Cu solder alloys depend strongly on test temperature and strain rate. The experimental results for elastic modulus, yield stress, and UTS have been curve-fitted to comprehensive empirical equations given in Eqs. (4.2.1-4.2.6), respectively.
2. Sn-3.8Ag-0.7Cu and Sn-0.7Cu lead-free solder alloys have better mechanical properties than 63Sn-37Pb solder under the conditions tested here. The author's test data were compared to other reported results.
3. Material constants in Anand visco-plastic model for Sn-3.8Ag-0.7Cu and Sn-0.7Cu lead-free solders were derived and given in Table 4.2-3.

9.2 Creep properties

With reference to the specific research objective (ii), the creep properties for the two Pb-free solders were investigated and the following conclusions can be made,

1. The creep behaviors of Sn-3.8Ag-0.7Cu and Sn-0.7Cu solder alloys depend strongly on test stress level and temperature. The experimental results for steady state creep strain rates had been curve-fitted to a hyperbolic-sine power law model as given in Eq. (5.2.3) and (5.2.4).
2. Sn-3.8Ag-0.7Cu and Sn-0.7Cu lead-free solder alloys have better creep properties than 63Sn-37Pb solder under the conditions tested here. The author's creep test data were compared with other reported solder joint creep results and show similar trends.

9.3 Low cycle fatigue behavior

With reference to the specific research objective (iii), low cycle fatigue behavior for the two Pb-free solders at different temperatures and frequencies were investigated and the following conclusions can be made,

1. Low cycle fatigue models for 95.5Sn-3.8Ag-0.7Cu and 99.3Sn-0.7Cu solder is provided for different temperatures (25°C, 75°C and 125°C) and frequencies (10^{-3} , 10^{-2} and 1Hz). The Coffin-Manson model and Morrow model were used to describe the low cycle fatigue behavior of the two lead-free solder alloys. The fatigue exponent m (or n) and ductility coefficient C (or A) in these models are dependent on temperature and frequency. Frequency-modified Coffin-Manson

model and Morrow model were used to compensate for the frequency effect.

2. Sn-3.8Ag-0.7Cu and Sn-0.7Cu lead-free solder alloys have better fatigue properties than 63Sn-37Pb solder under the conditions tested here. The author's fatigue data show the similar trend with other reported fatigue test results.

9.4 New mechanics models for visco-plastic, fatigue and impact properties

With reference to the specific research objective (iv) and (v), visco-plastic behavior, load drop effects in fatigue and impact property of Sn-3.8Ag-0.7Cu solder were studied, and the conclusions are as follows,

1. A new constitutive model to characterize the visco-plastic behavior of solder material has been developed. It can accurately simulate the strain-stress response over the temperature and strain rate range tested. A hardening-softening parameter and a new strain hardening equation are introduced. The new constitutive model was applied to characterize the Sn-3.8Ag-0.7Cu lead-free solder alloy and implemented as a subroutine in the ANSYS finite element program (See Appendix A).
2. A new low cycle fatigue model has been developed. It overcomes the problem in conventional Coffin-Manson model and Morrow model, where the fatigue behavior at different temperatures and frequencies can be fitted to a master curve with the load drop rate parameter. A damage mechanics approach was developed to calculate the load drop rate at different test conditions. The low cycle fatigue behavior of Sn-3.8Ag-0.7Cu was characterized by the load drop rate fatigue

model.

3. In addition, impact characterization using the Split Hopkinson Pressure Bar impact test provided yield stress for high dynamic strain rates above 10^2s^{-1} . The yield stress for Sn-3.8Ag-0.7Cu over a wide strain rate range (from 10^{-4}s^{-1} to 10^3s^{-1}) is given in Eq. (7.3.2).

9.5 Application to Micro-BGA assembly with Sn-3.8Ag-0.7Cu solder joints

With reference to the specific research objective (vi), micro-deformation analysis of a Micro-BGA assembly was studied by in-situ DIC and FEA methods,

The Micro-BGA assembly with Sn-3.8Ag-0.7Cu lead-free solder was subject to thermal loading and the in-situ strain was measured by the Digital Image Correlation (DIC) method, and compared to FEA analysis. In DIC measurement, the displacement and strain field of the solder joint at 75°C and 125°C were computed. In FEA simulation, the newly developed visco-plastic constitutive model was used to characterize the Sn-Ag-Cu lead-free solder displacement and strain distribution. The FEA results compared fairly well with the in-situ DIC measurement results. It is encouraging that the new visco-plastic constitutive model is able to characterize the non-linear deformation behavior of the solder joints subject to thermal loading.

9.6 Achievements and Recommendations

The key contributions and achievements of this work are noted in the following areas:

1. A systematic study of 95.5Sn-3.8Ag-0.7Cu and Sn-0.7Cu lead-free solders on mechanical properties, creep and low cycle fatigue behavior. Derive mechanics of material models for stress-strain behavior, comprehensive empirical equations for tensile properties, hyperbolic-sine power law models for creep strain rate, material constants for Anand model and fatigue exponent and ductility coefficients in Coffin-Manson and Morrow's models for low cycle fatigue behavior.
2. A new visco-plastic constitutive model has been developed for Sn-3.8Ag-0.7Cu solder and applied to characterize the solder joint non-linear deformation behavior in a Micro-BGA assembly subject to thermal loading.
3. A new load drop rate fatigue model has been developed. This model is more sophisticated than the conventional Coffin-Manson and Morrow models. The fatigue lives at different temperatures and frequencies can be reduced to a master curve with the load drop rate parameter.
4. In-situ micro-deformation analysis of the Micro-BGA assembly under thermal loading was measured by Digital Image Correlation (DIC). The measured strain results compared fairly well with the FEA simulation results using the new visco-plastic constitutive model implemented in a ANSYS subroutine (See Appendix A)
5. A list of journal publication achieved during this project is given in Appendix C.

Some recommendations to improve and make use of the developments made in this project are as follows,

- (i) More repeated tests should be conducted to update the database of lead-free solders;
- (ii) Specimen of different microstructure is suggested to study the effect of microstructure on mechanical properties, creep and low cycle fatigue behavior;
- (iii) The link between the isothermal fatigue micro-mechanism and thermal cycling fatigue micro-mechanism should be investigated.

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Appendix A. USERMAT Subroutine Code

This ANSYS subroutine code was programmed for applying the new constitutive model to Finite Element Analysis (FEA). User material subroutine, USERMAT was chosen to implement the new constitutive model subroutine code. The schematic illustration of the subroutine is shown in Fig. 1.

Fig. 1 Schematic illustration of new constitutive model subroutine

```

subroutine usermat3d(
&          matId, elemId, kDomIntPt, kLayer, kSectPt,
&          ldstep, isubst, keycut,
&          nDirect, nShear, ncomp, nStatev, nProp,
&          Time, dTime, Temp, dTemp,
&          stress, statev, dsdePl, sedEl, sedPl, epseq,
&          Strain, dStrain, epsPl, prop, coords,
&          rotateM, defGrad_t, defGrad,
&          tsstif, epsZZ,
&          var1, var2, var3, var4, var5,
&          var6, var7, var8)

#include "impcom.inc"
c
  INTEGER
&          matId, elemId,
&          kDomIntPt, kLayer, kSectPt,
&          ldstep, isubst, keycut,
&          nDirect, nShear, ncomp, nStatev, nProp
  DOUBLE PRECISION
&          Time,    dTime,    Temp,    dTemp,
&          sedEl,   sedPl,   epseq,   epsZZ
  DOUBLE PRECISION
&          stress (ncomp ), statev (nStatev),
&          dsdePl (ncomp, ncomp),
&          Strain (ncomp ), dStrain (ncomp ),
&          epsPl (ncomp ), prop (nProp ),
&          coords (3),    rotateM (3,3),
&          defGrad (3,3),    defGrad_t(3,3),
&          tsstif (2)

c --- parameters
c
  INTEGER          mcomp
  DOUBLE PRECISION HALF, THIRD, ONE, TWO, SMALL, ONEHALF,
&          ZERO, TWOthird, ONEDM02, ONEDM05, sqTiny
  PARAMETER      (ZERO      = 0.d0,
&          HALF      = 0.5d0,
&          THIRD     = 1.d0/3.d0,
&          ONE       = 1.d0,
&          TWO       = 2.d0,
&          SMALL     = 1.d-08,
&          sqTiny    = 1.d-20,
&          ONEDM02   = 1.d-02,

```

Appendix A. USERMAT Subroutine Code

```

&          ONEDM05      = 1.d-05,
&          ONEHALF      = 1.5d0,
&          TWOTHIRD     = 2.0d0/3.0d0,
&          mcomp        = 6
&          )

EXTERNAL      vmove, rotVect
DOUBLE PRECISION sigElp(mcomp), dsdeEl(mcomp,mcomp), G(mcomp),
&          sigDev(mcomp), JM      (mcomp,mcomp), dfds(mcomp),
&          dsdeVp(mcomp,mcomp), sigvp(mcomp),
&          stresslast(mcomp)

DOUBLE PRECISION var1, var2, var3, var4, var5,
&          var6, var7, var8

DATA G/1.0D0,1.0D0,1.0D0,0.0D0,0.0D0,0.0D0/
c
INTEGER      i, j
DOUBLE PRECISION pEl,   qEl,   pleq_t,  sigy_t, sigy,
&          dpleq, pleq,
&          young, posn,   sigy0,  dsigdep,
&          elast1, elast2,
&          twoG,  threeG,  oneOv3G, qElOv3G, threeOv2qEl,
&          fratio, con1,   con2, sigts, dqElstrain,
&          strainrate, h, tyoung, sstr, qElstrain,
&          sigyhistory, visplas1, visplas2, sigyts
c*****
c
      keycut   = 0
      dsigdep  = ZERO
      pleq_t   = statev(1)
      pleq     = pleq_t
c *** get Young's modulus and Poisson's ratio, initial yield stress and others
      young    = prop(1)
      posn     = prop(2)
      sigy0    = prop(3)
c *** plastic strain tensor
      do i = 4, ncomp
          statev(i+1) = 0.5d0 * statev(i+1)
      end do
c *** update plastic strain
      call rotVect(rotateM,statev(2),ncomp)
c *** back to engineering strain form
      do i = 4, ncomp

```

```

        statev(i+1) = 2.0d0 * statev(i+1)
    end do
    call vmove(statev(2), epsPl(1), ncomp)
c *** calculate plastic slope
    dqElstrain=
    & (dStrain(1) - dStrain(2))*(dStrain(1) - dStrain(2))+
    & (dStrain(1) - dStrain(3))*(dStrain(1) - dStrain(3))+
    & (dStrain(3) - dStrain(2))*(dStrain(3) - dStrain(2))+
    & TWOTHIRD*(dStrain(4)**2+dStrain(5)**2+dStrain(6)**2)
    dqElstrain = sqrt( 4.d0/9.d0 * dqElstrain)
qElstrain=
    & (Strain(1) - Strain(2))*(Strain(1) - Strain(2))+
    & (Strain(1) - Strain(3))*(Strain(1) - Strain(3))+
    & (Strain(3) - Strain(2))*(Strain(3) - Strain(2))+
    & TWOTHIRD*(Strain(4)**2+Strain(5)**2+Strain(6)**2)
    qElstrain = sqrt( 4.d0/9.d0 * qElstrain)
strainrate=dqElstrain/dTime
    h=((strainrate/18.59d0)*EXP(5.645d03/Temp))**3.0d-01
    sstr=13.1d0*log10(h+SQRT(h*h+1))
    dsigdep=ssstr*5.5d-04/
    & ((5.5d-04+qElstrain)*(5.5d-04+qElstrain))
    twoG      = young / (ONE+posn)
    threeG     = ONEHALF * twoG
    elast1=young*posn/((1.0D0+posn)*(1.0D0-TWO*posn))
    elast2=HALF*twoG
c *** define tsstif(1) since it is used for calculation of hourglass stiffness
    tsstif(1) = elast2
c
c *** calculate elastic stiffness matrix (3d)
c
    dsdeEl(1,1)=(elast1+TWO*elast2)*G(1)*G(1)
    dsdeEl(1,2)=elast1*G(1)*G(2)+elast2*TWO*G(4)*G(4)
    dsdeEl(1,3)=elast1*G(1)*G(3)+elast2*TWO*G(5)*G(5)
    dsdeEl(1,4)=elast1*G(1)*G(4)+elast2*TWO*G(1)*G(4)
    dsdeEl(1,5)=elast1*G(1)*G(5)+elast2*TWO*G(1)*G(5)
    dsdeEl(1,6)=elast1*G(1)*G(6)+elast2*TWO*G(4)*G(5)
    dsdeEl(2,2)=(elast1+TWO*elast2)*G(2)*G(2)
    dsdeEl(2,3)=elast1*G(2)*G(3)+elast2*TWO*G(6)*G(6)
    dsdeEl(2,4)=elast1*G(2)*G(4)+elast2*TWO*G(1)*G(4)
    dsdeEl(2,5)=elast1*G(2)*G(5)+elast2*TWO*G(1)*G(5)
    dsdeEl(2,6)=elast1*G(2)*G(6)+elast2*TWO*G(2)*G(6)
    dsdeEl(3,3)=(elast1+TWO*elast2)*G(3)*G(3)
    dsdeEl(3,4)=elast1*G(3)*G(4)+elast2*TWO*G(5)*G(6)
    dsdeEl(3,5)=elast1*G(3)*G(5)+elast2*TWO*G(5)*G(3)

```


Appendix A. USERMAT Subroutine Code

```

dsdeEl(3,6)=elast1*G(3)*G(6)+elast2*TWO*G(6)*G(3)
dsdeEl(4,4)=elast1*G(4)*G(4)+elast2*(G(1)*G(2)+G(4)*G(4))
dsdeEl(4,5)=elast1*G(4)*G(5)+elast2*(G(1)*G(6)+G(5)*G(4))
dsdeEl(4,6)=elast1*G(4)*G(6)+elast2*(G(4)*G(6)+G(5)*G(2))
dsdeEl(5,5)=elast1*G(5)*G(5)+elast2*(G(1)*G(3)+G(5)*G(5))
dsdeEl(5,6)=elast1*G(5)*G(6)+elast2*(G(4)*G(3)+G(5)*G(6))
dsdeEl(6,6)=elast1*G(6)*G(6)+elast2*(G(2)*G(3)+G(6)*G(6))
do i=1,ncomp-1
  do j=i+1,ncomp
    dsdeEl(j,i)=dsdeEl(i,j)
  end do
end do

c
c *** calculate the trial stress and
c   copy elastic moduli dsdeEl to material Jacobian matrix
do i=1,ncomp
  sigElp(i) = stress(i)
  do j=1,ncomp
    dsdePl(j,i) = dsdeEl(j,i)
    sigElp(i) = sigElp(i)+dsdeEl(j,i)*dStrain(j)
  end do
end do

c *** hydrostatic pressure stress
pEl = -THIRD * (sigElp(1) + sigElp(2) + sigElp(3))

c *** compute the deviatoric stress tensor
sigDev(1) = sigElp(1) + pEl
sigDev(2) = sigElp(2) + pEl
sigDev(3) = sigElp(3) + pEl
sigDev(4) = sigElp(4)
sigDev(5) = sigElp(5)
sigDev(6) = sigElp(6)

c *** compute von-mises stress
qEl =
& sigDev(1) * sigDev(1)+sigDev(2) * sigDev(2)+
& sigDev(3) * sigDev(3)+
& TWO*(sigDev(4) * sigDev(4)+ sigDev(5) * sigDev(5)+
& sigDev(6) * sigDev(6))
qEl = sqrt( ONEHALF * qEl)

c *** compute current yield stress
sigy0=(-1.36d-1*(Temp-273)+67.54)*
& (strainrate**(5.59d-4*(Temp-273)+0.0675))
sigy = sigy0+ dsigdep * pleq

c
fratio = qEl / sigy - ONE

```



```

c *** check for yielding
      IF (sigy .LE. ZERO.or.fratio .LE. -SMALL) GO TO 500
c
      sigy_t = sigy
      threeOv2qEl = ONEHALF / qEl
c *** compute derivative of the yield function
      DO i=1, ncomp
          dfds(i) = threeOv2qEl * sigDev(i)
      END DO
      oneOv3G = ONE / threeG
      qElOv3G = qEl * oneOv3G
c *** initial guess of incremental equivalent plastic strain
      dpleq = qElOv3G - sigy * oneOv3G
      pleq = pleq_t + dpleq
      sigy = sigy0 + dsigdep * pleq
c
c *** update stresses
      DO i = 1 , ncomp
          stress(i) = sigElp(i) - TWOTHIRD * (qEl-sigy) * dfds(i)
      END DO
c
c *** update plastic strains
      DO i = 1 , nDirect
          epsPl(i) = epsPl(i) + dfds(i) * dpleq
      END DO
      DO i = nDirect + 1 , ncomp
          epsPl(i) = epsPl(i) + TWO * dfds(i) * dpleq
      END DO
      epseq = pleq
c *** Update state variables
      statev(1) = pleq
      do i=1,ncomp
          statev(i+1) = epsPl(i)
      end do
c *** Update plastic work
      sedPl = sedPl + HALF * (sigy_t+sigy)*dpleq
c
c *** Material Jacobian matrix
c
      IF (qEl.LT.sqTiny) THEN
          con1 = ZERO
      ELSE
          con1 = threeG * dpleq / qEl
      END IF

```

Appendix A. USERMAT Subroutine Code

```

con2 = threeG/(threeG+dsigdep) - con1
con2 = TWOTHIRD * con2
DO i=1,ncomp
  DO j=1,ncomp
    JM(j,i) = ZERO
  END DO
END DO
DO i=1,nDirect
  DO j=1,nDirect
    JM(i,j) = -THIRD
  END DO
  JM(i,i) = JM(i,i) + ONE
END DO
DO i=nDirect + 1,ncomp
  JM(i,i) = HALF
END DO
DO i=1,ncomp
  DO j=1,ncomp
    dsdePl(i,j) = dsdeEl(i,j) - twoG
&      * ( con2 * dfds(i) * dfds(j) + con1 * JM(i,j) )
  END DO
END DO
c
  goto 600
500 continue

c *** Update stress in case of elastic/unloading
  do i=1,ncomp
    stress(i) = sigElp(i)
  end do

600 continue
  sedEl = ZERO
  DO i = 1 , ncomp
    sedEl = sedEl + stress(i)*(Strain(i)+dStrain(i)-epsPl(i))
  END DO
  sedEl = sedEl * HALF
  statev(nStatev) = sigy
c
990 CONTINUE
c
  return
end

```

Appendix B. FEA Simulation of Simple Tension Displacement Case Study

A simple tension displacement simulation was conducted to verify the new visco-plastic model subroutine. A 2-Dimension plane strain model was used to model simple tension displacement. Fig. 1 shows the boundary condition of the simulation. PLANE183 element was used for new model simulation; while VISCO108 element was used for Anand model simulation. The simple tension case study was simulated at different temperatures and strain rates by changing the uniform temperature and loading time, the simulation matrix is shown in Table 1. Each simulation used displacement loading up to 1% strain.

The FEA simulation was also conducted by using Anand model for comparison to the new visco-plastic model results. It was found that both the new visco-plastic model and Anand model simulation results gave a computed stress (at 1% strain) which decrease with temperature and increase with strain rate. The simulation results at 10^{-3} s⁻¹ strain rate at different temperatures are shown in Fig. 2. It can be seen that both the models have similar trend and agree fairly well. Fig. 3 shows the comparison of the computed stress at 1% strain in tension for the new model and Anand model results. The new visco-plastic constitutive model show similar trend compared with the Anand model and gave higher computed stress by 12%.

Appendix B. FEA Simulation of Simple Tension Displacement Case Study

Fig. 1 Boundary condition of tensile simulation

Table 1 Simulation matrix

	25°C	75°C	125°C
10^{-4} s^{-1}	✓	✓	✓
10^{-3} s^{-1}	✓	✓	✓
10^{-2} s^{-1}	✓	✓	✓

Anand model

Own model

Fig. 2(a) Simple tensile test simulation result at 25°C and strain rate of 10^{-3} s^{-1}

Anand model

Own model

Fig. 2(b) Simple tensile test simulation result at 75°C and strain rate of 10^{-3} s^{-1}

Appendix B. FEA Simulation of Simple Tension Displacement Case Study

Fig. 2(c) Simple tensile test simulation result at 125°C and strain rate of 10^{-3} s^{-1}

Fig. 3 Comparison of simple tensile test at 10^{-3} s^{-1} and different temperatures

Appendix C. List of Journal Publication

1. Pang H.L. John, **Xiong B.S.** and Low T.H., "Low Cycle Fatigue Study of Lead Free 99.3Sn-0.7Cu Solder Alloy," International Journal of Fatigue, Vol. 26, Issue 8, August 2004, pp.865-872.
2. Pang H.L. John., **Xiong B.S.** and Low T.H., "Comprehensive Mechanics Characterization of Lead-Free 95.5Sn-3.8Ag-0.7Cu Solder," Micromaterials and Nanomaterials, Issue 3, 2004, pp.86-93.
3. Pang H.L. John, **Xiong B.S.** and Low T.H., "Low Cycle Fatigue Models For Lead Free Solders," Thin Solid Film, Vol. 462-463, September 2004, pp. 408-412.
4. Pang H. L. John, Low T. H., **Xiong B.S.**, Xu Luhua and Neo C. C., "Thermal cycling aging effects on Sn-Ag-Cu solder joint microstructure, IMC and strength," Thin Solid Film, Vol. 462-463, September 2004, pp. 370-375.
5. Pang H.L. John, **Xiong B.S.**, Neo C.C. and Low T.H., "Mechanical Properties for 95.5Sn-3.8Ag-0.7Cu Lead Free Solder Alloy," IEEE Transactions of Components and Packaging Technologies (Accepted).