

# Particle Classification by the Tandem Differential Mobility Analyzer–Particle Mass Analyzer System

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**Supplemental Information**  
**Particle Classification by the Tandem Differential Mobility Analyzer –**  
**Particle Mass Analyzer System**

by

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## S1. APM transfer function for the parabolic flow model

In the case of the parabolic flow model,  $s_1^\pm$  are provided by numerically solving the following equation (Ehara et al. 1996)

$$\lambda (s_1^\pm) = \frac{3}{2} [1 - \rho^2 (s_1^\pm)] \ln \left[ \frac{\rho (s_1^\pm) \mp 1}{\rho (s_1^\pm) \pm 1} \right] + 3\rho (s_1^\pm) \quad (\text{S1}).$$

In this equation,  $\rho(s)$  is defined as

$$\rho (s) = \frac{1}{\delta} \left( \sqrt{\frac{V_{APM}}{s\omega^2 \ln (r_{2\_APM} / r_{1\_APM})}} - r_{c\_APM} \right) \quad (\text{S2}).$$

The APM transfer function  $\Omega (s)$  is represented by

$$\Omega (s) = (\rho_0^h - \rho_0^l) \frac{[3 - (\rho_0^h)^2 - \rho_0^h \rho_0^l - (\rho_0^l)^2]}{4} \quad (\text{S3}).$$

$\rho_0^l$  and  $\rho_0^h$  are calculated using the following equation

$$\zeta = \frac{3}{2\lambda} [1 - \rho^2 (s)] \ln \left[ \frac{\rho - \rho (s)}{\rho_0 (\rho, \zeta) - \rho (s)} \right] - \frac{3}{4\lambda} \left\{ [\rho + \rho (s)]^2 - [\rho_0 (\rho, \zeta) + \rho (s)]^2 \right\} \quad (\text{S4}).$$

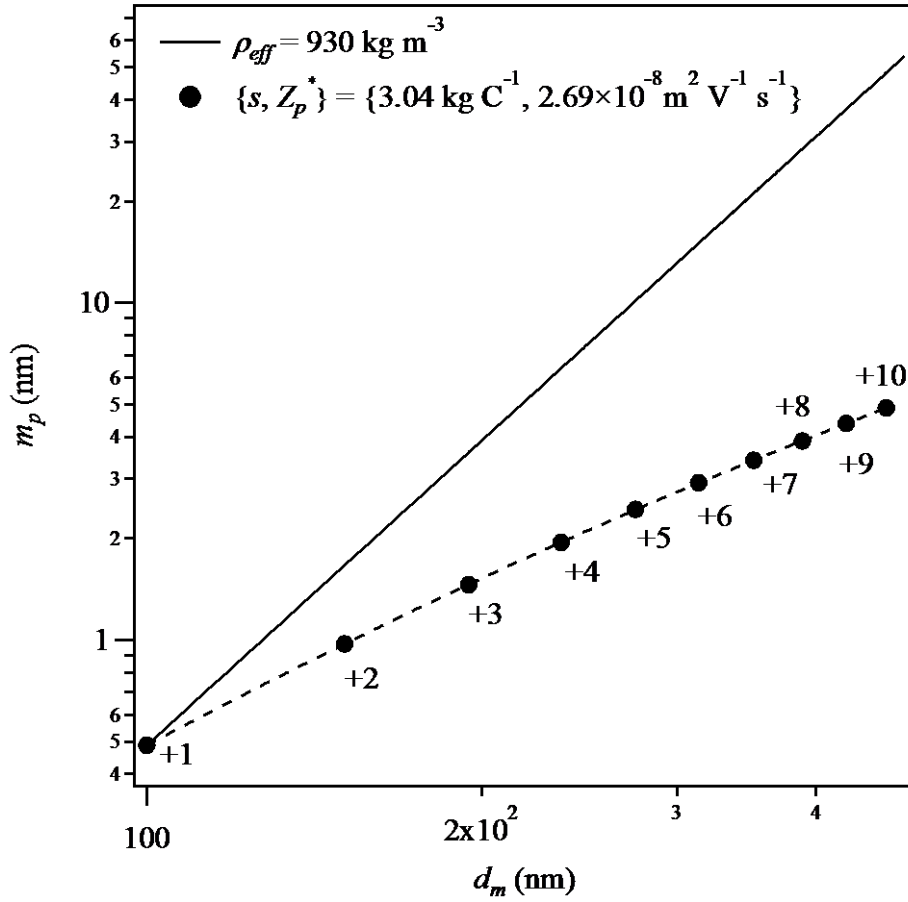
For the regions B and C,  $\rho_0^l$  is calculated using equation S4 by substituting  $\{ \rho, \zeta \} = \{-$

$1, 1\}$ .  $\rho_0^h$  for the regions C and D are similarly obtained using a parameter set of

$\{ \rho, \zeta \} = \{1, 1\}$ .  $\rho_0^h$  for the region B is 1, and  $\rho_0^l$  is equal to -1 for the region D.

## References

Ehara, K., Hagwood, C., and Coakley, K. J. (1996). Novel method to classify aerosol particles according to their mass-to-charge ratio - Aerosol particle mass analyser. *J. Aerosol Sci.* 27:217-234.



**Figure S1.** Examples of locations for multiple charged particles. The integers in the figure indicate the number of particle charges. The specific mass  $s$  and electrical mobility  $Z_p$  were fixed at  $3.04 \text{ kg C}^{-1}$  and  $2.69 \times 10^{-8} \text{ m}^2 \text{ V}^{-1} \text{ s}^{-1}$ , respectively. For single charged particles (+1), these values correspond to  $\{m_p, d_c\} = \{0.49 \text{ fg}, 100 \text{ nm}\}$ . The corresponding value of  $\rho_{eff}$  for such single charged particles is  $930 \text{ kg m}^{-3}$ . The distance between the line for  $\rho_{eff} = 930 \text{ kg m}^{-3}$  and the positions of the multiple charged particles tends to be far for highly charged particles. When particles have a narrow population around the line for  $\rho_{eff} = 930 \text{ kg m}^{-3}$ , highly charged particles have a lower chance of being selected by the DMA-APM system due to the longer distance in the  $\log(m_p)$ - $\log(d_m)$  space.