

# Effect of transition metal (M = Co, Ni, Cu) substitution on electronic structure and vacancy formation of Li<sub>3</sub>N

Wu, Shunnian; Dong, Zhili; Wu, Ping; Boey, Freddy Yin Chiang

2011

Wu, S., Dong, Z., Wu, P., & Boey, F. Y. C. (2011). Effect of transition metal (M = Co, Ni, Cu) substitution on electronic structure and vacancy formation of Li<sub>3</sub>N. *Journal of Materials Chemistry*, 21(1), 165-170.

<https://hdl.handle.net/10356/96313>

<https://doi.org/10.1039/c0jm01883j>

---

© 2011 The Royal Society of Chemistry. This is the author created version of a work that has been peer reviewed and accepted for publication by *Journal of Materials Chemistry*, The Royal Society of Chemistry. It incorporates referee's comments but changes resulting from the publishing process, such as copyediting, structural formatting, may not be reflected in this document. The published version is available at: [<http://dx.doi.org/10.1039/c0jm01883j>].

*Downloaded on 02 Dec 2020 06:02:50 SGT*

# Effect of transition metal (M = Co, Ni, Cu) substitution on electronic structure and vacancy formation of Li<sub>3</sub>N

Shunnian Wu,<sup>ab</sup> Zhili Dong,<sup>a</sup> Ping Wu<sup>\*ab</sup> and Freddy Boey<sup>\*a</sup>

Received (in XXX, XXX) Xth XXXXXXXXX 20XX, Accepted Xth XXXXXXXXX 20XX

DOI: 10.1039/b000000x

We carried out first principles calculations to investigate the effect of transition metal (M = Co, Ni, Cu) substitution on electronic structure and vacancy formation of Li<sub>3</sub>N in this study. Transition metals are shown to selectively substitute interplanar Li(1) atoms. Both Co and Ni substitution remarkably reduces the energy band gap to 0.55 eV in comparison with 1.13 eV of Li<sub>3</sub>N, while Cu substitution insignificantly decreases the energy band gap by 0.07 eV. Covalent bonding between transition metal atom and the coordinated N, which is manifested both visually by the contour plots of valence charge density difference and numerically by bond length variation, results in the formation of Li<sub>3-x-y</sub>M<sub>x</sub>□<sub>y</sub>N with *y* dependent on the covalency and concentration of transition metal. Ni substitution significantly reduces *V*<sub>Li(2)</sub> formation energy, which suggests greatly increased Li vacancy concentration for improved Li ionic mobility and conduction. Therefore, controlling the energy band gap and vacancy concentration by transition metal substitution provides a viable approach to tailor Li<sub>3</sub>N for variable applications in rechargeable lithium ion batteries.

## Introduction

Transition metal substituted lithium nitrides have emerged as promising candidates for anode materials in rechargeable lithium ion batteries.<sup>1-5</sup> Li<sub>3</sub>N can react with transition metals at approximately 600–900 °C under nitrogen-rich conditions to form two groups of ternary nitride compounds, one with the anti-fluorite structure and the other with the layered Li<sub>3</sub>N

structure.<sup>6-8</sup> The structure of these ternary lithium nitrides follows a predictable trend that the anti-fluorite structure is favored for Ti through Fe and a structure is based on the layered Li<sub>3</sub>N structure for Co, Ni and Cu.<sup>9</sup> Transition metals (M = Co, Ni, Cu) are proposed to substitute Li in Li(1) sites of Li<sub>3</sub>N as shown in Fig. 1, irrespective of the dopant concentration and the synthesis conditions applied.<sup>10-14</sup> The layered morphology is claimed to be beneficial to fast Li-ion conduction and low transition metal oxidation states.<sup>9</sup> It is claimed that no ternary lithium nitrides could surpass the high capacity of the Li<sub>2.6</sub>Co<sub>0.4</sub>N nitride at low potential, yet substitution of Co by Ni or Cu can dramatically improve the cycling performance with a slightly decreased capacity.<sup>1,15</sup>

Two disputable models have been proposed to account for the substitution of Li by transition metals in Li<sub>3</sub>N. Some claimed ostensibly isovalent substitution of Li<sup>+</sup> by M<sup>+</sup>, which leads to the formation of Li<sub>3-x</sub>M<sub>x</sub>N. Consequently, the Li vacancy concentration would be about 1–2% generally observed in Li<sub>3</sub>N. The charge balance of Li<sub>2.6</sub>Co<sub>0.4</sub>N was well described with monovalent cobalt.<sup>16,17</sup> Negligible lithium vacancies were determined in Li<sub>2.6</sub>Co<sub>0.4</sub>N from chemical composition analysis.<sup>16</sup> Li<sub>2.57</sub>Cu<sub>0.43</sub>N showed 1–2% disordered Li vacancies similar to Li<sub>3</sub>N,<sup>10</sup> which seemed insensitive to reaction temperature. Niewa *et al.* also claimed that transition metal (M = Ni and Cu) substituted Li<sub>3</sub>N contains predominately M<sup>+</sup> species over the whole range of *x* in Li<sub>3-x</sub>M<sub>x</sub>N based on their X-ray diffraction data, thermal measurements, and chemical analysis.<sup>13</sup>

Since transition metals rarely exist in the +1 oxidation state as M<sup>+</sup> (Cu<sup>+</sup> and few Ni<sup>+</sup>, Co<sup>+</sup> oxo-ligands are exceptions<sup>18-22</sup>), others asserted aliovalent substitution of Li<sup>+</sup> by M<sup>+2</sup>, which gives

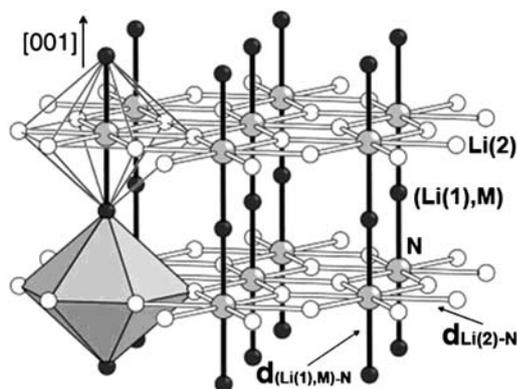


Fig. 1 Schematic illustration of transition metal substituted Li<sub>3</sub>N.

<sup>a</sup>School of Materials Science and Engineering, Nanyang Technological University, Nanyang Avenue, Singapore 639798. E-mail: mychoey@ntu.edu.sg

<sup>b</sup>Institute of High Performance Computing, 1 Fusionopolis Way, #16-16 Connexis, Singapore 138632. E-mail: wuping@ihpc.a-star.edu.sg

rise to the formation of  $\text{Li}_{3-2x}\text{M}_x\text{Li}_x\text{N}$  ( $\square = \text{Li}$  vacancy). This suggests that high concentration of Li vacancies is required to compensate the charge balance for divalent (or even trivalent) transition metals, and that Li vacancy concentration increases with the concentration of doped transition metal.  $\text{LiNiN}$  was claimed to serve as an excellent model compound of the stoichiometric  $\text{LiNi}\square\text{N}$  with 50% Li vacancies in the  $[\text{Li}_2\text{N}]$  plane.<sup>23</sup> Ducros *et al.* declared to synthesize a series of stoichiometric  $\text{Li}_{3-2x}\text{Ni}_x\text{N}$  ( $0.20 \leq x \leq 0.60$ ) compounds with the existence of  $\text{Ni}^{2+}$  and correspondingly compensated Li vacancies.<sup>24</sup>  $\text{Li}_{1.99}\text{Co}_{0.53}\text{N}$  synthesized by Gordon *et al.*,<sup>11</sup>  $\text{Li}_{1.36}\text{Ni}_{0.79}\text{N}$  and  $\text{Li}_{2.25}\text{Cu}_{0.43}\text{N}$  by Gregory *et al.*,<sup>12</sup> and  $\text{Li}_{2.2}\text{Cu}_{0.5}\text{N}$  by Weller *et al.*<sup>25</sup> were also proposed to support the predominant aliovalent substitution model.

These two discrepant substitution models bring about distinct transition metal oxidation states and thus Li vacancy concentrations. The ionic conduction of these substituted lithium nitrides originates from hopping of Li ions among the Li vacancies and Li occupied sites. Therefore, an understanding of the nature of Li vacancies in transition metal substituted  $\text{Li}_3\text{N}$  is essential for their potential applications. However, to date, there is little relevant theoretic work reported in the literature. In this study, we carried out first principles calculations to study the effect of transition metal substitution on the electronic structure and vacancy formation of  $\text{Li}_3\text{N}$ . These results would provide an insight into the dopant selection and vacancy tailoring for improved performance of ternary lithium nitrides.

## Methodology

First principles calculations were carried out using the plane-wave based Vienna *ab initio* simulation package VASP.<sup>26–28</sup> Exchange and correlation were treated within the Perdew–Burke–Ernzerhof (PBE) generalized gradient approximation (GGA).<sup>29,30</sup> For the electronic configuration, the states treated as bands were: Li (2s, 2p), N (2s, 2p), Co (4s, 3d), Ni (4s, 3d) and Cu (4s, 3d). The cutoff energy for the plane-wave expansion was set to be 500 eV, sufficiently high to give well-converged total energies and structures.  $4 \times 4 \times 4k$ -point mesh according to the Monkhorst–Pack method<sup>31</sup> was adopted in all total energy calculations. With this setup, total energies in our calculations are converged to within 0.01 eV. In the relaxation of  $\text{Li}_3\text{N}$  unit cell, both cell parameters and ionic positions were fully optimized so as to obtain the minimum total energies. Our calculated lattice constants are  $a = 3.64 \text{ \AA}$  and  $c = 3.87 \text{ \AA}$ , which are in good agreement with the experimental values  $3.65 \text{ \AA}$  and  $3.87 \text{ \AA}$ ,<sup>32</sup> respectively.  $\text{Li}_3\text{N}$  supercells were constructed by  $3 \times 3 \times 3$  expansion of  $\text{Li}_3\text{N}$  unit cell and one Li atom was substituted to model the substituted structure, yielding a dopant concentration of 1.23 at%. To establish clearly the effect of transition metal substitution without much interference from structural changes, the lattice parameters of  $\text{Li}_3\text{N}$  supercells with transition metal substitution were fixed as those of the  $\text{Li}_3\text{N}$  supercells, as we assumed the conditions at the dilute limit. Our preliminary calculations indicate that substitution brings about negligible lattice variation with observed volume change less than 0.3%. A Li vacancy was generated by removing one Li atom near the transition metal atom to observe its effect more clearly. Spin-polarization was also included where excess spins are expected.

## Results and discussion

Hexagonal layer-structured  $\text{Li}_3\text{N}$  consists of alternating  $[\text{Li}(2)_2\text{N}]$  and Li(1) layers, where two types of Li exist, *i.e.* one Li(1) coordinated with 2 N atoms and two equivalent Li(2) coordinated with 3 N atoms. Therefore, transition metal ( $\text{M} = \text{Co}, \text{Ni}, \text{Cu}$ ) may substitute Li either in Li(1) site or in Li(2) site in  $\text{Li}_3\text{N}$  structure. Total energy calculations were first carried out to determine the substitution site. The energy differences  $\Delta E$  for transition metal substitution in two different Li sites are calculated with:

$$\Delta E = E_{\text{T}}(M_{\text{Li}(1)}) - E_{\text{T}}(M_{\text{Li}(2)}) \quad (1)$$

where  $E_{\text{T}}(M_{\text{Li}(1)})$  and  $E_{\text{T}}(M_{\text{Li}(2)})$  are the total energies of  $\text{Li}_3\text{N}$  supercell with one Li substituted by one M atom in Li(1) site and Li(2) site, respectively. A negative  $\Delta E$  value indicates that Li(1) substitution is energetically favored.

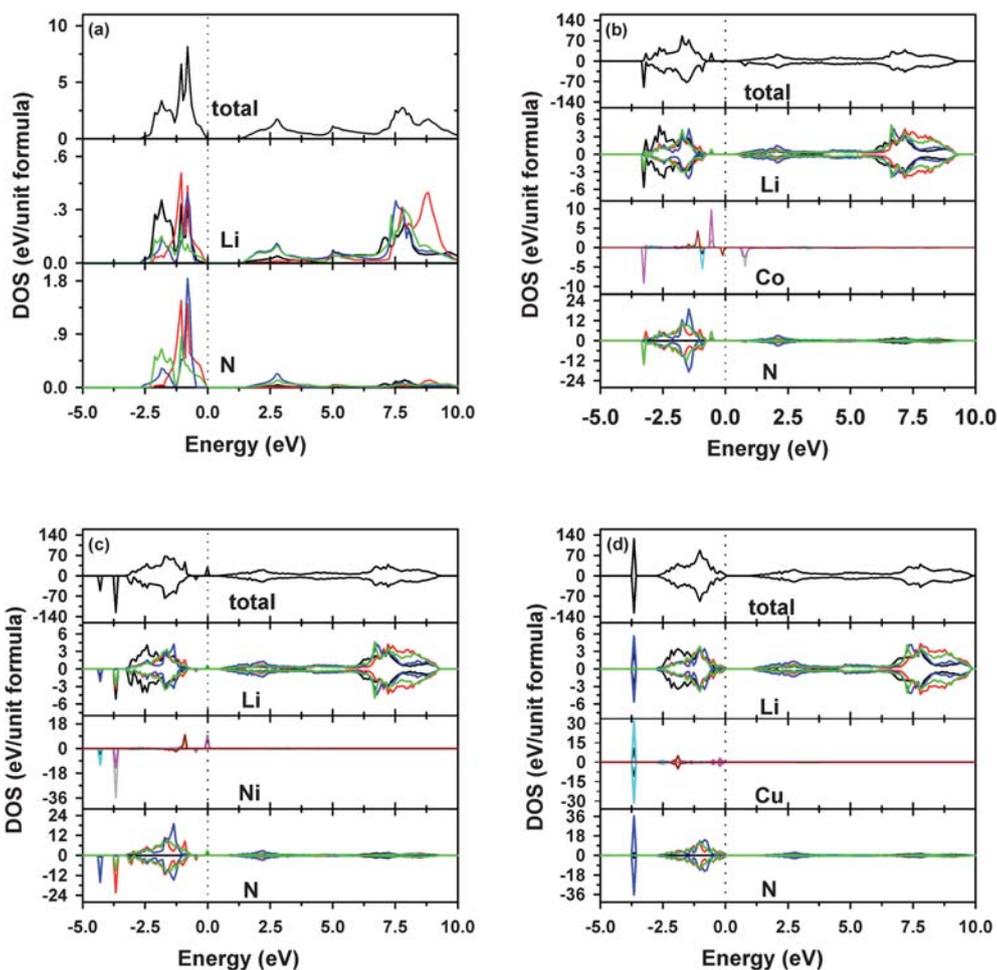
The obtained  $\Delta E$  values for different transition metals ( $\text{M} = \text{Co}, \text{Ni}, \text{Cu}$ ) are listed in Table 1. The  $\Delta E$  values being less than  $-1.2 \text{ eV}$  suggests that transition metals selectively replace Li in Li(1) sites. This is consistent with the experimentally observed transition metal substitution for Li at the interplanar site.<sup>10–14</sup> Therefore,  $\text{Li}_3\text{N}$  with transition metal doped in Li(1) site was selected for the following study.

The densities of states (DOS) and the projected densities of states (PDOS) for  $\text{Li}_3\text{N}$  and transition metal substituted  $\text{Li}_3\text{N}$  are shown in Fig. 2. It shows that  $\text{Li}_3\text{N}$  is an ionic semiconductor with occupied valence band mainly derived from N 2p states and conduction bands from Li 2s and 2p states. The appreciable overlapping of Li 2s states with N 2p states implicates weak covalent bonding in the structure. This is consistent with the electron energy loss spectroscopy study, which discloses that  $\text{Li}_3\text{N}$  is not completely ionic but has at least weak covalent characteristics.<sup>17</sup> Transition metal substitution significantly changes the electronic structure of  $\text{Li}_3\text{N}$ . Spin-polarization is observed in both  $\text{Li}_3\text{N}/\text{Co}$  and  $\text{Li}_3\text{N}/\text{Ni}$ , suggesting the existence of unpaired 3d electrons in Co and Ni, while no spin-polarization in  $\text{Li}_3\text{N}/\text{Cu}$  indicates fully paired 3d electrons in Cu. The valence bands in transition metal substituted  $\text{Li}_3\text{N}$  are composed of both M 3d states and N 2p states, and the conduction bands mainly come from Li 2s and 2p states. Substitution of Li by both Co and Ni greatly reduces the energy band gap to 0.55 eV in comparison with 1.13 eV of  $\text{Li}_3\text{N}$ , which can be attributed to the formation of tangling bonds at the Fermi surface. This suggests possible electronic conduction *via* electron hopping in Co or Ni substituted  $\text{Li}_3\text{N}$ . It is expected that the substituted  $\text{Li}_3\text{N}$  can even become a metallic conductor with formation of infinite N–M–N chains,  $\frac{1}{\infty}[\text{MN}_{2/2}]$ , with increasing dopant concentration.<sup>33</sup> On the other hand, Cu substitution insignificantly reduces the energy band gap by 0.07 eV without formation of tangling bonds

**Table 1** Calculated energy difference  $\Delta E$  for different dopants<sup>a</sup>

	$\text{Li}_3\text{N}/\text{Co}$	$\text{Li}_3\text{N}/\text{Ni}$	$\text{Li}_3\text{N}/\text{Cu}$
$\Delta E/\text{eV}$	–1.34	–1.30	–1.23

<sup>a</sup>  $\text{Li}_3\text{N}/\text{Co}$ ,  $\text{Li}_3\text{N}/\text{Ni}$  and  $\text{Li}_3\text{N}/\text{Cu}$  denote  $\text{Li}_3\text{N}$  supercell with one Li substituted by Co, Ni and Cu separately.



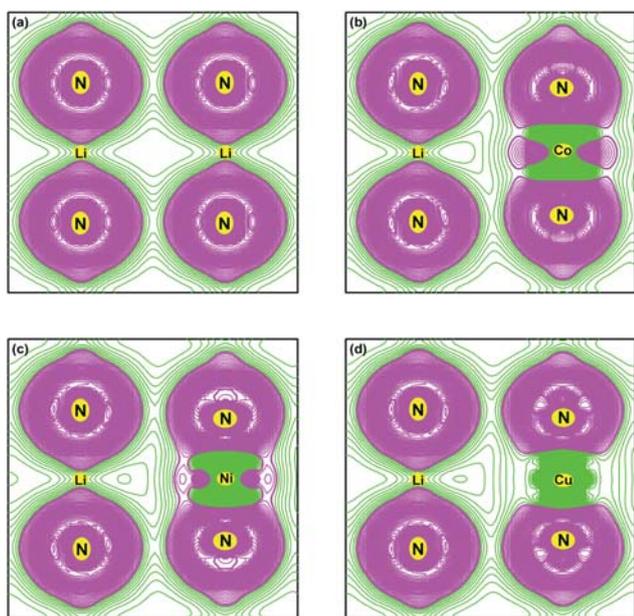
**Fig. 2** DOS and PDOS for  $\text{Li}_3\text{N}$  (a), and  $\text{Li}_3\text{N}/\text{Co}$  (b),  $\text{Li}_3\text{N}/\text{Ni}$  (c) and  $\text{Li}_3\text{N}/\text{Cu}$  (d) respectively. The PDOS components are  $s$  black;  $p_x$  red;  $p_y$  blue;  $p_z$  green;  $d_{xy}$  (overlapped with  $d_{x^2-y^2}$ ) yellow;  $d_{yz}$  gray;  $d_{xz}$  cyan;  $d_{z^2}$  pink; and  $d_{x^2-y^2}$  dark red. The Fermi level is set to zero.

at the Fermi surface. Therefore, different transition metal substitution suggests a viable approach to tailor the electronic conduction of  $\text{Li}_3\text{N}$  for various electrochemical applications.

It is seen from Fig. 2 that the five-fold degenerate 3d states of transition metal splits to delocalized  $d_{xz}$  state and localized  $d_{xy}/d_{x^2-y^2}$  and  $d_{yz}/d_{z^2}$  states. Therefore, there are one unpaired 3d electron in Co of  $3d^7$ , two unpaired 3d electrons in Ni of  $3d^8$  and no unpaired electron in Cu of  $3d^{10}$ , which is consistent with the observed spin-polarization. The overlapping of N  $p_x/p_y$  states with M  $d_{xy}/d_{x^2-y^2}$  states in the valence band region suggests the occurrence of  $\pi$ -bonding, while the M  $d_{yz}/d_{z^2}$  states may interact with N  $p_z$  state to form  $\sigma$ -bonding. This implicates covalent bonding between N and M in transition metal substituted  $\text{Li}_3\text{N}$ . The 3d states of Co and Ni located at approximately 0.6 eV above the original valence band maximum (VBM) of  $\text{Li}_3\text{N}$  interact with Li and N states which are partly pushed to higher energies. This upward shift of valence bands decreases the cohesion in Co or Ni substituted  $\text{Li}_3\text{N}$  and thus brings about the destabilization. On the contrary, the interaction of 3d states of Cu with N and Li states does not push N and Li states to higher energies, since the 3d states of Cu to build up the valence bands are close to the original VBM of  $\text{Li}_3\text{N}$ . Therefore, Cu substitution marginally affects the thermodynamic stability of  $\text{Li}_3\text{N}$ . Experiments observed that ternary copper lithium nitrides are

more stable than ternary nickel lithium nitrides and ternary cobalt lithium nitrides.<sup>14</sup> Destabilization by transition metal substitution was also asserted in lithium borohydride<sup>34</sup> and lithium amide-imide structures.<sup>35</sup> The destabilization might be beneficial to the intercalation and deintercalation processes in rechargeable lithium ion batteries, which leads to improved charge-discharge cyclability.

The different bonding in  $\text{Li}_3\text{N}$  and transition metal substituted  $\text{Li}_3\text{N}$  is illustrated by the contour plots of valence charge density difference of the plane through substitution site in [001] direction shown in Fig. 3. The difference is defined as  $\Delta\rho = \rho_{\text{solid}} - \sum\rho_{\text{atom}}$ , *i.e.* the difference between the total charge density of the solid and the superposition of independent atomic charge densities placed at the atomic sites of the same solid, which is instructive to evaluate valence charge density distribution. The weak interactions between Li(1) and M in the (Li(1),M) layer are not shown here. It can be seen that conspicuous ionic bonding between Li and N predominates in  $\text{Li}_3\text{N}$ . Electrons accumulate around the N atoms while deplete around the Li atoms, indicating that the charges transfer from Li to N. On the other hand, electrons accumulate between N and M in transition metal substituted  $\text{Li}_3\text{N}$ , forming a marked directional bonding. This remarkable charge polarization indicates formation of both ionic and covalent bonding between N and M, significantly different



**Fig. 3** Valence charge density difference of the plane through substitution site in [001] direction for  $\text{Li}_3\text{N}$  (a), and  $\text{Li}_3\text{N}/\text{Co}$  (b),  $\text{Li}_3\text{N}/\text{Ni}$  (c) and  $\text{Li}_3\text{N}/\text{Cu}$  (d) respectively. The contour interval is  $0.004 \text{ e } \text{\AA}^{-3}$ . The electron accumulation is depicted by pink lines, while the electron depletion is represented by green lines.

from the predominant ionic bonding in  $\text{Li}_3\text{N}$ . A distinct difference is seen between Co/Ni and Cu in the binding with nitrogen. Nitrogen back donates electrons to Co and Ni while does not back donate electrons to Cu. This can be attributed to the unpaired electrons in 3d orbitals in Co and Ni and totally paired electrons in the fully filled 3d orbitals in Cu. The 3d orbitals with unpaired electrons in Co and Ni can accept electrons back donated by nitrogen, while the fully filled 3d orbitals in Cu cannot accept back donated electrons. The covalent bonding between transition metal and N reduces the oxidation state of transition metal and leads to an effective oxidation state below the nominal +2 depending on the covalency. Consequently, this decreases the Li vacancies required to compensate the charge balance derived from the nominal oxidation state of transition metal. This indicates that nonstoichiometric Li vacancies would form in the substituted structure due to the covalent bonding between transition metal and nitrogen.

Therefore, both ostensibly isovalent substitution model and aliovalent substitution model could not capture the apparent oxidation state of transition metal and Li vacancy concentration due to occurrence of the marked covalent bonding between transition metal and N, particularly the apparent charge transfer from nitrogen to Co and Ni. The reported transition metal substituted  $\text{Li}_3\text{N}$  rarely approaches the supposed composition  $\text{Li}_{3-x}\text{M}_x\text{N}$  or  $\text{Li}_{3-2x}\text{M}_x\text{N}$ .  $\text{LiNiN}$  can be regarded as an exception owing to alteration of crystal structure and formation of ordered structure. It is concluded that transition metal substitution results in the formation of  $\text{Li}_{3-x-y}\text{M}_x\text{N}$ , in which  $y$  is dependent on the covalency and concentration of transition metal in the structure. The preparation conditions may also affect the covalency of transition metal, consequently the Li vacancy concentration. For example, a series of  $\text{Li}_{3-x-y}\text{Ni}_x\text{N}$

**Table 2** Comparison of bond lengths in  $\text{Li}_3\text{N}$  and transition metal substituted  $\text{Li}_3\text{N}$ <sup>a</sup>

	$d_{\text{Li}(1), \text{M}-\text{N}}/\text{\AA}$	$d_{\text{Li}(2)-\text{N}}/\text{\AA}$
$\text{Li}_3\text{N}$	1.936 (1.939 <sup>32</sup> )	2.101 (2.106 <sup>32</sup> )
$\text{Li}_3\text{N}/\text{Co}$	1.801 (1.804 <sup>11</sup> )	2.137 (2.156 <sup>11</sup> )
$\text{Li}_3\text{N}/\text{Ni}$	1.844 (1.806 <sup>14</sup> )	2.125 (2.155 <sup>14</sup> )
$\text{Li}_3\text{N}/\text{Cu}$	1.896 (1.886 <sup>11</sup> )	2.116 (2.124 <sup>11</sup> )

<sup>a</sup> Values in the brackets are from experimental observations with nearest substitution concentration.

with  $x = 0.339, y = 0.126$ ;  $x = 0.360, y = 0.162$ ;  $x = 0.362, y = 0.320$ ;  $x = 0.565, y = 0.412$ ;  $x = 0.577, y = 0.188$ ;  $x = 0.743, y = 0.626$  reported by Stoeva *et al.*<sup>14</sup> show that Li vacancy concentrations are higher than 1–2% of  $\text{Li}_3\text{N}$  but lower than the corresponding substitution concentrations with ambiguous correlation.

The covalent bonding between transition metal and N may be further manifested by variation of the bond lengths  $d_{\text{Li}(1), \text{M}-\text{N}}$  and  $d_{\text{Li}(2)-\text{N}}$  as listed in Table 2. The calculated  $d_{\text{Li}(1)-\text{N}}$  and  $d_{\text{Li}(2)-\text{N}}$  in  $\text{Li}_3\text{N}$  are 1.944 Å and 2.106 Å respectively, which is well consistent with the experimental values.<sup>32</sup> Substitution for Li by Co, Ni and Cu reduces the interplanar  $d_{\text{Li}(1), \text{M}-\text{N}}$  in the order  $\text{Li}_3\text{N}/\text{Co} < \text{Li}_3\text{N}/\text{Ni} < \text{Li}_3\text{N}/\text{Cu}$ , while increases the  $d_{\text{Li}(2)-\text{N}}$  in  $[\text{Li}_2\text{N}]$  layer in the order  $\text{Li}_3\text{N}/\text{Co} > \text{Li}_3\text{N}/\text{Ni} > \text{Li}_3\text{N}/\text{Cu}$ . This trend is in agreement with experimental observations.<sup>11,12,23,25,36</sup> However, it is difficult to make strict comparison of the calculated bond lengths with the available experimental values, since these values are dependent on transition metal substitution concentration and Li vacancy concentration.<sup>25</sup> The ionic radii for Co, Ni, Cu and Li in their low oxidation states from Shannon<sup>37</sup> are 0.65, 0.69, 0.77 and 0.76 Å, respectively. The six-coordination values are used here to examine the trend since 2-coordination values are not available for all the ions considered. The apparent decrease of  $d_{\text{Li}(1), \text{M}-\text{N}}$  with substitution for Li by Cu of similar size indicates the covalent bonding between Cu and N. However, the markedly decreased  $d_{\text{Li}(1), \text{M}-\text{N}}$  with substitution for Li by Co/Ni indicates that the dopant size also plays an important role. Covalent bonds between transition metal and N strengthen the interplanar binding, thus the  $d_{\text{Li}(1), \text{M}-\text{N}}$  is reduced with the reduction dependent on the covalent binding strength. The interplanar covalent binding decreases the charge of N, thus weakens the N–Li(2) binding in the  $[\text{Li}_2\text{N}]$  layer. This results in the extension of  $d_{\text{Li}(2)-\text{N}}$ .

The alteration of  $\text{Li}_3\text{N}$  electronic structure with transition metal substitution significantly influences Li vacancy formation. Li vacancies are crucial to the fast Li ionic conduction of lithium nitrides for the hopping of Li ions between occupied Li sites and Li vacancies. Theoretical study has disclosed that Frenkel defect is not possible to be formed in lithium nitride,<sup>38</sup> therefore, Li vacancy is generated from removal of one Li(1) or Li(2) atom in the parent and doped  $\text{Li}_3\text{N}$  supercells. Neutral Li vacancy formation energy  $E_F$  is evaluated as:

$$E_F = E_T(V) - E_T(\text{bulk}) + \mu_{\text{Li}} \quad (2)$$

where  $E_T(V)$  and  $E_T(\text{bulk})$  are the total energies of a supercell with Li vacancy and without vacancy, respectively;  $\mu_{\text{Li}}$  is the

chemical potential of a Li atom removed from the supercell.  $\mu_{\text{Li}}$  is constrained by the following condition:

$$l\mu_{\text{Li}} + m\mu_{\text{M}} + n\mu_{\text{N}} = \mu_{\text{bulk}} \quad (3)$$

where  $\mu_{\text{M}}$  and  $\mu_{\text{N}}$  denote the chemical potential of transition metal and nitrogen atom, respectively, and  $\mu_{\text{bulk}}$  is the chemical potential of the studied system.  $l$ ,  $m$  and  $n$  are the number of constituent atoms Li, M and N, respectively. The total energies of per atom for nitrogen gas, bulk Co ( $P6_3/mmc$ ), bulk Ni ( $Fm\bar{3}m$ ) and bulk Cu ( $Fm\bar{3}m$ ) were chosen as the upper limits of chemical potential of nitrogen, cobalt, nickel and copper, respectively. The calculated total energies per unit formula were applied as the chemical potentials of the studied systems. We consider the Li-poor limitation employed in practical synthetic conditions.

The calculated formation energies  $E_{\text{F}}$  for Li vacancy in Li(1) site  $V_{\text{Li}(1)}$  and in Li(2) site  $V_{\text{Li}(2)}$  are listed in Table 3. It shows that the formation energy of  $V_{\text{Li}(1)}$  is much larger than that of  $V_{\text{Li}(2)}$  in transition metal substituted  $\text{Li}_3\text{N}$  with the same trend as in  $\text{Li}_3\text{N}$ . Thus, Li vacancies mainly form in  $[\text{Li}_2\text{N}]$  layers owing to the energetically favorable process. This is in agreement with the reported Li vacancies in  $[\text{Li}_2\text{N}]$  layers.<sup>11–14</sup>

It is found from Table 3 that Co and Ni substitution reduces the  $V_{\text{Li}(2)}$  formation energy by 0.28 eV and 0.66 eV respectively, while Cu substitution slightly reduces the  $V_{\text{Li}(2)}$  formation energy by 0.06 eV. The effective decrease of  $V_{\text{Li}(2)}$  formation energy with Co and Ni substitution can bring about significant increase of  $V_{\text{Li}(2)}$  concentration, which remarkably improves the Li diffusion, Li ionic conduction and thus the charge–discharge capacity.<sup>8,33</sup> This makes lithium cobalt nitride and particularly lithium nickel nitride outstanding candidates for use as anode materials in rechargeable lithium ion batteries. The slight decrease of  $V_{\text{Li}(2)}$  formation energy with Cu substitution indicates unsubstantial increase of Li vacancy concentration. The distinct discrepancy in  $V_{\text{Li}(2)}$  formation energy between Co, Ni and Cu substituted  $\text{Li}_3\text{N}$  is consistent with the observed back donation of nitrogen electrons in Fig. 3. It seems that N back donates charge into the  $d_{xy}$  orbit of Co in  $\text{Li}_3\text{N}/\text{Co}$  while back donates charge into both  $d_{xy}$  and  $d_{x^2-y^2}$  orbitals of Ni in  $\text{Li}_3\text{N}/\text{Ni}$ , which correlates with the unpaired electrons in 3d orbitals. Back donation of nitrogen electrons to Co and Ni reduces the charge of nitrogen, and thus weakens the binding between N and Li(2), which facilitates the  $V_{\text{Li}(2)}$  formation. Since Ni has more unpaired 3d electrons in the splitted 3d orbitals than Co, thus nitrogen may back donate more electrons in Ni substituted  $\text{Li}_3\text{N}$ , which is beneficial to stabilize the  $V_{\text{Li}(2)}$  containing structure. This can explain the reported better stability on cycling of  $\text{Li}_{3-x}\text{Ni}_x\text{N}$  due to its tolerance to low Li concentration during a wider range of Li deintercalation and intercalation.<sup>32</sup> The low  $V_{\text{Li}(2)}$  formation energy may also lead to the formation of the exceptionally ordered compound  $\text{LiNiN}$ . The ordering reduces

**Table 3** Li vacancy formation energies for  $\text{Li}_3\text{N}$  and transition metal substituted  $\text{Li}_3\text{N}$

	$\text{Li}_3\text{N}$	$\text{Li}_3\text{N}/\text{Co}$	$\text{Li}_3\text{N}/\text{Ni}$	$\text{Li}_3\text{N}/\text{Cu}$
$V_{\text{Li}(1)}$	2.23	1.99	1.88	2.13
$V_{\text{Li}(2)}$	0.52	0.24	−0.14	0.46

the Li ionic mobility but improves the structural stability during charge–discharge cycling. The different effect of Co, Ni and Cu substitution on Li vacancy formation suggests that transition metal substitution could be employed to control the ionic mobility and conduction properties of  $\text{Li}_3\text{N}$  for various electrochemical applications.

Back donated nitrogen electrons seems to correlate with the unpaired electrons in transition metals, therefore, it is possible to predict the effects of other transition metals assuming that their ternary lithium nitrides can maintain the layered  $\text{Li}_3\text{N}$  structures at diluted doping concentrations. Sc, V, Cr and Mn are expected to have unpaired electrons in the splitted 3d orbitals, thus can accept the electrons back donated by nitrogen. Therefore, their substitution for Li may also significantly reduce Li vacancy formation energy, which brings about improved Li ion mobility and conduction. The ionic radii for Sc, V, Cr and Mn in their low oxidation states are 0.75, 0.79, 0.80 and 0.67 Å, respectively.<sup>37</sup> Compared with Sc, V and Cr of similar size to Li or larger than Li, the much smaller Mn can form interplanar covalent binding with N with shortened bond length, which suggests that Mn be a promising candidate for Li substitution for further investigation.

## Conclusions

Transition metal (M = Co, Ni, Cu) substitution significantly influences the electronic structures and the Li vacancy formation of  $\text{Li}_3\text{N}$ . First principles calculations indicate that transition metal substitution takes place mainly at Li(1) sites, which agrees well with the experimental observations. Co or Ni substitution can reduce the energy band gap and even change  $\text{Li}_3\text{N}$  from a semiconductor to a metallic-like conductor, which has the advantage of both electronic and ionic conduction. Transition metal substitution reduces the thermodynamic stability of  $\text{Li}_3\text{N}$ , which might benefit the intercalation and deintercalation of lithium during charge–discharge cycling in rechargeable lithium batteries. Covalent bonding is formed between transition metal atom and the coordinated N, which results in the weakening of the intraplanar binding and the strengthening of the interplanar binding. This reduces the nominal oxidation state of transition metal, and decreases the Li vacancies required for charge compensation, leading to the formation of  $\text{Li}_{2-x-y}\text{M}_x\text{N}_y$  with  $y$  dependent on the transition metal nature and the substitution concentration. Co or Ni substitution brings about remarkable reduction of Li vacancy formation energy in comparison with  $\text{Li}_3\text{N}$ , which is attributed to their 3d orbitals with unpaired electrons to accept the electrons back donated by nitrogen. This leads to significant improvement in ionic mobility and conduction. Therefore, transition metal substitution provides a viable approach to control the electronic properties and electrochemical performance of  $\text{Li}_3\text{N}$  in anode applications. It may render appreciable electronic conduction to the original material and generate a vacancy-controlled charge compensation system for active oxidation–reduction reaction during charge–discharge cycling.

## References

- 1 D. H. Gregory, *Chem. Rec.*, 2008, **8**, 229–239.
- 2 M. Nishijima, T. Kagohashi, M. Imanishi, Y. Takeda, O. Yamamoto and S. Kondo, *Solid State Ionics*, 1996, **83**, 107–111.

- 3 M. Nishijima, T. Kagohashi, Y. Takeda, M. Imanishi and O. Yamamoto, *J. Power Sources*, 1997, **68**, 510–514.
- 4 T. Shodai, S. Okada, S. Tobishima and J. Yamaki, *Solid State Ionics*, 1996, **86–88**, 785–789.
- 5 T. Shodai, S. Okada, S. Tobishima and J. Yamaki, *J. Power Sources*, 1997, **68**, 515–518.
- 6 R. Juza, K. Langer and K. V. Benda, *Angew. Chem., Int. Ed. Engl.*, 1968, **7**, 321–406.
- 7 R. Niewa, D. Zhrebtsov and Z. Hu, *Inorg. Chem.*, 2003, **42**, 2479–2816.
- 8 Z. Stoeva, R. Gomez, D. H. Gregory, G. B. Hix and J. J. Titman, *Dalton Trans.*, 2004, 3093–3097.
- 9 J. L. C. Rowsell, V. Pralong and L. F. Nazar, *J. Am. Chem. Soc.*, 2001, **123**, 8598–8599.
- 10 A. G. Gordon, D. H. Gregory, A. J. Blake, D. P. Weston and M. O. Jones, *Int. J. Inorg. Mater.*, 2001, **3**, 973–981.
- 11 A. G. Gordon, R. I. Smith, C. Wilson, Z. Stoeva and D. H. Gregory, *Chem. Commun.*, 2004, 2812–2813.
- 12 D. H. Gregory, P. M. O'Meara, A. G. Gordon, J. P. Hodges, S. Short and J. D. Jorgensen, *Chem. Mater.*, 2002, **14**, 2063–2070.
- 13 R. Niewa, Z.-L. Huang, W. Schnelle, Z. Hu and R. Kniep, *Z. Anorg. Allg. Chem.*, 2003, **629**, 1778–1786.
- 14 Z. Stoeva, R. I. Smith and D. H. Gregory, *Chem. Mater.*, 2006, **18**, 313–320.
- 15 Y. Liu, K. Horikawa, M. Fujiyosi, N. Imanishi, A. Hirano and Y. Takeda, *Electrochim. Acta*, 2004, **49**, 3487–3496.
- 16 T. Shodai, Y. Sakurai and T. Suzuki, *Solid State Ionics*, 1999, **122**, 85–93.
- 17 S. Suzuki, T. Shodai and J. Yamaki, *J. Phys. Chem. Solids*, 1998, **59**, 331–336.
- 18 F. Bernhardt and R. Hoppe, *Z. Anorg. Allg. Chem.*, 1993, **619**, 969–975.
- 19 W. Burow, J. Birx, F. Bernhardt and R. Hoppe, *Z. Anorg. Allg. Chem.*, 1993, **619**, 923–933.
- 20 A. Möller, *Z. Anorg. Allg. Chem.*, 2001, **627**, 2625–2629.
- 21 A. Möller, M. A. Hitchman, E. Krausz and R. Hoppe, *Inorg. Chem.*, 1995, **34**, 2684–2691.
- 22 M. Sofin and M. Jansen, *Z. Anorg. Allg. Chem.*, 2001, **627**, 2115–2117.
- 23 M. G. Barker, A. J. Blake, P. P. Edwards, D. H. Gregory, T. A. Hamor, D. J. Siddons and S. E. Smith, *Chem. Commun.*, 1999, 1187–1188.
- 24 J. B. Ducros, S. Bach, J. P. Pereira-Ramos and P. Willmann, *Electrochim. Acta*, 2007, **52**, 7035–7041.
- 25 M. T. Weller, S. E. Dann, P. F. Henry and D. B. Currie, *J. Mater. Chem.*, 1999, **9**, 283–287.
- 26 G. Kresse and J. Furthmüller, *Comput. Mater. Sci.*, 1996, **6**, 15–50.
- 27 G. Kresse and J. Furthmüller, *Phys. Rev. B: Condens. Matter*, 1996, **54**, 11169–11186.
- 28 G. Kresse and D. Joubert, *Phys. Rev. B: Condens. Matter Mater. Phys.*, 1999, **59**, 1758–1775.
- 29 J. P. Perdew, K. Burke and M. Ernzerhof, *Phys. Rev. Lett.*, 1996, **77**, 3865–3868.
- 30 J. P. Perdew, K. Burke and M. Ernzerhof, *Phys. Rev. Lett.*, 1997, **78**, 1396–1396.
- 31 H. J. Monkhorst and J. D. Pack, *Phys. Rev. B: Solid State*, 1976, **13**, 5188–5192.
- 32 A. Rabenau and H. Schulz, *J. Less Common Met.*, 1976, **50**, 155–159.
- 33 Z. Stoeva, B. Jäger, R. Gomez, S. Messaoudi, M. B. Yahia, X. Rocquefelte, G. B. Hix, W. Wolf, J. J. Titman, R. Gautier and P. Herzog, *J. Am. Chem. Soc.*, 2007, **129**, 1912–1920.
- 34 K. Miwa, N. Ohba, S. Towata, Y. Nakamori and S. Orimo, *J. Alloys Compd.*, 2005, **404–406**, 140–143.
- 35 M. Gupta and R. P. Gupta, *J. Alloys Compd.*, 2007, **446–447**, 319–322.
- 36 D. H. Gregory, P. M. O'Meara, A. G. Gordon, D. J. Siddons, A. J. Blake, M. G. Barker, T. A. Hamor and P. P. Edwards, *J. Alloys Compd.*, 2001, **317–318**, 237–244.
- 37 R. D. Shannon, *Acta Crystallogr., Sect. A: Cryst. Phys., Diffr., Theor. Gen. Crystallogr.*, 1976, **32**, 751–767.
- 38 J. R. Walker and C. R. A. Catlow, *J. Phys. C: Solid State Phys.*, 1980, **6**, 32–34.