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<td><strong>Author(s)</strong></td>
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GRID-BASED LOCAL FEATURE BUNDLING FOR EFFICIENT OBJECT SEARCH AND LOCALIZATION

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ABSTRACT
We propose a new grid-based image representation for discriminative visual object search, with the goal to efficiently locate the query object in a large image collection. After extracting local invariant features, we partition the image into non-overlapped rectangular grid cells. Each grid bundles the local features within it and is characterized by a histogram of visual words. Given both positive and negative queries, each grid is assigned a mutual information score to match and locate the query object. This new image representation brings in two great benefits for efficient object search: 1) as the grid bundles local features, the spatial contextual information enhances the discriminative matching; and 2) it enables faster object localization by searching visual object on the grid-level image. To evaluate our approach, we perform experiments on a very challenging logo database BelgaLogos [1] of 10,000 images. The comparison with the state-of-the-art methods highlights the effectiveness of our approach in both accuracy and speed.

Index Terms— grid feature, mutual information

1. INTRODUCTION
Visual object search in large image collections is an important technique for many applications, such as object recognition, image annotation and image understanding. Given a query object, our objective is to not only find out in the database all images that contain the object, but also locate the object in these images (see Figure 1). In this respect, visual object search can be viewed as two tasks: object matching and object localization.

Though previous work [2] [1] [3] has been focused on this area in recent years, visual object search, especially for small objects (e.g. logos), remains a challenging problem. On one hand, challenges for object matching mainly come from the fact that the target objects usually differ a lot from the query due to changes in scale, viewpoint or color, or due to partial occlusion. These all lead to difficulties in object matching and thereby we raise the need for a highly discriminative feature. [2] [4] opt for Nearest-Neighbor (NN) classifier to avoid the quantization error caused by the bag-of-visual-words (BOVW) scheme. However, these NN-based algorithms are all under the Naive-Bayes assumption that each feature point is independent from the others. Without considering the spatial context, matching individual features can not provide satisfied results. Besides, searching nearest neighbors for all query feature points is costly in both memory and time, hence prohibiting the application of NN classifiers to large datasets.

On the other hand, object localization is formulated as the problem of finding the subimage with maximum similarity to the query object [2] [5]. Although use of branch-and-bound algorithm can avoid linearly searching all the subimages of an image, object localization is still a computationally expensive job for high resolution images (e.g. 800 x 800 or higher), especially when the target object appears in a small size.

To address the two tasks mentioned above, we propose a grid-based visual object search approach in this paper. We first partition each image into non-overlapping rectangular grids and bundle local features in each grid into a grid feature, which is described as a visual word histogram under the BOVW framework. Then given the positive and negative queries, each grid will be assigned a mutual information score determined by its histogram intersections with both positive and negative sets. Finally the subimage with maximum mutual information, computed as the summation of the mutual information scores of all its grids, is retrieved by the branch-and-bound algorithm.

Our approach contributes to both tasks involved in visual object search. First, for object matching, it improves the matching accuracy in terms of the discriminative grid matching. On one hand, instead of matching individual local features, the bundled features within the grid are matched as a whole. By considering the spatial context, it thus improves
the matching quality. On the other hand, instead of matching the query object only, each grid will match both positive and negative queries to enable a more discriminative matching. Moreover, for object localization, branch-and-bound search on a grid basis drastically reduces both the time and space complexity, as it is essentially performing search on downsampled images.

2. ALGORITHM

This section is organized as follows: firstly we give the definition of the grid feature in § 2.1; then in § 2.2, the mutual information score based on histogram intersection is introduced; § 2.3 describes how to derive the quality bound to enable efficient subimage retrieval via branch-and-bound algorithm.

2.1. Grid Feature

Given an image database \( D = \{I_1\} \), we denote by \( \{f_{i,j}\} \) all the high-dimensional local descriptors extracted from the image \( I_1 \). Follow the BOVW scheme, each local descriptor \( f \) will be quantized to a visual word using a vocabulary of \( K \) words, represented as \( w = \{x, y, d\} \), where \((x, y)\) is the location and \( d \in \{1, \ldots, K\} \) is the corresponding index of the visual word.

Then we partition each image \( I_1 \) into \( M_i \times N_i \) non-overlapped rectangular grid cells \( \{R_{i,m,n}\}, m \in \{1, \ldots, M_i\} \) and \( n \in \{1, \ldots, N_i\} \). A grid feature is then defined as:

\[
G_{i,m,n} = \{w_{i,j}|w_{i,j} \propto R_{i,m,n}\}, \tag{1}
\]

where \( w_{i,j} \propto R_{i,m,n} \) means the point feature \( w_{i,j} \) falls inside the grid cell \( R_{i,m,n} \). Empty grids will be discarded. Furthermore, each grid feature \( G_{i,m,n} \) is represented as a \( K \)-dimensional histogram of visual word occurrences \( h_{i,m,n} \), and indexed by an inverted file to take advantage of its sparsity in most cases. Figure 2 illustrates how to construct and index the grid features.

A grid feature is more discriminative than an individual local feature, as it contains multiple features considered as the context [6] [7]. And with the advantages of BOVW scheme, we need not to store and match all local features in a high-dimensional space. In practise the inverted index results in complexity, as it is essentially performing search on downsampled images.

2.2. Mutual Information Score based on Histogram Intersection

After representing each grid as a sparse histogram \( h_{i,m,n} \), our objective is to evaluate the similarity between each subimage \( I \) and the query object. Here we propose the mutual information score as the similarity measure based on histogram intersection. First let us introduce the Normalization Histogram Intersection (NHI). For any two histogram \( h_1 \) and \( h_2 \), we have:

\[
NHI(h_1, h_2) = \frac{|h_1 \cap h_2|}{|h_1 \cup h_2|} = \frac{\sum_k \min(h_{1,k}^i, h_{2,k}^i)}{\sum_k \max(h_{1,k}^i, h_{2,k}^i)}, \tag{2}
\]

where \( h_{1,k}^i \) and \( h_{2,k}^i \) are the \( k \)-th dimensions of the histograms.

Then we have:

\[
D(G, Q) = 1 - NHI(h_G, h_Q) \in [0, 1]. \tag{3}
\]

Assume that grids are independent from each other, the mutual information score of the subimage \( I \) can be calculated as the summation of the scores of all the grids it contains [2] [8]:

\[
s(I) = MI(Q_+, I) = \log \frac{p(I|Q_+)}{p(I)} = \log \frac{\prod_{G \in I} p(G|Q_+)}{\prod_{G \in I} p(G)} = \sum_{G \in I} \log \frac{p(G|Q_+)}{p(G)} = \sum_{G \in I} \log \frac{p(G|Q_+)}{p(Q_+)} + \log \frac{p(Q_+)}{p(Q_-)+p(G|Q_-) p(Q_-)} = \sum_{G \in I} s(G), \tag{4}
\]

where \( s(G) \) is the mutual information score of a grid feature \( G \). To evaluate the conditional distributions \( p(G|Q_-) \) and \( p(G|Q_+) \), the Gaussian kernel based on histogram intersection is adopted:

\[
\frac{p(G|Q_-)}{p(G|Q_+)} = e^{-\frac{1}{2\sigma^2} \left( D(G, Q_-) - D(G, Q_+) \right)} = e^{-\frac{1}{2\sigma^2} \left( NHI(h_G, h_{Q_-}) - NHI(h_G, h_{Q_+}) \right)}. \tag{5}
\]

Compared to the NN-based method [2] assigning each local feature a mutual information score, the grid-based approach relaxes the Naive-Bayes assumption, as we allow intra-grid dependence over feature points, while still enforcing inter-grid independence.

2.3. Branch-and-Bound Search

For an image \( I \), object localization is formulated as the problem of finding the rectangular region \( I^* \) of \( I \) that has the max-
imum mutual information score to the query:

\[ I^* = \arg \max_{I \subseteq I} \sum_{G \in I} s(G). \] (6)

Since exhaustively locating the subimage is \(O(M^2N^2)\) if the image \(I\) consists of \(M \times N\) grids, here we employ the branch-and-bound algorithm to avoid the exhaustive search. Now given the mutual information score \(s(I)\) as the quality function, in the following we will explain how to derive the upper bound function \(\tilde{s}(I)\), where \(I\) is a collection of subimages in image \(I\).

Similar to the ESS algorithm [5], we assume that there exist two subimages \(I_{\text{min}}\) and \(I_{\text{max}}\) such that for any \(I \subseteq I\), \(I_{\text{min}} \leq I \leq I_{\text{max}}\). Then the upper bound function is defined as:

\[ \tilde{s}(I) = s^+(I_{\text{max}}) + s^-(I_{\text{min}}), \] (7)

where \(s^+(I) = \sum_{G \in I} \max(s(G), 0)\) contains only positive grids, while \(s^-(I) = \sum_{G \in I} \min(s(G), 0)\) contains only negative ones. Both \(s^+(I)\) and \(s^-(I)\) can be computed in \(O(1)\) operations using the integral images. It is easy to see that this \(\tilde{s}(I)\) will meet the two conditions of an upper bound function, as proposed in [5]:

\[ i) \quad \tilde{s}(I) \geq \max_{I \subseteq I} s(I), \] (8)

\[ ii) \quad \tilde{s}(I) = s(I), \text{ if } I \text{ is the only element in } I. \] (9)

Consider that our objective is to find the top-K subimages from the entire image database \(D\), the branch-and-bound algorithm will be initialized using all images \(I_i \in D\). The iteration will stops after the top-K results are returned so that these images with low scores will never be processed.

Essentially, the grid-level subimage search down-samples the images to a lower resolution, which greatly decreases the total number of subimages. In our experiment it performs object search in a database of 10,000 images within seconds. At the same time, memory usage is reduced because the integral images are constructed on grid level as well. For example, an image of resolution 800 \(\times\) 800 only costs 10\(K\) of RAM when the grid size is fixed at 16 \(\times\) 16, while it costs more than 25\(M\) if using the original resolution of 800 \(\times\) 800.

3. EXPERIMENTS

3.1. Experimental Setup

We evaluate our approach on a very challenging logo database of 10,000 images covering various aspects of life and current affairs. As in [1], all images are re-sized with a maximum value of height and width equal to 800 pixels, preserving the original aspect ratio. And in total more than 24 millions scale and affine invariant interest points are extracted by the Harris-Affine detector and described by 128-dimensional SIFT descriptors [9]. Finally all the descriptors are clustered into a vocabulary of 1M visual words using the Hierarchical K-Means (HKM) method in [10].

Since the images in BelgoLogos are of different aspect ratios, in practice we fix the grid size when dividing up the images. We test 4 different grid sizes (8 \(\times\) 8, 16 \(\times\) 16, 24 \(\times\) 24 and 32 \(\times\) 32) and compare their performance. To test the effectiveness of our object search algorithm, 5 external logos used in [2] are selected as the query objects. Meanwhile, we randomly pick out two images containing no logos from the database as the negative queries.

3.2. Results Evaluation

To make a fair comparison with previous work, we evaluate our approach using both Precision/Recall (P/R) scores and Average Precision (AP). Since the BelgaLogo database does not provide the location of each logo in its groundtruth images, we regard the retrieved image containing the query logo as a correct detection. Actually we manually check the correct detections to ensure the bounding box touches the target object. For each query, the top 100 subimages are returned as the retrieval results.

First, we test how the grid size affects AP, as shown in Figure 3. We can see that as the grid size increases, AP of each logo changes in different ways. For instance, AP for the Presidential logo increases while AP for the Ferrari logo falls slightly. The reason is that in the database the President logos always appear in a larger size than Ferrari, and enlarging grid size may risk introducing noise for small logos, hence affecting the precision adversely.

Then we compare our approach with the discriminative mutual information algorithm (DMI) [2] and the baseline method [1]. The grid size is set to 24 \(\times\) 24. Since the published DMI results were evaluated by P/R score, here we compare our precision with it given the same recall. To make a fair comparison, our initial retrieved results are re-ranked by the RANSAC algorithm as is done in the baseline method. The comparison results are showed in Table 1 and Table 2 respectively. It demonstrates that our approach has a significant improvement over DMI; and the re-ranking results are slightly better than that of the baseline method. Furthermore, compared with the baseline method [1] we can accurately operate the object from cluttered background (see Figure 4).
Fig. 4. Examples of search results for 3 logos: President, Dexia and Mercedes. The query is shown on the left, with selected top ranked retrieved images shown on the right.

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<tr>
<th>Grid size</th>
<th>8 × 8</th>
<th>16 × 16</th>
<th>24 × 24</th>
<th>32 × 32</th>
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<tr>
<td>Running time(s)</td>
<td>26.1</td>
<td>13.9</td>
<td>7.2</td>
<td>4.9</td>
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</table>

Table 3. Time cost at different grid scales.

As the time cost was not published in previous papers, here we just present the time cost of our approach and make the comparison between different grid scales. All algorithms are implemented by C++ and run on a single PC of 2.6G Intel CPU and 2G main memory. The running time showed in Table 3 is the average time cost for 5 logos, including query feature extraction, similarity measurement and subimage search. From Table 3 we can see that enlarging grid size significantly speeds up the subimage retrieval.

3.3. Running Time

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4. CONCLUSION

In this paper, we introduce a grid feature to search visual object in a large image collection. By bundling the spatial near-