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Optomechanics with Cavity Polaritons: Dissipative Coupling and Unconventional Bistability

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We study a hybrid system formed from an optomechanical resonator and a cavity mode strongly coupled to an excitonic transition inside a quantum well. We show that due to the mixing of cavity photon and exciton states, the emergent quasiparticles—polaritons—possess coupling to the mechanical mode of both a dispersive and dissipative nature. We calculate the occupancies of polariton modes and reveal bistable behavior, which deviates from conventional Kerr nonlinearity or dispersive coupling cases due to the dissipative coupling. The described system serves as a good candidate for future polaritonic devices.

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Introduction.—Cavity optomechanics is a field of physics which studies hybrid systems of optical resonators coupled to mechanical oscillators [1,2]. A central role there is played by phenomena of radiative pressure and dynamical backaction, which allow optical control of the mechanical system. An ultimate milestone of cavity optomechanics is optomechanical cooling of the mechanical resonator leading to the achievement of the long-thought regime where physics on the boundary of classical and quantum mechanics can be studied. Being realized recently in various optomechanical systems [3], quantum optomechanical coupling triggered numerous proposals and experimental observations of both applied and fundamental interest, including quantum nondemolition measurements [4], possible achievement of the standard quantum limit [5–8], protocols for quantum computing [9], quantum communication [10,11] and optomechanical entanglement [12], optical bistability [13], strong optomechanical coupling [14,15], optomechanically induced transparency [16,17], photon blockade and single-photon emission [18–21], and many others [2].

Cavity optomechanics is essentially a hybrid area of physics, largely involving other components and subsystems to increase the number of applications. In this fashion, optomechanical systems with coupling to single atoms [22], collective spins [23], superconducting qubits [4], cold atom Bose-Einstein condensates [24], quantum dots [25] and carbon nanotubes [26] were studied. Furthermore, the experimental unification of solid-state physics with cavity optomechanics became possible with the growth of semiconductor structures first in a vibrating disk [27] or membrane [28] geometry, and recently in a conventional vertical-cavity surface-emitting laser structure [29].

The aforementioned optomechanical systems are based on the conventional *dispersive* coupling mechanism, originating from the mechanical modulation of the cavity photon frequency. Recently it was realized that another type of photon-phonon coupling, namely *dissipative* coupling, is

possible [30] due to the mechanical modulation of the cavity damping rate. This allows optomechanical cooling in the bad cavity limit [30], reactive optical forces [31], squeezing [32], and leads to Fano line shapes in the force spectrum [33]. However, other optomechanical effects modified by dissipative coupling are yet to be studied.

Another widely studied branch of nonlinear optics, which originates from the strong light-matter coupling between microcavity photons and excitonic transitions, is *polaritonics* [34]. The resulting mixed quasiparticles—exciton polaritons—obey bosonic statistics, have very small effective mass and can form nonequilibrium Bose-Einstein condensates at relatively high temperatures [35,36]. The Kerr nonlinearity appearing from the exciton-exciton interaction, enables polariton bistability [37], which was shown to be useful for optical circuits [38–40] and optical memories [41].

In this Letter, we propose to merge the physics of optomechanics and polaritonics, with both phonon-photon and strong exciton-photon coupling being present. This crucially changes the nature of optomechanical coupling leading to the simultaneous presence of dispersive and dissipative coupling of the phonon mode to the polariton state. Using the master equation we calculate the steady-state solutions for polariton occupation numbers and analyze the bistable behavior coming from two mechanisms of optomechanical coupling. Additionally, we point out that an emergent squeezer-type Hamiltonian for the phonon subsystem appears.

The model.—We study an optomechanical resonator formed by a micropillar with moveable Bragg reflectors, recently realized experimentally in Ref. [29], supplemented with an undoped quantum well (QW) placed in the antinode of the resonator (Fig. 1). Considering a sample with comparably high mirror quality factor ($Q_{\text{opt}} \sim 10^4$), the strong coupling between cavity photons and two-dimensional QW excitons is possible. The generic Hamiltonian of the system can be written as

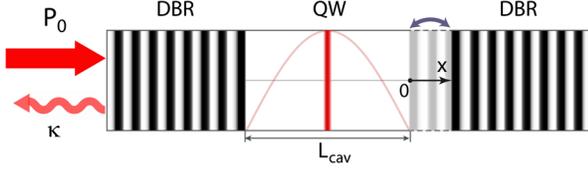


FIG. 1 (color online). Sketch of the system. Optical and mechanical resonators formed by two distributed Bragg reflectors (DBR) with a QW placed in the antinode of an optical cavity. Black (white) stripes correspond to GaAs (AlAs) layers. Here P_0 denotes the pumping rate of an external laser, and κ refers to the decay rate of the cavity photon, and L_{cav} is the cavity length.

$$\hat{\mathcal{H}} = \hbar\omega_{\text{cav}}(x)\hat{a}^\dagger\hat{a} + \hbar\omega_{\text{exc}}\hat{c}^\dagger\hat{c} + \frac{\hbar\Omega}{2}(\hat{a}^\dagger\hat{c} + \hat{c}^\dagger\hat{a}) + \hbar\Omega_m\hat{b}^\dagger\hat{b} + \hbar P_0 e^{-i\omega_p t}\hat{a}^\dagger + \hbar P_0 e^{i\omega_p t}\hat{a}, \quad (1)$$

where \hat{a} , \hat{b} , and \hat{c} correspond to field operators for cavity photons, phonons (oscillation quanta of the mirrors), and QW excitons, respectively, with bare energies $\hbar\omega_{\text{cav}}(x)$, $\hbar\Omega_m$, and $\hbar\omega_{\text{exc}}$. Here, x is a displacement of the mirror, and the mechanical resonator makes $\hbar\omega_{\text{cav}}(x)$ displacement dependent. The third term describes exciton-photon coupling, with Rabi splitting $\hbar\Omega$. Finally, the last two terms in the equation (1) describe the continuous wave coherent pumping of the cavity mode, at rate P_0 and frequency ω_p . For brevity, we neglect exciton-exciton interactions, targeting optomechanical effects.

The strong exciton-photon coupling causes the hybridization of the modes and the first three terms in equation (1) can be diagonalized using lower polariton (LP) and upper polariton (UP) eigenstates, which can be written as $\hat{a}_L = \alpha(x)\hat{a} - \beta(x)\hat{c}$, $\hat{a}_U = \beta(x)\hat{a} + \alpha(x)\hat{c}$, and $\alpha(x)$, $\beta(x)$ are position dependent Hopfield coefficients [42]. To allow a simple quantum description of the system we consider the case of small exciton-photon detuning, $\delta = \omega_{\text{cav}} - \omega_{\text{exc}} \ll \Omega$, and the typical case of small optomechanical displacement, where a linear expansion of the cavity mode frequency can be made, $\omega_{\text{cav}}(x) \approx \omega_{\text{cav}} + x\partial\omega_{\text{cav}}/\partial x + \mathcal{O}[x]^2$ [2]. Using a quantum description, the displacement operator reads $\hat{x} = x_{\text{ZPF}}(\hat{b} + \hat{b}^\dagger)$, where x_{ZPF} is a zero-point fluctuation amplitude defined by the properties of the moving mirror. The LP and UP states are separated in energy and decoupled, such that one can neglect the UP state, assuming the pumping frequency is close to the LP frequency.

The resulting Hamiltonian can be rewritten as a sum of four terms: $\hat{\mathcal{H}} = \hat{\mathcal{H}}_0 + \hat{\mathcal{H}}_{\text{int}}^{(1)} + \hat{\mathcal{H}}_{\text{int}}^{(2)} + \hat{\mathcal{H}}_p$. $\hat{\mathcal{H}}_0$ refers to the energy of free LP and phonon modes,

$$\hat{\mathcal{H}}_0 = \hbar\tilde{\omega}_L\hat{a}_L^\dagger\hat{a}_L + \hbar\Omega_m\hat{b}^\dagger\hat{b}, \quad (2)$$

where the modified LP frequency is

$$\tilde{\omega}_L = \frac{\omega_{\text{cav}} + \omega_{\text{exc}}}{2} - \frac{\Omega}{2} \left(1 + \frac{\delta^2}{2\Omega^2} \right) - \frac{g_0^2}{4\Omega^2}, \quad (3)$$

and g_0 denotes the vacuum optomechanical strength [2].

The interaction part of the Hamiltonian comprises two terms. The first term describes the conventional dispersive polariton-phonon coupling,

$$\hat{\mathcal{H}}_{\text{int}}^{(1)} = -\frac{\hbar g_0}{2}\hat{a}_L^\dagger\hat{a}_L(1 - \delta/\Omega)(\hat{b}^\dagger + \hat{b}), \quad (4)$$

where a weak nonlinear polariton-phonon coupling can be controlled by the exciton-photon detuning δ .

The second interaction term can be written as

$$\hat{\mathcal{H}}_{\text{int}}^{(2)} = -\frac{\hbar^2 g_0^2}{4\hbar\Omega}\hat{a}_L^\dagger\hat{a}_L(\hat{b}^\dagger\hat{b}^\dagger + \hat{b}\hat{b}) - \frac{\hbar^2 g_0^2}{2\hbar\Omega}\hat{a}_L^\dagger\hat{b}^\dagger\hat{a}_L\hat{b}. \quad (5)$$

The first term is quadratic in the phonon operators, corresponding to the typical squeezer Hamiltonian, which can lead to the appearance of nonclassical phonon states suitable for quantum computational schemes. The second term describes polariton-phonon scattering.

Finally, the pumping term for LPs contains both purely static and mechanically modulated terms:

$$\hat{\mathcal{H}}_p = -\frac{\hbar P_0}{\sqrt{2}} \left(1 - \frac{\delta}{2\Omega} \right) (e^{-i\omega_p t}\hat{a}_L^\dagger + e^{i\omega_p t}\hat{a}_L) - \frac{\hbar P_0}{2\sqrt{2}} \frac{g_0}{\Omega} (\hat{b}^\dagger + \hat{b})(e^{-i\omega_p t}\hat{a}_L^\dagger + e^{i\omega_p t}\hat{a}_L). \quad (6)$$

So far we have rewritten the coherent part of the Hamiltonian and have shown that strong exciton-photon coupling leads to the modification of the optomechanical coupling. Now let us consider the changes that it introduces in the incoherent part of dynamics. This can be treated using the master equation approach for the density matrix ρ of the system where $\dot{\rho} = -i/\hbar[\hat{\mathcal{H}}, \rho] + \hat{\mathcal{L}}\rho$, and $\hat{\mathcal{L}}\rho$ corresponds to the Lindblad superoperator, which describes the decay of the cavity photon and exciton modes. Equivalently, we can write the decay terms using the polariton picture [42]. Finally, for the relevant case of the semiclassical approximation, the traced value of the LP Lindblad superoperator reads

$$\text{Tr}\{\hat{\mathcal{L}}\rho[\hat{a}_L]\} = \text{Tr}\left\{ \left[\tilde{\kappa}_L + \frac{g_0(\kappa - \kappa_{\text{exc}})}{\Omega} (\hat{b}^\dagger + \hat{b}) \right] \times (\hat{a}_L\rho\hat{a}_L^\dagger - \hat{a}_L^\dagger\hat{a}_L\rho/2 - \rho\hat{a}_L^\dagger\hat{a}_L/2) \right\}, \quad (7)$$

where we introduced the LP decay rate, $\tilde{\kappa}_L = (\kappa + \kappa_{\text{exc}})/2 - \delta(\kappa - \kappa_{\text{exc}})/2\Omega$, with κ and κ_{exc} being decay rate of bare cavity photon and nonradiative decay rate of an exciton, respectively.

One can see that the decay rate for polaritons is modified, since it shares contributions from both cavity photons and excitons. Moreover, the second term in the first brackets is

influenced by the mechanical system. This corresponds to dissipative coupling between phonons and polaritons. It linearly depends on the ratio of phonon-photon to exciton-photon interaction constants, as well as the difference of decay rates of the modes, and can be modified for particular semiconductor structures. Similarly, due to the relations between pump and decay, the same considerations are valid for the coherent pumping term, Eq. (6), where an analog of the dissipative coupling appears.

Equations of motion.—Knowing the coherent Hamiltonian written for LP states and their mechanically modulated dissipation, we proceed to derive dynamic equations for the mean values of the operators \hat{a}_L and \hat{b} . Here we will focus on the quasiclassical regime, which is judicious for studying optical bistability. Also, we disregard the interaction term $\hat{\mathcal{H}}_{\text{int}}^{(2)}$ in the Hamiltonian (5), which is quadratic in the phonon-photon coupling constant.

Using the master equation, we can write the dynamic equations for the mean value of, e.g., the LP field:

$$\dot{\bar{a}}_L = -\frac{i}{\hbar} \langle [\hat{a}_L, \hat{\mathcal{H}}] \rangle + \text{Tr}\{\hat{a}_L \hat{\mathcal{L}}\rho[\hat{a}_L]\}, \quad (8)$$

where $\bar{a}_L \equiv \langle \hat{a}_L \rangle = \text{Tr}\{\rho \hat{a}_L\}$. The commutators in Eq. (8) can be evaluated using bosonic commutation relations, the trace term rearranged using its cyclic properties, and in the lowest order mean-field approximation (MFA), $\langle \hat{a}_i \hat{a}_j \dots \hat{a}_k \rangle \approx \bar{a}_i \bar{a}_j \dots \bar{a}_k$. This MFA is fully justifiable for the case of relatively high occupation numbers, assuming strong pumping of the cavity mode.

Repeating this procedure for the phonon field, we obtain a closed system of quasiclassical equations:

$$\begin{aligned} \dot{\bar{a}}_L = & i\Delta_L \bar{a}_L + ig_0 \left(1 - \frac{\delta}{\Omega}\right) \underline{A} \text{Re}\{\bar{b}\} \bar{a}_L + \frac{iP_0}{\sqrt{2}} \left(1 - \frac{\delta}{2\Omega}\right) \\ & + \frac{iP_0 g_0}{\sqrt{2}\Omega} \underline{B} \text{Re}\{\bar{b}\} - \frac{\tilde{\kappa}_L}{2} \bar{a}_L - (\kappa - \kappa_{\text{exc}}) \frac{g_0}{\Omega} \underline{B} \text{Re}\{\bar{b}\} \bar{a}_L, \end{aligned} \quad (9)$$

$$\begin{aligned} \dot{\bar{b}} = & -i\Omega_m \bar{b} + \frac{ig_0}{2} \left(1 - \frac{\delta}{\Omega}\right) \underline{A} |\bar{a}_L|^2 \\ & + \frac{iP_0 g_0}{\sqrt{2}\Omega} \underline{B} \text{Re}\{\bar{a}_L\} - \Gamma_m \bar{b}/2, \end{aligned} \quad (10)$$

where we used the frame rotating at the pump frequency, with $\Delta_L = \omega_p - \tilde{\omega}_L$ being the laser-LP detuning, and introduced a decay of the mechanical oscillations with rate Γ_m . We note that the temperature of the environment does not enter the lowest order mean-field equations, and the proper accounting of its influence on the phonon subsystem requires calculations in the higher order MFA [42]. The second terms in the rhs of Eqs. (9) and (10) correspond to typical dispersive couplings, which are modified due to the strong exciton-photon coupling. For

the LP field evolution, Eq. (9), the dissipative coupling appears in both pump and decay terms, being the fourth and the last terms, respectively. On the contrary, the dissipative coupling for the phonon dynamics enters only in the third term in Eq. (10) corresponding to the pump. For convenience we introduced the constants \underline{A} and \underline{B} , which take values 0 and 1, and allow for switching between the dispersive and the dissipative coupling cases.

Finally, given the dynamic equations, we find steady-state solutions of the system, Eqs. (9), setting $\dot{\bar{a}}_L = 0$ and $\dot{\bar{b}} = 0$. Additionally, we can study the stability of these solutions analyzing the spectrum of fluctuations [42,43].

Results and discussion.—Let us now set realistic parameters, considering a system similar to that studied in Ref. [29]. For a GaAs/AlAs $\lambda/2$ micropillar cavity, the cavity wavelength is equal to $\lambda = 870$ nm and we consider a cavity mode lifetime of $\tau = 1/\kappa = 5$ ps. The mechanical resonator is characterized by frequency $\Omega_m/2\pi = 20$ GHz, lifetime $\tau_m = \hbar/\Gamma_m = 60$ ns, $x_{\text{ZPF}} = 5.8 \times 10^{-7}$ nm, and vacuum optomechanical strength $g_0/2\pi = 4.8 \times 10^7$ Hz. The exciton-photon coupling for a single GaAs QW typically gives a Rabi splitting $\Omega/2\pi = 0.48$ THz, which can be increased using a larger number of QWs. The nonradiative exciton lifetime is estimated as $\tau_{\text{exc}} = 1/\kappa_{\text{exc}} = 0.5$ ns.

First, we consider the case of negative laser detuning $\Delta_L = -1.5$ THz (Fig. 2) which is typically required for multibranch solutions in the case of dispersive coupling [2]. In Fig. 2(a) we show the phase diagram of the system as a

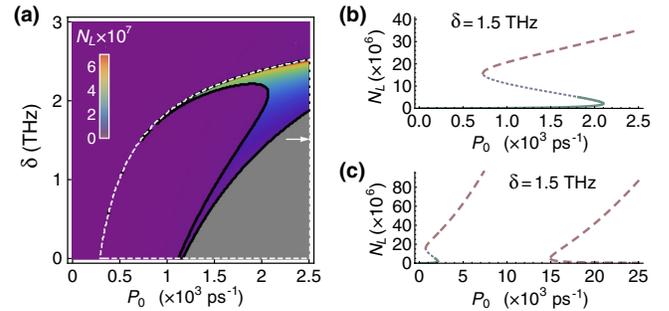


FIG. 2 (color online). (a) Phase diagram showing the LP occupation of the highest intensity stable state for varying δ and P_0 . The dotted white curve represents the boundary between stable and unstable solutions, with the gray region being parametrically unstable. The solid black curve indicates the region where two stable states exist and the system is bistable. The white arrow indicates a cross section for which power dependences are shown in (b)–(c) for low (b) and high (c) pump intensity. (b) Dispersively driven S-shaped mean-field solution for low pump intensity, showing a zoomed-in region of plot (c). (c) Large scale behavior revealing the appearance of dissipatively driven solutions. In (b)–(c) the green solid curves represent stable states, blue dotted curves show the saddle node instability, while magenta dashed curves represent parametrically unstable states.

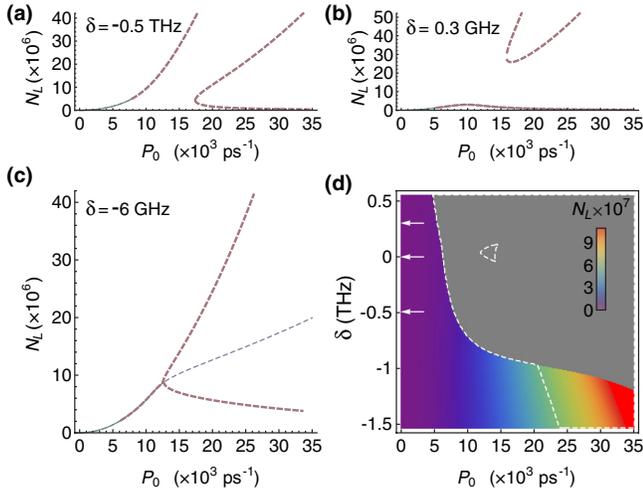


FIG. 3 (color online). (a), (b), (c) Stationary solutions plotted for positive laser detuning $\Delta_L = 3$ THz, and exciton-photon detuning $\delta = -0.5$ THz, $\delta = 0.3$ THz, and $\delta = -6$ GHz, respectively. (d) Phase diagram showing the stability of solutions, with white arrows corresponding to the detunings δ chosen in (a)–(c). The notation coincides with that of Fig. 2.

function of pump intensity P_0 and exciton-photon detuning δ . It reveals a large region with parametrically unstable solutions (white dashed area), which corresponds to the presence of Hopf bifurcation in the system, while a bistable region is denoted by the black curves. The former can be explained by the fact that the chosen parameters correspond to the unresolved sideband regime with small mechanical damping, where the optomechanical system deviates from the Kerr-nonlinear-like behavior [44]. The LP occupation numbers $N_L = |\bar{a}_L|^2$ are given in Figs. 2(b) and 2(c) for positive exciton-photon detuning $\delta = 1.5$ THz, showing low (b) and high (c) pump intensity regions. In the low pump strength region we observe an S -shaped behavior of the LP occupation number, characteristic of dispersive coupling. Here the bistable window is present, accomplished by the single-mode unstable middle branch, and parametrically unstable upper branch [Fig. 2(b)]. At the higher pump intensity, a dissipative coupling mechanism comes into play, leading to the appearance of a second branch solution [Fig. 2(c), right]. However, for the chosen system parameters it is parametrically unstable. While the calculations were done in lowest order MFA assuming a zero environment temperature, in the Supplemental Material we performed an analysis of temperature effects and found that their contribution is negligible for the considered occupation numbers [42].

Next, we examine the case of positive laser detuning Δ_L , which is usually overlooked in the dispersive coupling case, being characterized by the single-mode optical limiter solution. However, here the dissipative coupling plays a major role, leading to the aforementioned double-branch

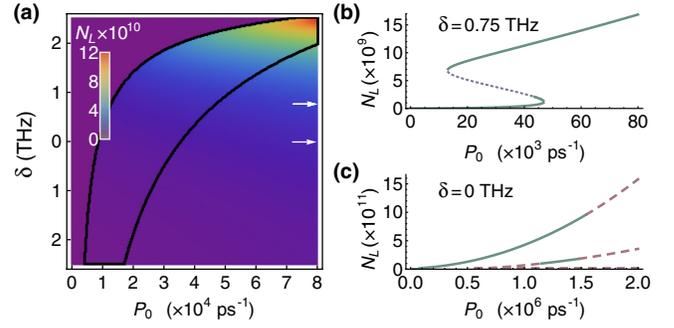


FIG. 4 (color online). Unconventional bistability of the modified system, where mechanical oscillator damping is increased, $\tau_m = 1.2 \times 10^{-14}$ s, $Q_m = 2$, and negative laser detuning $\Delta_L = -1.5$ THz. (a) Phase diagram showing a large bistable window, and the absence of parametric instability. (b) Stationary solutions with S -shaped bistability present at small pump intensity. (c) Solutions for high pump intensity showing unconventional bistability, fully driven by the dissipative coupling.

solution for large exciton-photon detuning δ [Fig. 3(a)], and a modified unstable branch for small detuning [Fig. 3(b)]. An intriguing behavior of the modes is revealed for the case of intermediate detuning δ shown in Fig. 3(c), where three solutions incorporate two branches with Hopf bifurcation corresponding to unstable behavior and a middle single-mode unstable branch, though much different from the conventional S -shaped form. We verify that this behavior is a result of the complex interplay between both dispersive and dissipative couplings by switching on and off the couplings, finding that for $\underline{A} = 0$, $\underline{B} = 1$ and $\underline{A} = 1$, $\underline{B} = 0$ only single solutions are present [42]. In Fig. 3(d) we supplement the mean-field solutions with a phase diagram, indicating the stable and parametrically unstable regions. Numerical modeling of the system dynamics reveals self-sustained oscillations in the mechanical amplitude $x = x_{ZPF}(\bar{b} + \bar{b}^*)$, representing a potential tunable saser [42]. Additionally, we observed anharmonic oscillations of polariton density, leading to the Q -switching behavior of a polariton laser [42].

Finally, in Fig. 4 we present calculations for a theorized system, where parameters satisfy the resolved sideband regime with large mechanical damping, where $\Gamma_m > \kappa$, and the mechanical resonator quality factor Q_m is of the order of unity. This enlarges the region of stable solutions [Fig. 4(a)]. Here a bistable region appears for the S -shaped solution at small pump intensities [Fig. 4(b)]. Moreover, it reappears in the high pumping region, which is fully governed by the dissipative coupling mechanism, manifesting an unconventional bistability present in the system.

Conclusions.—We considered an optomechanical system, where a cavity mode is additionally strongly coupled to a quantum well exciton. Because of the modification of the eigenstates of the system, the mechanical coupling

contains both dispersive and dissipative channels. This strongly modifies the stationary states of the system, which can demonstrate both unconventional bistable and parametrically unstable behavior.

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