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Disorder and spectral line shapes in two-level systems

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Using a stochastic model, we examine disorder-induced changes in the absorption line shape of a chromophore embedded in a matrix of noninteracting two-level systems (TLSs) with randomly oriented dipole moments. By systematically controlling the degree of TLS positional disorder, a perfectly crystalline, glassy or a combination of the two environments is obtained. The chromophore is assumed to interact with TLSs via long-range dipole-dipole coupling. At long times and in the absence of disorder, Gaussian line shapes are found, which morph into Lorentzian for a completely disordered environment owing to strong coupling between the chromophore and a TLS in close vicinity.

Keywords: Absorption line shape, Two-level systems, Disordered media.

I. INTRODUCTION

With the advent of low-temperature single molecule spectroscopy (SMS), it has become possible to probe the immediate microscopic environment of a single molecule of interest, such as chromophores embedded in organic glasses.1–4 SMS has been employed mostly to measure the absorption spectral line-shape,5–8 typically by fluorescence excitation techniques.9 In the presence of a medium, the transition frequencies of molecules are altered due to the fluctuations of the local environment, resulting in absorption spectrum broadening.10 The optical spectroscopy of chromophores at low concentration can thus play an important role in elucidating the structure and dynamics of solids, especially at very low temperatures. The absorption spectrum of a dilute chromophore in glass or structurally disordered solvents is usually inhomogeneously broadened,11–14 which is related to the local disorder around the chromophore.

The model of a collection of two-level systems (TLSs)15–20 has been satisfactorily employed to study many properties of amorphous systems such as the anomalous specific heat and thermal conductivities.21–27 Within the context of glassy systems, such a TLS is considered to be manifestation of an asymmetric double well potential with respect to some collective configurational coordinate. Typically the two local minima on the potential energy surface are believed to arise from local rearrangements of atomic or molecular clusters.28 Flipping between the two eigenstates is suggested to occur by phonon-assisted tunneling at low temperatures.28–30 Despite decades of research, only a few pointers to interpretations of TLSs such as their speculated relation with the motion of domain walls in glasses31 and possibility of studying the validity32 of standard TLS model with SMS experiments have emerged, and a fundamental understanding of their physical meaning and origin remains largely elusive. In their study of absorption line shape by Orth et al.,27 it was found that the defect density is an important parameter and under the assumption of dipolar-dipolar TLS-chromophore interactions, the line shape changes from Lorentzian to Gaussian form as the defect density is changed from very low to high values, respectively.

In this Letter, we aim to investigate the specific role of disorder on absorption line shape of a chromophore coupled to a collection of noninteracting flipping TLSs. With the introduction of a disorder parameter to simulate different environments, we calculate the absorption line shape as an average over an initial distribution of static TLS configurations. This paper is organized as follows. The details of underlying theoretical model and computational methodology are described in Section II. The results obtained on the analysis of absorption line shapes by both the theoretical and the computational approaches are presented and discussed in Section III. In the final Section IV, conclusions are drawn.

II. THEORETICAL MODEL AND COMPUTATIONAL DETAILS

The chromophore as a TLS with the ground (|g⟩) and excited (|e⟩) electronic states separated by energy equal to hωeg, is coupled to a collection of TLSs6,10,33,34 representing the host solid environment. It is essential to note that even though the chromophore and the host matrix are represented as TLSs, they possess distinctly different characteristics. The TLS of the chromophore, which can also be considered as an optical impurity, refers to its two electronic levels (ground state |g⟩ and excited state |e⟩). The TLSs representing the solid matrix, on the other hand, correspond to the double-well potential states. This standard model is depicted schematically in Figure 1. The two zeroth-order states of a TLS localized in the left well |L⟩ and the right well |R⟩ of the potential are separated by an energy barrier justifiably assumed to be infinite, at low temperatures. The Hamiltonian for a TLS can be completely specified by two parameters: ΔJ, the energy asymmetry between the localized...
the perturbation that the statistical properties of temperature, and rate. Assuming the relaxation to be dominated by phonon-assisted tunneling, we can write the renormalized transition frequency of the chromophore as \(\omega_{\text{eg}} = \omega_{\text{eg}}^0 + \sum_j v_j \xi_j\), where \(\omega_{\text{eg}}^0\) is the unperturbed chromophore transition frequency and \(v_j\) is the perturbation that the \(j\)th TLS in its excited state induces to the chromophore transition frequency. Statistical properties of \(\xi_j\) are determined by the relaxation rate \(K_j = k_j^u + k_j^d\) where \(k_j^u\) (\(k_j^d\)) is the upward (downward) rate. Assuming the relaxation to be dominated by phonon-assisted tunneling, we can write\(^{33}\):

\[
k_j^u = C \epsilon_j M_j^3 \frac{\exp(-\epsilon_j/k_BT)}{1 - \exp(-\epsilon_j/k_BT)} \tag{1a}
\]

\[
k_j^d = C \epsilon_j M_j^3 \frac{1}{1 - \exp(-\epsilon_j/k_BT)} \tag{1b}
\]

where \(C\) is the TLS-phonon coupling constant, \(T\) is temperature, and \(\epsilon_j = \sqrt{A_j^2 + M_j^2}\) is the energy separation of the eigenstates of the \(j\)th TLS. In thermal equilibrium, the probability of finding the \(j\)th TLS in state \(k (k = 0, 1)\) is \(P_j^k\), which is given as:

\[
P_j^k = p_j \delta_{k,1} + (1 - p_j) \delta_{k,0} \tag{2}
\]

where \(p_j = [\exp(\epsilon_j/k_BT) + 1]^{-1}\) is the probability that the \(j\)th TLS is excited, and \(k_B\) is Boltzmann constant.

The approach proposed by Reilly and Skinner is adopted to derive the time-domain response function \(J(t)\) from the product of individual response functions \(J_j(t)\)\(^{6,34}\) and the linear absorption line-shape function \(\sigma(\omega)\) is then given by the Fourier transform of the response function \(J(t)\). The interaction between the chromophore and the \(j\)th TLS has the form

\[
v_j = B f_j \frac{B(n_j \cdot n - 3(n_j \cdot \hat{r}_j)(n \cdot \hat{r}_j))}{r_j^3} \tag{3}
\]

where \(f_j\) is a dimensionless angular factor calculated assuming dipolar coupling between the chromophore and the \(j\)th TLS, whose positions (dipole directions) are \(\mathbf{r}_j\) and \(\mathbf{n}_j\) (\(\mathbf{n}\) and \(\mathbf{n}_j\), respectively; \(\mathbf{r}_j = |\mathbf{r}_j - \mathbf{r}|\) and \(\hat{\mathbf{r}}_j = (\mathbf{r}_j - \mathbf{r})/r\) are the distance and the direction between them, respectively; \(B = A_j C'/\epsilon_j\) with \(C'\) as the TLS-chromophore coupling constant. The approximation of dipole-dipole coupling between the chromophore and the TLSs is commonly employed in most of the studies of such systems and is well supported by spectroscopic studies. Such nonresonant coupling between the chromophore and TLSs is thought to be mediated by a strain field resulting from conformational state transitions,\(^{36,38,39}\) thereby implying that a TLS can behave like an ‘elastic dipole moment’.\(^{22,40}\)

We first describe the numerical approach, in which a simple cubic lattice of TLSs with one chromophore at a substitutional site is considered. The dipole directions are randomly distributed, with the azimuthal angle \(\theta\) in the \(xy\) plane and the polar angle \(\phi\) defined in the standard way from the and \(x\) and \(z\) axis, respectively such that \(-1 \leq \cos \theta < 1\) and \(-\pi \leq \phi < \pi\). The simulation volume is divided into 1331(11 \times 11 \times 11) unit cells each of a side length of \(a_0\). The central unit cell is occupied by the sole chromophore, while other cells contain one TLS in each. As shown in Figure 2, the precise position of the chromophore or a TLS is assigned to a randomly selected point inside an even smaller cubic subunit of sides of length \(w = \alpha a_0\), with \(\alpha\) as the parameter to control the degree of spatial disorder. For \(\alpha = 0\), all the TLSs occupy points on the simple cubic lattice. An increase in \(\alpha\) implies an increase in the perturbation in the positions about the lattice points. Thus, \(\alpha = 1\) corresponds to a completely random distribution of TLSs, thereby simulating a glassy environment. The intermediate cases denote the varying degrees of amor-
phous nature of the TLS environment. The TLSs themselves are assumed to be non-interacting, as such TLS-TLS coupling is known not to affect the absorption line shape. In our calculations, we set $C = 3.9 \times 10^8 \text{K}^{-3} \text{s}^{-1}$, $C' = 3.75 \times 10^{11} \text{nm}^3 \text{s}^{-1}$, $M_j = 0.008 \text{K}$, $A_j = 0.006 \text{K}$, $a_0 = 4.43 \text{ nm}$, $T = 1.7 \text{ K}$, which are representative of typical glassy systems. In numerical results, frequencies are expressed in the units of $B/e_0^3$. The total simulation time is set to 20 ns and results are averaged over 30,000 randomly sampled iterations.

### III. ABSORPTION LINE SHAPES

The numerical simulations with the aforementioned parameters correspond to the high-temperature and static regime, which allows us to set, while maintaining accuracy, $p_j = 0.5$ and $K_j = 0$, that yields $J_j(t) = (1 + e^{-jv_jt})/2$, in full accordance with the well-known expression for the static limit. Furthermore, in the presence of disorder, the value $J(t) = (J(t))$ that describes the line shape, with angular brackets denoting average over the disorder, as well as dipole directions, can be represented in a form

$$\bar{J}_j(t) = \frac{1}{\Omega_j} \int dr \rho(r) \int dn \bar{J}_j(t, r, n)$$

$$= \frac{1}{\Omega_j} \int dr \rho(r) \int dn \bar{J}_j(t, r, n)$$

$$\bar{J}_j(t, r, n) = \int dr \rho_j(r) \int dn \frac{1 + e^{-jv_jt}}{2}$$

where $\rho(r)$ and $\rho_j(r)$ are the distributions functions of the chromophore and TLSs positions, respectively, with the homogeneous distributions over the dipole directions, as assumed in our numerical simulations. The integration measures in Eqs. (4) and (5) are normalized

$$\int dn = \int dn_j = \int dr \rho_j(r) = \int dr \rho(r) = 1$$

In order to explicitly calculate the integral over $n_j$ in eq (5), we first represent $v$ as:

$$v = \frac{B}{r_j^3} |n - 3(n \cdot \hat{r}_j)\hat{r}_j| \cdot n_j.$$

Using $|n - 3(n \cdot \hat{r}_j)\hat{r}_j| = \sqrt{1 + 3(n \cdot \hat{r}_j)^2}$, we obtain

$$\int dn_j e^{-jv t} = \frac{1}{4\pi} 2\pi \int_0^\theta \sin \theta d\theta$$

$$\times \exp \left( \frac{iBt}{r_j^3} \sqrt{1 + 3(n \cdot \hat{r}_j)^2} \cos \theta \right)$$

$$= \frac{\sin (\Omega_j(t))}{\Omega_j(t)}.$$

where we have introduced

$$\Omega(r_j) = B \sqrt{1 + 3(n \cdot \hat{r}_j)^2}.$$  \hspace{1cm} (9)

Substituting eq (8) into eq (5) we arrive at

$$\bar{J}_j(t, r, n) = 1 - p_j \int dr \rho_j(r) h(r_j, t),$$

by introducing

$$h(r_j, t) = 1 - \frac{\sin (\Omega(r_j)t)}{\Omega(r_j)t} = 1 - x \sin \frac{1}{x},$$

and keeping the arbitrarily valued $p_j$ rather than setting it to 0.5. Note that the function $h(r_j, t)$ is continuous (although not smooth) at $r_j = 0$, and $h(r_j, t) \sim r_j^{-6}$ for large values of $r_j$.

If the distributions $\rho_j(r_j)$ have the property of $\Omega(r_j)t \ll 1$ for relevant times $t$, we write $h(x) \sim 1/(6x)^2$ and obtain

$$\bar{J}_j(t, r, n) = 1 - g_j(t, r, n) \approx \exp(-g_j(t, r, n)),$$

with

$$g_j(t, r, n) = -\sigma_j(r, n) \frac{t^2}{2},$$  \hspace{1cm} (13)

and

$$\sigma_j(r, n) = \sum_{ab=1}^3 \alpha_{ab}^{(r)n^a n^b},$$  \hspace{1cm} (14)

where $a$ and $b$ label the cartesian coordinates, and

$$\alpha_{ab}^{(r)} = 2p_j B^2 \int dr \rho_j(r) \frac{\delta_{ab} + 3r^a r^b}{6r^a r^b}.$$  \hspace{1cm} (15)

If the approximation made to derive eq (12) is valid for all TLSs, we have

$$\bar{J}(t, r, n) = \exp \left( -\frac{t^2}{2} \sum_{ab} \alpha_{ab}^{(r)} n^a n^b \right),$$

with

$$\alpha_{ab}^{(r)} = \sum_j \alpha_{ab}^{(r)}(r_j),$$  \hspace{1cm} (17)

which means that under the above assumption and if the position and dipole direction of the chromophore is fixed, the absorption line, even in the presence of positional and dipole-orientational disorder of the TLSs, has a Gaussian shape. Disorder in the chromophore position, as well as random distribution of its dipole orientation will create deviations from the Gaussian shape.

There is still a situation when random orientations of the chromophore dipole do not cause the absorption line.
Figure 3: (a)-(d) The calculated absorption line shapes fitted with the Gaussian (G), Lorentzian (L) and their linear combinations for $\alpha = 0.0, 0.4, 0.8$ and 1.0, respectively.

to deviate from Gaussian shape, namely when the chromophore is fixed at the center of its cell $r = 0$, or equivalently, $\rho(r) = \delta(r)$, whereas the distribution functions of the TLS positions preserve the symmetry of the cubic lattice (note that disorder considered in this work obviously satisfies the above property). In this case we deal with $\alpha^{ab}(0)$, as defined for the general case by eq (17), that can be viewed as a symmetric rank 2 tensor, invariant under the rotations that preserve the cubic lattice. A tensor that satisfies the above property is known to be, up to a scalar multiplicative factor, the Kronecker delta $\delta^{ab}$, which implies

$$\alpha^{ab}(0) = \frac{1}{3} \text{Tr}[\alpha(0)]\delta^{ab}.$$  \hspace{1cm} (18)

Taking the trace in eq (15), and making use of Eqs. (17) and (18) we obtain

$$\bar{J}(t; 0, n) = \exp \left(-\frac{\sigma t^2}{2}\right),$$  \hspace{1cm} (19)

with

$$\sigma = \sum \int dr_j \rho_j(r_j) \frac{B^2}{3|r_j|^6},$$  \hspace{1cm} (20)

which yields the Gaussian line shape independent of the chromophore dipole orientation $n$, and therefore, invariant upon any averaging over the latter.

Figure 3 shows the frequency-domain absorption line shapes calculated numerically for $\alpha = 0.0, 0.4, 0.8$ and 1.0, as well as their fitting by Gaussian (G) and Lorentzian (L) functions with the same FWHM and their linear combinations $\alpha L + (1-\alpha)G$. For the perfectly crystalline environment ($\alpha = 0.0$), as seen in Figure 3(a), the line shape is of Gaussian profile, in agreement with our theoretical prediction and previous results. \textsuperscript{27,42} Furthermore, we have verified that the value of $\sigma = 1.956 \times 10^{-5}$ ps\textsuperscript{-2} obtained by applying eq 20 to our model, yields a satisfactory fit to the averaged response function $\bar{J}(t)$.

We further note that for $\alpha = 0.0$, while all the TLSs on a regular lattice, their dipole moments are randomly oriented implying simply the steric disorder. After averaging over the distribution of dipole directions, the interactions along different directions will be different, which may result in the inhomogeneously broadened Gaussian profile. This is consistent with earlier results showing the broadening due to the static heterogeneity to be inhomogeneous. \textsuperscript{43}

With an increase in $\alpha$, a change in line shape as well as an increase in the full width at half-maximum (FWHM) can be observed in Figures 3(b)-(d). As the finite FWHM results from the chromophore-TLS interactions, it is apparent that the stronger the interaction, the greater its influence on the broadening. This implies that as $\alpha$ increases, the average chromophore-TLS separation will tend to decrease thereby leading to an increase in FWHM. Evident from the Figure 3(d), for $\alpha = 1.0$ which represents the glassy environment, the line shape is fitted well by a Lorentzian. For this case, as the TLSs are completely disordered in both spatially and steric sense within their residence cells. Therefore, after averaging over a large number of initial conditions, the distribution of the TLSs around the chromophore should be statistically isotropic, and one can observe homogeneous broadening which can induce the Lorentzian profile. In the intermediate regime, the degree of spatial disorder increases gradually thereby leading to a gradual change from inhomogeneous to homogeneous influence of the environment, and thus the absorption line shape can be approximately fitted by a superposition of the individual G and L components, $\alpha L + (1-\alpha)G$ [see Figure 3 (b) to (c)]. In essence, we observe a smooth transition of the line shape from Gaussian to Lorentzian with an increase in spatial disorder of the host medium to the chromophore.

To gain further insights into disorder-induced changes in the line shapes, we examined the binning-statistics of chromophore-TLS pairwise distances, especially in the regime of pairwise distances equal to or less than $a_0$. Whereas for $\alpha = 0$ the minimum separation is equal to $a_0$, that for $\alpha = 1$ can even be vanishingly small. The presence of TLSs in such close proximity of the chromophore implies a much stronger perturbation to the transition frequency of the chromophore as compared that due to the relatively distant TLSs. We carried out constrained simulations such that the chromophore and its 6 nearest neighbors are fixed to the corresponding lattice points, while allowing their transition dipoles to be randomly oriented. The rest of the TLSs are subjected to the condition of $\alpha = 1$, and thus, the smallest possible separation is $\sqrt{2}a_0$ (see inset in Figure 4). The resulting absorption line shape depicted in Figure 4 is found to be Gaussian. This implies that the aforementioned transition from Gaussian to Lorentzian line shape when $\alpha$ is changed from 0 to 1 can be ascribed to the strong...
Figure 4: The absorption line shape and its fitting by a Gaussian (G) and Lorentzian (L) functions when $\alpha = 1.0$, and the chromophore and its 6 nearest neighbor TLSs are fixed at the centers of their unit cells. The inset shows the pairwise distance distribution.

The effect exerted by the TLSs in the immediate vicinity of the chromophore. This argument is further supported by Figure 5 in which the absorption line shapes for $\alpha = 1.0$ for various lattice sizes. The line shapes yielded even by the smallest possible lattice size is nearly the same as that by the larger lattices, barring a small difference in the peak amplitude. As seen from the inset therein, both the FWHM and the peak intensities are satisfactorily converged. This again emphasizes that even for the largest lattice size studied in this work, the predominant contribution to the spectral line shape is provided by the close TLS neighbors of the chromophore.

The qualitative analysis, as well as the quantitative arguments, presented above, clearly demonstrate that the substantial deviation from the Gaussian line shape in the case of complete or almost complete disorder originating from the configurations when a TLS come close to the chromophore, and the approximation, invoked to derive eq (12), is no longer valid. To rationalize the Lorentzian line shape in the $\alpha = 1$ case of complete disorder we start with considering a similar, yet not less physical model of disorder when the chromophore position is fixed, whereas $N$ identical TLSs are independently and randomly distributed inside some region $\mathcal{U} \subset \mathbb{R}^3$ of large enough size with volume $V$. Formally, this means that

$$\rho_j(r_j) = V^{-1}, \quad r_j \in \mathcal{U}, \quad j = 1, \ldots, N.$$  

In substituting eq (21) into eq (10) we can make use of the $\sim r_j^{-6}$ behavior of $h$ at large values of $r_j$, as well as the assumption of large size of $\mathcal{U}$, and extend integration in eq (10) from $\mathcal{U} \subset \mathbb{R}^3$ to the entire Euclidean space $\mathbb{R}^3$, followed by switching to the variables $r_j = (x, \hat{r}_j)$ with $x = (\Omega t)^{-1}$, which results in

$$\tilde{J}_j(t) = 1 - \frac{\zeta B}{V} t \approx e^{-\zeta gBV^{-1} t},$$  

with the dimensionless factor

$$\zeta = \frac{4\pi}{3} \int_0^1 d\tau \sqrt{1 + 3\tau^2} \int_0^\infty dx \left(1 - x \sin \frac{1}{x}\right)$$

$$= \frac{\pi^2}{3} \int_0^1 d\tau \sqrt{1 + 3\tau^2}.$$  

Finally we arrive at

$$\tilde{J}(t) = (\tilde{J}_j(t))^N = e^{-\gamma t}, \gamma = \zeta p B n,$$  

where $n = N/V$ is the TLS concentration, which immediately leads to the Lorentzian line shape. Note that $B n$ has a meaning of a typical dipole coupling, i.e., the value of the dipole coupling at the average distance $a_0 = (n)^{-1/3}$ between the chromophore and a TLS, and $\zeta$ is a dimensionless factor of the order of 1 that reflects a particular model of disorder.

We are now in a position to consider the model of disorder that has been used in our numerical simulations, and thus introduce the line shape function $g(t)$ so that

$$\tilde{J}(t) = e^{-g(t)}.$$  

The short-time asymptotic corresponding to $\gamma t = B t/a_0^3 \ll 1$ can be computed by noting that the contribution to $J(t)$ in this case is dominated by configurations with $|r_j - r| \ll a_0$, which is possible only if both $r_j$ and $r$ are located in the close vicinity of the chromophore cell border. The major contribution from each face thus comes from the coupling between the chromophore and the TLS that resides in the cell on the opposite side of the face. The line shape function can then be obtained by performing the integration in this restricted regime. On the other hand, for calculating the long-time asymptotic, we employ the fact that each of the cells containing a
TLS contributes to $J(t)$ and thus integration can be performed over the whole Euclidian space $\mathbb{R}^3$. Thus, for our $\alpha = 1$ model of disorder we finally obtain:

$$
\begin{align*}
g(t) &= \zeta_s(\gamma_0 t)^{4/3}, \quad \text{for } \gamma_0 t \ll 1, \\
g(t) &= \zeta_L(\gamma_0 t), \quad \text{for } \gamma_0 t \gg 1. \quad (26)
\end{align*}
$$

where

$$
\zeta_L = -\frac{4\pi}{3} \int_0^1 d\tau \sqrt{1 + 3\tau^2} 
\times \int_0^\infty dx \ln \left( 1 - p + px \sin \left( \frac{1}{x} \right) \right), 
$$

and

$$
\zeta_s = 4\pi p \int_0^1 d\tau \left( 1 + 3\tau^2 \right)^{2/3} 
\times \int_0^\infty dx x^{1/3} \left( 1 - x \sin \left( \frac{1}{x} \right) \right). \quad (28)
$$

For the model used in this work, we have evaluated eq (27) and eq (28), and the obtained value of $\zeta_s \gamma_0^{4/3} = 2.26 \times 10^{-3}$ ps$^{-4/3}$ is found yield a satisfactory fit to the $\tilde{J}(t)$, in the short-time limit. At long times, on the other hand, the calculated value of $\zeta_t \gamma_0 = 7.36 \times 10^{-3}$ ps$^{-1}$ is roughly two times smaller than that obtained by fitting $\tilde{J}(t)$ in the long-time limit.

IV. CONCLUSIONS

In summary, we have systematically investigated the influence on the absorption line shape of a chromophore of the disorder in the solid matrix in which it is embedded. In the absence of disorder, the absorption line shape is revealed to be of inhomogeneously broadened Gaussian form, whereas in a glassy environment, it is found to be of homogeneously broadened Lorentzian profile. We have demonstrated both theoretically and numerically that the origin of the Lorentzian line shape in glassy systems lies in enhanced chromophore-TLS coupling due to close proximity. An interesting parallel can be drawn from our earlier studies of finite sized single-domain micromagnetc particle arrays, in which disorder was found to lead to an increase in the coercitivity. Our results thus emphasize on a broader perspective, that the disorder in the environment of a system of interest can significantly impact its macroscopic observables and provide insights in elucidating the nature of immediate microscopic enviroment of a chromophore from studying its absorption line shapes.

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