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Relative Intensity Noise of Silicon Hybrid Laser

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Abstract—We theoretically investigate the relative intensity noise (RIN) of a silicon hybrid laser by taking into account two-dimension transverse modes in the hybrid waveguide. It shows that, when only one transverse mode is excited, RIN spectrum of the hybrid laser exhibits a larger peak value at a lower relaxation oscillation (RO) frequency as compared to the case of a conventional multiple-quantum well (MQW) laser with the same active region design and dimension. In contrast, when two transverse modes are excited, the hybrid laser shows a lower peak value at a higher RO frequency as compared to the MQW laser. The effects of waveguide dimensions e.g., Si ridge height and III-V ridge width on RIN spectra of the hybrid laser are also investigated.

Index Terms—Relative Intensity Noise (RIN), semiconductor laser, silicon photonics, transverse modes.

I. INTRODUCTION

The on-going rapid development of microprocessor chips is facing several challenges, e.g., limited bandwidth, capacity and heat dissipation. To overcome these challenges, there are tremendous interests in developing silicon-on-insulator (SOI) platforms to replace the current electrical interconnects and networks with optical counterparts. Although SOI amplifiers [1], modulators [2], and detectors [2] have already been demonstrated on SOI platforms, optical lasing from silicon becomes a bottleneck to fully realize this platform due to its intrinsic indirect bandgap. Optically pumped Raman lasers [3], rare-earth doped Si rich oxides lasers [4], etc. have been demonstrated in silicon, but they could not fully act as transmitters in the platform because of their restricted performance and operation conditions. Recently, an electrically pumped silicon hybrid laser has been demonstrated based on wafer-to-wafer bonding techniques [5]. This hybrid laser is constructed by the integration of III-V epitaxial wafers on SOI wafers, followed by standard photolithograph and etching processes to define the device structure. The advantages of large-scale low-cost integration and relaxed alignment requirements make it a suitable candidate for the platform. With similar technology and concepts, other devices, e.g., racetrack [6], distributed feedback (DFB) [7], mode-locked silicon hybrid laser [8, 9] and amplifier [10] as well as detector [11], are also successfully demonstrated.

To be a promising and reliable candidate for the platform, a hybrid laser with excellent noise performance is highly desired. As one of the noise sources, relative intensity noise (RIN) is an important indicator for intensity stability of devices. A low RIN results in a low error rate in optical data communication, and the relaxation oscillation (RO) frequency derived from the RIN spectrum shows an associated theoretical maximum modulation bandwidth of the device [12]. A lot of works are devoted to RIN analysis. For instance, the effect of the number of quantum wells as well as associated differential gain, etc. on the RIN of multiple-quantum-well (MQW) lasers has been investigated [13], and a much lower peak value of RIN below -157dB/Hz has been reported for MQW lasers [14]. Although many efforts were made on the study of intrinsic frequency response of MQW lasers, there is no detailed study of such dynamics or experimental report in the new-developed silicon hybrid lasers.

In the hybrid laser, two waveguides are put together closely: one is the III-V region which provides the gain, and the other is the SOI region which transmits light to subsequent devices in the platform. Therefore, its cavity mode profile has to be described in two-dimension transverse plane. As far as we know, the waveguide dimension can strongly influence the coupled mode profile in hybrid lasers. This hybrid mode characteristic is different from that in conventional MQW lasers. Since it is reported that the mode distribution has a great influence on the RIN of a laser in MQW lasers [15], a hybrid laser is predicted to have a different RIN characteristic from the conventional MQW laser. Therefore, a study on RIN in hybrid lasers including two-dimension profiles is necessary.

In this manuscript, we extend the RIN calculation model by incorporating two-dimension transverse profiles and investigate on the RIN of a hybrid laser, for the first time, to theoretically show its intrinsic frequency response. The manuscript is organized as follows: in section II we simulate the optical mode in our considered cavity of hybrid lasers. And then, in section III, we present a theoretical model for the RIN analysis by considering two-dimension transverse modes. In
section IV, both steady state and small signal modulation scenarios are analyzed. In section V, the RIN spectra of hybrid lasers are compared in terms of different dimensions e.g., III-V ridge widths and Si ridge heights. The comparison between a hybrid laser and a MQW laser is also discussed. Finally, we summarize the result.

II. TRANSVERSE MODE IN HYBRID LASER

Silicon hybrid laser is a coupled waveguide structure, which comprises vertically a top active III-V waveguide providing the optical gain, and an underneath passive SOI waveguide transmitting light to other components on SOI. The SOI waveguide consists of Si ridge, buried oxide (BOX) layer and Si substrate. BOX thickness is fixed at 2 μm to prevent the coupling of light into Si substrate. When the III-V and SOI waveguides are designed to be evanescently coupled with homogenous width, a higher confinement in SOI will lead to a higher threshold current density due to a lower confinement in III-V active region. Although taper design can be used to improve the threshold performance [16], it is beyond the scope of this manuscript and only evanescent coupling is considered in our computation.

Typical TE\(_{00}\) mode and TE\(_{10}\) even supermode [17] are shown in Fig. 1 with a relatively large confinement in active region. The III-V material structure consists of an InAlGaAs-based MQW sandwiched by asymmetric InP cladding layers to couple more light into SOI waveguide, with reference to [5]. It is found that the TE\(_{10}\) mode has a larger confinement in active region than that of the TE\(_{00}\) mode due to no lateral carrier confinement in the III-V ridge. In the following model, we will investigate the effects of these two modes on the RIN. We assume uniform current injection over the entire III-V ridge without injection carrier confinement within the ridge. Current leakage from sidewalls is also ignored as the optical profile is independent on it. In addition, under some certain dimensions, TE\(_{10}\) mode will be excited first due to larger confinement in active region and moderate mode loss as compared to TE\(_{00}\) mode. To avoid this, the confinement in active region for the TE\(_{00}\) mode is maintained above 6% by controlling the hybrid laser structure in our calculation to ensure that the TE\(_{00}\) mode will be excited first. It is noted that the TE\(_{10}\) mode cannot be coupled into SOI, thus could not transmit into subsequent devices in the circuit. In the below discussion, we only focus on the RIN of the TE\(_{00}\) mode.

![Fig. 1. The optical field distributions of the TE\(_{00}\) (a) and TE\(_{10}\) (b) mode of a hybrid laser with a 4μm-wide III-V ridge, a 1μm-wide and 500 nm-high Si ridge with arrows indicating the silicon-on-insulator (SOI) structure. BOX in (b) refers to buried oxide.](image)

III. TWO-DIMENSION SPATIAL-TEMPORAL MODEL

The model extended in this manuscript includes both spatial dependence of the carrier and the optical field profile, hence the electric field can be expressed as

\[
E(x, y, t) = \frac{1}{2} \sum \Phi_i(x, y) E_i(t) e^{-i\omega t} + cc. \tag{1}
\]

where \(E_i(x, y), \psi_i(x, y)\) and \(\omega_i\) are the complex field amplitude, optical field profile, and angular velocity of the \(i\)th transverse mode, respectively, and cc. refers to the complex conjugate of the first term. In this manuscript, we consider DFB silicon hybrid laser at 1.55μm with a normal ridge-air facet. Only up to the first two transverse modes are excited and \(\psi_i(x, y)\) is obtained from two-dimension simulations.

The time evolution of the carrier distribution within III-V ridge can be expressed as [15]

\[
\frac{\delta N_i(x, y, t)}{\delta t} = D_s \nabla^2 N_i(x, y, t) - \frac{N_i(x, y, t)}{\tau_n} \tag{2}
\]

\[
+ \frac{j}{ed} \int \int \psi_i^* \psi_j \gamma_i(x, y) g_j(t) P_j(t) \tag{2}
\]

where \(N_i(x, y), D_s, \tau_n, \psi_i, j, d, g, P_j\) are carrier density profile associated with \(i\)th mode, electron diffusion constant, electron lifetime, group velocity, \(i\)th mode confinement factor in active region, injection current density, total quantum wells thickness (including barriers), \(j\)th mode gain and the number of photons in \(j\)th mode, respectively.

\[\overline{\psi_j(x, y)^2}\] is the \(j\)th mode average optical profile and can be written as

\[
\overline{\psi_j(x, y)^2} = \int_0^{L_1} \int_0^{L_2} \psi_j^2(x, y) dx dy \tag{3}
\]

where \(L_1, L_2\) are III-V ridge height and width, respectively. The rate equation for the photon number can be expressed as

\[
\frac{dP_i(t)}{dt} = \left[ \psi_i^2 \gamma_i \xi_i(t) \right] \tag{4}
\]

\[
- \frac{1}{\tau_p} P_i(t) \frac{1}{\tau_s} \int \int N_i(x, y, t) dx dy \tag{4}
\]

where \(\tau_p, \gamma_i\) are \(i\)th mode photon lifetime, and spontaneous emission factor, respectively. The last term in (4) represents the noise component and \(\xi_i(t)\) is a real Gaussian noise term of zero mean, whose time correlation is given as

\[
< \xi_i(t) \xi_j(s) >= 2D_e \delta(t - s) \tag{15}
\]

In addition, there is a relationship between the carrier density and the gain as

\[
\frac{1}{A} \int_0^{L_1} \int_0^{L_2} \psi_j^2(x, y) A[N_i(x, y, t) - N_0] dx dy \tag{5}
\]

where \(A\) is the differential gain and \(N_0\) is transparent carrier density. Here we assume the laser is operated under normal condition where there is no gain saturation.
IV. Steady State and Small Signal Analysis

For intensity noise investigation, the above rate equations could be expanded around the steady state values for small signal analysis. Using the boundary condition that 
\[ N(0, y) = N(L_0, y) = N(x, 0) = N(x, L_0) = 0, \]
the steady state carrier density \( N(x, y) \) can be solved by setting (2) and (4) to be equal to zero as

\[
N(x, y) = \sum_{m=1}^{\infty} \sum_{n=1}^{\infty} \int_0^{L_0} \int_0^{L_0} \sin \left( \frac{m \pi}{L_x} x \right) \sin \left( \frac{n \pi}{L_y} y \right) \frac{v_x}{d} d \psi_j(x, y) g_{oj} dxdy
\]

where \( g_{oj} \) is \( j \)th mode steady state gain and can be solved from the steady state of (4) (ignore second term which is very close to zero and noise average is zero) that

\[
g_{oj} = \frac{1}{v_x \tau_{r,j}}
\]

Then (6) and (7) are substituted into (5) thus \( i \)th mode power could be solved. For the TE00 mode,

\[
a_1 \overline{P}_1 = b_1
\]

where \( a_1, b_1 \) are expressed as

\[
a_1 = 4 \sum_{m=1}^{\infty} \sum_{n=1}^{\infty} \int_0^{L_0} \int_0^{L_0} \frac{\sin \left( \frac{m \pi}{L_x} x \right) \sin \left( \frac{n \pi}{L_y} y \right)}{\psi_j(x, y)} d \psi_j(x, y) dxdy
\]

\[
\times \int_0^{L_0} \int_0^{L_0} \frac{\sin \left( \frac{m \pi}{L_x} x \right) \sin \left( \frac{n \pi}{L_y} y \right)}{L_x} \left[ \frac{m \pi}{L_x} \right] - \left[ \frac{n \pi}{L_y} \right] \frac{1}{D_{r_a}}
\]

\[
b_1 = \frac{\psi_j(x, y)^2}{v_x \tau_{r,j}} + AN_j \int_0^{L_0} \int_0^{L_0} \psi_j(x, y) dxdy
\]

\[
-16A \sum_{m=1}^{\infty} \sum_{n=1}^{\infty} \int_0^{L_0} \int_0^{L_0} \frac{\sin \left( \frac{m \pi}{L_x} x \right) \sin \left( \frac{n \pi}{L_y} y \right)}{L_x} \left[ \frac{m \pi}{L_x} \right] - \left[ \frac{n \pi}{L_y} \right] \frac{1}{D_{r_a}}
\]

If both TE00 and TE10 modes exist simultaneously, then we have

\[
a_{11} \overline{P}_1 + a_{12} \overline{P}_2 = b_1
\]

\[
a_{21} \overline{P}_1 + a_{22} \overline{P}_2 = b_2
\]

where \( a_{ij}, b_j \) are (i=1,2; j=1,2)

In the above equations, \( m \) and \( n \) are odd numbers for b1 and b2, respectively.

The typical L-I curves of a hybrid laser are shown in Fig. 2, where L-I curves in III-V waveguide are also given (see Fig. 2b). Since TE10 mode cannot be coupled into SOI waveguide, we only have interests in TE00 mode for a hybrid laser. Although the TE10 mode is not coupled into the SOI waveguide, it will affect the RIN characteristics of the TE00 mode once it is excited. Noted that the calculated power, in linear regime, of the TE00 mode coupled into SOI waveguide and the threshold current density are slightly higher than experimental values reported in [7]. The small discrepancy is caused by uncertainties in the parameters chosen for calculations. In addition, there is a kink in the calculated L-I curve of the TE00 mode due to the existence of mode competition when the TE10 mode is excited.

For small signal analysis, time dependent terms are expanded around steady state values as

![Fig. 2. The LI curves for a silicon hybrid laser (a) The LI curves in SOI waveguide where TE10 mode will not be coupled. (b) The LI curves in III-V waveguide where TE00 mode is excited first. The typical parameters used are: \( L_0=2.196\mu m, \ D=1\text{cm/s}, \ A=3.4 \times 10^{-10}\text{cm}^2, \ N_p=8\times10^{19}\text{cm}^{-3}, \ \nu_p=0.75\times10^{10}\text{cm/s}, \ \tau_{p,1}=2\text{ns}, \ \tau_{p,2}=2.7\text{ps}, \ \tau_{p,2}=2.5\text{ps}, \ \beta=2\times10^4 \text{taken from [13, 15]}.]
\[ P(t) = \overline{P} + \Delta P(t) \]  
\[ N_i(x, y, t) = N_i^0(x, y) + \delta N_i(x, y, t) \]  
\[ \Delta g_i(t) = A_{ij}^{\text{lldf}} \int_0^t \delta N_j(x, y, t) \psi_i^2(x, y) \, dx \, dy / \psi_i(x, y)^2 \]  

Therefore when (10) is substituted into (2) and (4), we obtain (neglect the second order perturbation terms and the diffusion perturbation)

\[ \frac{\partial \delta N_i(x, y, t)}{\partial t} = -\delta N_i(x, y, t) \]  
\[ - \sum_j \frac{v_j \tau_j}{d \psi_j(x, y)} \psi_j^2(x, y) \left( \Delta g_j \overline{P} + g_{ij} \Delta P \right) \]  
\[ \frac{d \Delta P(t)}{dt} = v_e \tau_e \frac{\Delta g_i(t) \overline{P}}{\tau_n} + \frac{\sqrt{\overline{P} P_0} \delta}{\tau_n} \int_0^t \int_0^t \delta N(x, y, t) \psi_i^2(x, y) \, dx \, dy / \psi_i(x, y)^2 \]  

If both sides of (11) are multiplied by \( A_{ij}^{\text{lldf}} \psi_i^2(x, y) / \psi_j^2(x, y)^2 \) and integrated over the entire III–V ridge, we obtain

\[ \frac{d \Delta g_i(t)}{dt} = -\frac{\Delta g_i(t)}{\tau_n} - \sum_j \frac{A_{ij}^{\text{lldf}} \psi_i^2(x, y)}{d \psi_j(x, y)} - \frac{A_{ij}^{\text{lldf}} \psi_i^2(x, y)}{d \psi_j(x, y)} \]  
\[ \times \left( \Delta g_j \overline{P} + g_{ij} \Delta P \right) \int_0^t \int_0^t \delta N(x, y, t) \psi_i^2(x, y) \, dx \, dy / \psi_i(x, y)^2 \]  

Similarly, for the TE\(_{00}\) mode,

\[ \frac{d \Delta P_i(t)}{dt} = c_1 \Delta g_1(t) + d_1 \xi_1(t) \]  
\[ \frac{d \Delta g_1(t)}{dt} = e_1 \Delta g_1(t) + f_1 \Delta P_1(t) \]  

where

\[ c_1 = v_e \tau_e \overline{P}, \quad d_1 = \frac{\sqrt{\overline{P} P_0} \delta}{\tau_n} \int_0^t \int_0^t \delta N(x, y, t) \psi_1^2(x, y) \, dx \, dy / \overline{P} \]  
\[ e_1 = -\frac{A_{11}^{\text{lldf}} \psi_1^2(x, y)}{\tau_n} - \frac{A_{11}^{\text{lldf}} \psi_1^2(x, y)}{d \psi_1(x, y)^2} \]  
\[ f_1 = -\frac{A_{11}^{\text{lldf}} g_0 \psi_1^2(x, y)}{d \psi_1(x, y)^2} \]  

If both TE\(_{00}\) and TE\(_{10}\) modes exist simultaneously, we obtain

\[ \frac{d \Delta P_1(t)}{dt} = c_2 \Delta g_2(t) + d_2 \xi_2(t) \]  
\[ \frac{d \Delta g_2(t)}{dt} = e_2 \Delta g_2(t) + f_2 \Delta P_2(t) \]  

where

\[ c_2 = v_e \tau_e \overline{P}, \quad d_2 = \frac{\sqrt{\overline{P} P_0} \delta}{\tau_n} \int_0^t \int_0^t \delta N(x, y, t) \psi_2^2(x, y) \, dx \, dy / \overline{P} \]  
\[ e_2 = -\frac{A_{22}^{\text{lldf}} \psi_2^2(x, y)}{\tau_n} - \frac{A_{22}^{\text{lldf}} \psi_2^2(x, y)}{d \psi_2(x, y)^2} \]  
\[ f_2 = -\frac{A_{22}^{\text{lldf}} g_0 \psi_2^2(x, y)}{d \psi_2(x, y)^2} \]  

where \( \delta \) is the Kronecker delta function.

Therefore, by solving (14) or (15), the RIN spectra could be obtained.

V. RESULTS AND DISCUSSION

Once (14) and (15) are transformed into the frequency domain, \( \Delta P(\omega) \) and \( \Delta B(\omega) \) could be solved (the perturbation of diffusion is ignored). As defined in [18], RIN for the TE\(_{00}\) mode of a hybrid laser, is defined as

\[ RIN = 2 \left( \frac{\left| \Delta P(\omega) \right|^2}{\left| \overline{P} \right|^2} \right) \]  

where \( < > \) refers to the mean values. For all calculations, Si ridge width is fixed at 1 \( \mu \)m.

Figure 3 shows the RIN spectra of a hybrid laser at different injection currents, where the III–V ridge width is 3 \( \mu \)m and the height of Si ridge is 220 \( \mu \)m. At 1.051 \( \mu \)m, where \( \mu \)m is the threshold current density, the laser only operates at the TE\(_{00}\) mode, while, under 1.41 \( \mu \)m and 1.89 \( \mu \)m, TE\(_{10}\) mode is excited. The frequency at peak of RIN spectrum corresponds to RO frequency, which is related to the theoretical largest modulation bandwidth [12]. At 1.051 \( \mu \)m, the hybrid laser oscillates only at one RO frequency; but as two modes are excited, two RO frequencies appear, as shown in Fig. 3. Moreover, with the increase of the current, the RO frequency becomes blueshifted and the peak value of RIN decreases.

Fig. 3. The RIN spectra for hybrid laser with a 3 \( \mu \)m III–V ridge width, 220 \( \mu \)m Si ridge height under different injection current density: (a) Injection current density is 1.051 \( \mu \)m; (b) Injection current density is 1.41 \( \mu \)m; (c) Injection current density is 1.89 \( \mu \)m.
is blueshifted and the peak value of RIN decreases. Moreover, one of the peaks is gradually suppressed. It could be attributed to the variation of cavity mode profile in the hybrid laser. As shown in Fig. 1, a part of TE_{00} mode excited in the III-V waveguide couples into the SOI and the maximum intensity in III-V waveguide is located at the center of ridge. However, for the TE_{10} mode, the confinement in SOI is very small and the maximum intensity in III-V is located away from the center of ridge. Therefore, the overlap of cavity modes TE_{00} and TE_{10} is low so as to induce a low RIN at low frequency range. As Si ridge height increases, confinement of TE_{00} mode in SOI is even higher and the mode overlap of the TE_{00} and TE_{10} modes is further reduced. Therefore, the first peak at low frequency range is further suppressed. An optimum value. In addition, the first peak of the RIN spectrum is gradually suppressed as the III-V ridge width increases due to the lower and lower overlap of the TE_{00} and TE_{10} modes.

We will close our analysis by comparing the RIN spectrum of a hybrid laser with that of a conventional MQW laser with same epitaxial structures, as shown in Fig. 6. The III-V ridge widths for both lasers are 4μm and Si ridge in the hybrid laser is 340 nm high. When only TE_{00} mode is excited at 1.05J_{th}, the RIN spectrum of the hybrid laser shows a larger peak value and a lower RO frequency than those of the MQW laser, which is due to the lower confinement in active regions in hybrid laser [19]. In contrast, when both TE_{00} and TE_{10} modes are excited,

The III-V ridge dimension design can also influence the mode distributions in hybrid lasers hence the RIN, as shown in Fig. 5. As the III-V ridge width increases, if only TE_{00} mode is excited, the RO frequency is redshifted and the peak value of RIN increases. However, when both TE_{00} and TE_{10} modes are excited, the RO frequency is firstly blueshifted then redshifted and the peak value firstly decreases then increases. It shows us that, in our calculation, a 4μm width design has the highest RO frequency and the minimum peak value of RIN. This indicates a theoretically optimum III-V ridge width for the maximum modulation bandwidth and the lowest RIN with fixed 340nm Si ridge height. It is noted that for a fixed Si ridge height of 220nm, the RIN shows the same characteristic by changing the III-V ridge widths. These characteristics could be attributed to the ratio of confinement in active region to ridge area (ridge width × cavity length). It is experimentally found that it is not the confinement in quantum wells for conventional MQW lasers but the ratio of confinement to ridge area [13] which determines the RO frequency: the larger the ratio, the higher the frequency. In our calculations, as the III-V ridge width increases, the ratio first increases then decreases; therefore, the peak of RIN shows

![Fig. 4. The RIN spectra for hybrid laser with the same 3μm III-V width, different SOI height under two injection current density levels: (a) Injection current density is 1.05J_{th}, Si ridge height 220nm; (b) Injection current density is 1.4J_{th}, Si ridge height 220nm; (c) Injection current density is 1.05J_{th}, Si ridge height 340nm; (d) Injection current density is 1.4J_{th}, Si ridge height 340nm; (e) Injection current density is 1.05J_{th}, Si ridge height 500nm; (f) Injection current density is 1.4J_{th}, Si ridge height 500nm.](image)

![Fig. 5. The RIN spectra for hybrid laser with same SOI height 340nm, different III-V width under two injection current density levels: (a) Injection current density is 1.05J_{th}, 3μm III-V width; (b) Injection current density is 1.4J_{th}, 3μm III-V width; (c) Injection current density is 1.05J_{th}, 4μm III-V width; (d) Injection current density is 1.4J_{th}, 4μm III-V width; (e) Injection current density is 1.05J_{th}, 5μm III-V width; (f) Injection current density is 1.4J_{th}, 5μm III-V width; (g) Injection current density is 1.05J_{th}, 6μm III-V width; (h) Injection current density is 1.4J_{th}, 6μm III-V width.](image)

![Fig. 6. Comparison of the RIN spectra for a hybrid laser (a) (c) (e) and diode laser (b) (d) (f) with same ridge width of 4μm, under different injection current densities: Injection current density is 1.05J_{th} (first row); Injection current density is 1.4J_{th} (second row); Injection current density is 1.8J_{th} (third row).](image)
modes is very small in the hybrid laser. Furthermore, the second RO frequency of the MQW laser is lower than that of the hybrid laser. Our simulation result, as shown in Fig. 6(b), on the RIN for conventional MQW lasers can match well with the experimental values [20]. In addition, the simulated modulation bandwidth derived from the RIN spectrum of hybrid lasers is also comparable to the experimental modulation bandwidth [21]. The small discrepancy can be attributed to the gain saturation effect [18], which is not considered in this simulation for the sake of simplification. These results indirectly verify the model we proposed.

In terms of application of a laser system, noise floor level is also very important. Laser intensity noise, as one of the major noise sources, limits the application for high speed modulation system. When silicon hybrid laser is operated with high injection currents, our simulation results show that the noise level is close to the standard quantum limit which is \( 2\hbar / P_0 = -170.68 \text{dB/Hz} \) (with an output power of 30mW). In addition, our calculation shows that hybrid lasers have a similar noise level compared with conventional diode lasers. This result indicates that silicon hybrid laser is suitable as a source for high fidelity optical transmission.

VI. CONCLUSION

In this work, we theoretically investigate the RIN spectra of hybrid lasers considering the two-dimension transverse mode profiles. It shows that when only one transverse mode is excited, the RIN spectrum of the hybrid laser shows a larger peak value at RO frequency but a lower RO frequency than those of the MQW laser with the same ridge width. When two transverse modes are excited, the laser system shows two RO frequencies. In this case, the hybrid laser shows a lower peak value at RO frequency and a higher RO frequency than those of the MQW laser. The effects of Si ridge heights and III-V ridge widths on the RIN are also studied in details. Specifically, as Si ridge height increases, when only TE\(_{00}\) mode is excited, the RO frequency is red-shifted and the peak value of RIN increases; however, when both TE\(_{00}\) and TE\(_{01}\) modes are excited, RO frequencies are blue-shifted and the peak value of RIN decreases. In addition, as the III-V ridge width increases, when only TE\(_{00}\) mode is excited, the RO frequency is red-shifted and the peak value of RIN increases; however, when both TE\(_{00}\) and TE\(_{01}\) modes are excited, the RO frequency is firstly blue-shifted then red-shifted and the peak value first decreases then increases. The investigations on the RIN spectra of the hybrid laser show an associated theoretical maximum modulation bandwidth of the device.

The presented model can well reflect the noise characteristics of hybrid lasers to some extent and enable a fast prediction and optimization of device performance. However, there are still certain aspects that the model can be further improved. The most important issues, which should be taken into account for more accurate calculations, are to include gain saturation and heat effect. The lack of gain saturation will overestimate the RO frequency, and lack of heat effect will assume constant structure parameters and underestimate the noise floor level. This requires a further investigation.

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