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1 **Analysis of Geosynthetic Tubes Inflated by Liquid and** 2 **Consolidated Soil**

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11

12 **Abstract**

13 When permeable geosynthetic tubes are used for dewatering of waste sludge or construction
14 of dikes or embankments, the tubes have to be inflated using sludge or soil slurry several
15 times. After each inflation, the soil slurry is consolidated into solid. Hence from the second
16 inflation onwards, the geosynthetic tube is filled by both slurry and consolidated soil. In this
17 paper, a new analytical method is proposed to provide a solution to the above specific case.
18 Friction between geosynthetic sheet and soil, and friction between geosynthetic tube and
19 subgrade, are considered. Parametric studies are also carried out to compare the design
20 between geosynthetic tubes inflated using pure slurry and that using slurry and consolidated
21 soil to study the key factors affecting the design. The study shows that tensile forces vary
22 along the cross-section of the geosynthetic tube with the minimum value occurring at the
23 center of the base. The effect of friction and lateral earth pressure on the geometry and tensile
24 forces of the geosynthetic tube is insignificant when the height of the consolidated soil in the
25 tube is small, but increases considerably with an increase in the height.

26
27 **Keywords:** Geotextile Tube; Geosynthetic Tube; Consolidated Soil.

1 1 Introduction

2 Geosynthetic tubes have been widely used in breakwaters and beach restoration projects in
3 recent years (Leshchinsky et al., 1996; Shin and Oh, 2007; Lawson, 2008; Cantré and
4 Saathoff, 2011; Yan and Chu, 2010; Chu et al., 2012; Yee et al., 2012; Yee and Lawson,
5 2012; Lee and Douglas, 2012). These tubes are made of geosynthetic materials and inflated
6 with water, clay slurry or sand. Compared with traditional ways of constructing shoreline
7 structures using rock or precast concrete units, the use of geosynthetic tubes offers several
8 advantages. First, it is cost-effective. The use of a layer of geosynthetic sheet with soil to
9 form a tube is often more economical than the use of concrete or rocks. Second, the
10 construction process can be made simpler and faster. Third, local soils can be used as filling
11 materials. If sand is not readily available, silty clay or clay slurry can be used as well (Yan
12 and Chu, 2010; Chu et al., 2012; Yee et al., 2012; Yee and Lawson, 2012). Geosynthetic
13 tubes are also used to dewater waste sludge such as digested bio-solids, sewage sludge,
14 dredged materials (Moo-Young and Tucker, 2002), industrial solid wastes (Worley et al.,
15 2008), fly ash (Muthukumaran and Ilamparuthi, 2006) and coal slurry.

16
17 When permeable geosynthetics are used to form geosynthetic tubes, the geosynthetic sheet
18 will act as a filtering medium. The sand or clay slurry is firstly pumped into the geosynthetic
19 tube as shown in Figure 1(a). Then under the self-weight of the fill material and the confining
20 stress provided by the geosynthetic sheet, water seeps through the permeable geosynthetic
21 sheet and the solids are kept inside the tube, see Figure 1(b). The total volume of the filling
22 material inside the geosynthetic tube reduces considerably. To increase the volume of the
23 solids inside the tube, the geosynthetic tube has to be refilled several times. From the second
24 round of filling onwards as shown in Figure 1(c), the fill materials inside the tube become
25 two parts: the newly pumped slurry and the consolidated soil left from the first pumping.

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The analysis of geosynthetic tubes inflated by both slurry and consolidated soil is normally carried out using solutions for the analysis of geosynthetic tubes inflated with liquid or slurry. This is because most of the theoretical solutions available are for this type (Leshchinsky et al., 1996; Plaut and Suherman, 1998; Cantré and Saathoff, 2011; Yan and Chu, 2010; Chu et al., 2011; Guo et al, 2011; Malik and Sysala, 2011), except one solution provided by Plaut and Stephens (2012). However, the consolidated soils in the Plaut and Stephens’s (2012) solution are still simulated as a liquid with a different density and a unit earth pressure coefficient at rest which may not be suitable for the case when the water content of the consolidated soils is relatively low.

In this paper, a new analytical method is proposed to analyze the permeable geosynthetic tubes inflated by slurry and consolidated soil at the time when the tube is just fully inflated. At this state (see Figure 1(c)), the fill materials in the geosynthetic tube consist of newly inflated slurry and the consolidated soil left from the previous step. The actions from the consolidated soils onto the geosynthetic tube are separated into effective earth pressure and pores water pressure. The properties of water in pore are the same as liquid. The force components from the effective earth pressure of the consolidated soil are separated along the lateral and vertical directions. The effects of the two force components to the geosynthetic tube depend on their relative force directions on the selected infinitesimal calculation element. The friction between the geosynthetic sheet and the fill materials and that between geosynthetic tube and subgrade are also considered in the method. A computer program was developed to solve the differential equations. The solution is applicable to analyze the permeable geosynthetic tube when it is just fully inflated by the new pumped slurry and consolidated soil left from the previous pumping.

1

2 2 Derivation

3 2.1 Basic assumptions

4 In deriving the solutions, the following assumptions need to be made: 1) the geosynthetic
5 tube is sufficiently long to be assumed as a plane strain problem; 2) the geosynthetic shell is
6 thin and its weight can be neglected; 3) the extension of the geosynthetic sheet is negligible;
7 4) the friction between geosynthetic and consolidated soil or that between geosynthetic and
8 subgrade is sliding friction; 5) the top of the consolidated soil is horizontal; and 6) the water
9 content or unit weight of the consolidated soil are constant during filling. Some of the above
10 hypotheses are also made in the existing solutions for slurry inflated geosynthetic tubes
11 (Szyszkowski and Glockner, 1987; Kazimierowicz, 1994; Plaut and Suherman, 1998; Cantré,
12 2002; Ghavanloo and Daneshmand, 2009; Cantré and Saathoff, 2011; Malik and Sysala, 2011;
13 Chu et al, 2011; Guo et al, 2011; Plaut and Stephens, 2012; Guo et al., 2013).

14

15 2.2 Theoretical Derivations

16 A simplified cross-section of a geosynthetic tube inflated by new slurry and consolidated soil
17 is shown in Figure 2(a). The coordinates system is set-up with x in the horizontal direction
18 and y in the vertical direction. The origin of this coordinate is taken as the center of the
19 contact edge with the rigid subgrade. The unit weight of the slurry is written as γ_L . The
20 effective unit weight of the consolidated soil is denoted as γ_s' and $\gamma_s' = \gamma_s - \gamma_w$, where γ_s and γ_w
21 are the unit weight of consolidated soil and water, respectively. The height of the
22 consolidated soil is denoted as H_s . The height and width of the cross-section of the
23 geosynthetic tube are written as H and B , respectively. The contact width between the tube
24 and the subgrade is b . An infinitesimal small curve with a length of ds around an arbitrary
25 point $S(x, y)$ can be treated as an arc with the center at point C and radius of r as shown in

1 Figure 2(b). The angle between the tangential direction at point $S(x, y)$ and the x axis is
 2 denoted as θ . Then two geometrical equations relating the angle between the tangential
 3 direction along cross section and the x and y coordinates can be written as Equations (1) and
 4 (2). For $x < b/2$, the contact part with the rigid subgrade is a straight line. Therefore, the
 5 calculation for the curvature is starting from $x = b/2$.

6

$$\frac{dy}{ds} = \sin \theta \quad (1)$$

$$\frac{dx}{ds} = \cos \theta \quad (2)$$

7

8 For the points below the surface of consolidated soils such as point $S(x, y)$ in Figure 2(a), two
 9 cases have to be considered separately based on the different position of point $S(x, y)$. The
 10 first case is when the angle between the tangent line on point $S(x, y)$ and the x -axis, θ , is less
 11 than $\pi/2$ as shown in Figure 2(a). The vertical effective earth pressure from the solid layer
 12 above point $S(x, y)$ is acting on it. The range of action could be mathematically expressed as y
 13 $< y_{slice} < y_D$ and $x-dx/2 < x_{slice} < x+dx/2$ where y_D is the calculation variable which is equal to
 14 the minimum value of H_s and the y -coordinate of the point that has the same x -coordinate
 15 with $S(x, y)$. The second case is when the angle between the tangent line on point $S(x, y)$ and
 16 the x -axis, θ , is greater than $\pi/2$, where the effective stress is not acting on it. In order to
 17 combine the two cases together, the total force from the vertical earth pressure acting
 18 internally on point $S(x, y)$ can be mathematically written as $\alpha \gamma_s (y_D - y) \cos \theta ds$, where $\alpha = 1$
 19 when $\theta < \pi/2$ and $\alpha = 0$ when $\theta > \pi/2$. Then the components due to the vertical effective earth
 20 pressure acting at point $S(x, y)$ in the normal and tangential directions are expressed as
 21 $\alpha \gamma_s (y_D - y) \cos^2 \theta ds$ and $\alpha \gamma_s (y_D - y) \cos \theta \sin \theta ds$, respectively. The total force due to the lateral
 22 effective earth pressure can be calculated as $k \gamma_s (H_s - y) \sin \theta ds$ where k is the coefficient of

1 lateral earth pressure. The force components due to the lateral earth pressure that act on the
2 point $S(x, y)$ in normal and tangential direction can be calculated as $k\gamma'_s(H_s-y)\sin^2\theta ds$ and
3 $k\gamma'_s(H_s-y)\sin\theta\cos\theta ds$, respectively. The friction, f , between filling solid layer and the
4 geosynthetic sheet is calculated by multiplying the net resultant force in the normal direction,
5 N , with the friction coefficient between solid filling material and geosynthetic sheet, μ_1 , i.e. f
6 $= \mu_1 N$ and $N = (k\gamma'_s(H_s-y)\sin^2\theta + \gamma'_s(y_D-y)\cos^2\theta)ds$. The direction of the friction force is the
7 same as the direction indicated in Figure 2(a) because the whole tube is inflated to a sausage
8 shaped cross-section and the solids are pulled up. It should be pointed out that there is no
9 contact friction if there is no relative movement between the subgrade and the geosynthetic
10 tube skin because the geotextile sheet is assumed to be inelastic. The method of using the
11 friction coefficient multiplied by the normal stress acting on the point is a simplified
12 approach. In the real case, it is possible to have relative movement between the geosynthetic
13 tube and subgrade because of the extension of the geosynthetic material. The total force due
14 to the hydraulic pressure acting at point $S(x, y)$ is written as $(p_0 + \gamma_L(H - H_s) + \gamma_w(H_s - y))ds$ where
15 p_0 is the pumping pressure on top of the geosynthetic tube. The tensile force along the cross-
16 section is denoted as T . The tensile force additional along the differential direction is written
17 as dT . Based on the free-body diagram of the infinitesimal element shown in Figure 2(b),
18 equilibriums of the forces along the normal and tangential directions yields the following
19 equations:

20

$$\frac{dT}{ds} = (\alpha(y_D - y) - k(H_s - y))\gamma'_s \sin \theta \cos \theta + \mu_1 N \quad (3)$$

$$\frac{d\theta}{ds} = \frac{1}{T} [N + p_0 + \gamma_L(H - H_s) + \gamma_w(H_s - y)] \quad (4)$$

where $N = \gamma'_s(k(H_s - y)\sin^2\theta + \alpha(y_D - y)\cos^2\theta)ds$ (5)

21

1 For the point above the surface of consolidated soils such as point $S(x, y)$ in Figure 3(a), the
 2 calculation procedure is the same as that used for liquid inflated geosynthetic tubes. A free
 3 body diagram of the infinitesimal calculation element at point $S(x, y)$ is shown in Figure 3(b).
 4 The hydraulic pressure acting internally on the tube at a given depth is written as $p_0 + \gamma_L (H -$
 5 $y)$. The tension force along the cross-section is constant because the friction between filling
 6 slurry and geosynthetic tube can be neglected. Based on the force equilibrium equations in
 7 the normal and tangential directions along the infinitesimal element, the following equations
 8 can be obtained:

$$\frac{dT}{ds} = 0 \quad (6)$$

$$\frac{d\theta}{ds} = \frac{1}{T} (p_0 + \gamma_L (H - y)) \quad (7)$$

10

11 2.3 Boundary Conditions

12 In order to solve the differential equations, one more boundary condition related to the tensile
 13 force has to be established. A free body diagram of the half cross-section is presented in
 14 Figure 4 where T_{top} and T_{bottom} are denoted as the tensile forces on top (point M) and bottom
 15 middle point (point N), respectively. Because the cross-section is symmetric and the tensile
 16 forces are along its tangential directions, the direction of T_{top} and T_{bottom} must be horizontal as
 17 shown in Figure 4. The tensile force on the bottom, T_{Bottom} , has to be calculated from the
 18 tensile force on the point $(b/2, 0)$ by considering contact friction between the geosynthetic
 19 tube and the rigid subgrade. The decreasing rate of tensile force can be simplified as $dT/dx =$
 20 $-\mu_1 \gamma_s y_D - \mu_2 W/b$ where W is the total weight of the filling material. Thus $T_{Bottom} = T_{(b/2, 0)} +$
 21 $\int_{b/2}^x (\mu_1 \gamma_s y_D + \mu_2 W/b) dx$ where x ranges from $b/2$ to x_b and x_b is the x -coordinate along the
 22 rigid contact surface when $T_{Bottom} = 0$ (if $T_{Bottom} > 0$, $x_b = 0$). It should be pointed out that the

1 magnitude of y_D is from the calculated cross-section which is also an unknown variable. It
 2 will be further discussed in section 2.4 that a searching method (complex method) will be
 3 adapted to search for the target variables. Then for each searching loop, the y_D value is
 4 calculated from the cross-section of the previous loop. As the complex searching method
 5 narrows the range of the possible variables, the y_D value will become closer and closer to the
 6 real value. For the selected free body diagram in Figure 4, the forces acting along the
 7 horizontal direction involve the hydraulic pressure, the friction between the geosynthetic
 8 sheet and the ground ($\int_{b/2}^{xb}(\mu_2 W/b)dx$), and the tensile force in the geosynthetic sheet.
 9 Therefore, force equilibrium in the horizontal direction between these forces yields:

$$T_{Top} + T_{Bottom} = p_0 H + \frac{1}{2} \gamma_L (H^2 - H_s^2) + \frac{1}{2} (\gamma_w + k \gamma_s') H_s^2 + \mu_2 \frac{W}{b} (x_b - \frac{b}{2}) \quad (8)$$

11
 12 By combining Equations (1) to (8), the geometry and tensile force of the geosynthetic tube
 13 inflated by slurry and consolidated soil could be solved by a computer program. The unit
 14 weight of soil, γ_s , unit weight of liquid (or slurry), γ_L , unit weight of water, γ_w , the thickness
 15 of the solid layer, H_s , the coefficient of lateral earth pressure, k , and any two parameters from
 16 p_0 , L , H , are taken as inputs. The following two boundary conditions are adopted for the
 17 curved section: 1) when $y = 0$, $x = b/2$ and $\theta = 0$; and 2) when $y = H$, $x = 0$ and $\theta = \pi$.

18 19 *2.4 Iteration Method*

20 As there is no closed-form solution for the tensile force or cross-section of the geosynthetic
 21 tube from these differential equations, a computer program has been written to obtain a
 22 numerical solution using the adaptive Runge-Kutta-Merson method (RKM4). Programs for
 23 the RKM4 method had already been developed by Press et al. (2007), Xu (1995),
 24 Christiansen (1970) and Lukehart (1963). A mathematical programming scheme, the

1 Complex Method proposed by Box (1965), was used to search for the unknown parameters in
2 a specific range. Details of the calculation procedure are given in Lipson (1977) and Xu
3 (1995).

4

5 3 Parametric Studies

6 To better understand the influence of some major factors, parametric studies were carried out.
7 The input variables are the circumference of the cross-section (L) and pumping pressure (p_0).
8 The height of solid in the tube (H_s), the unit weight of consolidated soil (γ_s), unit weight of
9 the filling slurry (γ_L), the friction coefficient (μ) and the coefficient of lateral earth pressure (k)
10 are also taken as inputs. In order to avoid the influence of units, dimensionless parameters
11 were used in the analysis whenever possible. The normalization method adopted in this paper
12 was similar to that used by Plaut and Stephens (2012). The unit weights γ_L and γ_s were
13 divided by γ_w ; geometry parameters H_s , H , B and b were divided by L ; the area of the cross-
14 section was divided by L^2 ; pumping pressure was divided by $\gamma_w L$; and tensile force was
15 divided by $\gamma_w L^2$. In the calculation, the unit weight of the fill slurry was taken as 1.2 times
16 that of water, and the unit weight of the consolidated soil was 1.78 times that of water. The
17 water content of the soil was taken as 40% and its specific gravity was 2.61.

18

19 Some comparisons of analytical results between geosynthetic tubes fully inflated by liquid
20 and those inflated by liquid and consolidated soils are shown in Figure 5. Six different cases
21 were considered to illustrate the effects of normalized height of consolidated soil, coefficient
22 of lateral earth pressure and the friction coefficient. It should be noted that the lateral earth
23 pressure may vary from an active case to a positive case depending on the reaction between
24 geosynthetic tube and consolidated soil. It can be seen that the height of the geosynthetic tube
25 inflated using liquid and consolidated soils is lower than that using liquid only. This is

1 because of the influence from the soil heights and coefficient of lateral earth pressure. The
2 difference is up to 18.4% for the case with $p_0/\gamma_w L = 0.3$, $H_s/L = 0.2$, $k = 3.0$ and $\mu = 0.5$ as
3 shown in Figure 5(b). Therefore, design for geosynthetic tubes inflated using liquid and
4 consolidated soils using an analytical method for those using liquid alone will overestimate
5 the height of the geosynthetic tube.

6

7 As shown in Figure 5, the tensile force distribution along the cross-section of a geosynthetic
8 tube above the ground surface is uniform for a tube inflated with slurry alone. On the other
9 hand, the tensile force distribution varies along a tube inflated using both slurry and
10 consolidated soil with the maximum value occurring at the top of the tube, point D, and the
11 minimum value at point A which is the center point at the base. The tensile force increases
12 when the point moves from point A towards the boundary of the contact between the tube
13 and the ground at B (Figure 5). The change in the tensile forces from A to B is due to the
14 friction between the geosynthetic and the ground. For the tensile forces in section BC of the
15 geosynthetic tube that does not contact with the ground, the tensile force distributions are also
16 not uniform. Generally, the tensile force increases from point B towards C as shown in Figure
17 5 except for the case in Figure 5(b) because of the larger coefficient of lateral earth pressure
18 ($k = 3.0$). Since the center point A has the smallest tensile force, it will be an ideal position to
19 put the joint of the geosynthetic tube as the seam strength is usually lower than the
20 geosynthetic itself (Gughelmetti et al. 1996; TenCateTM, 2010; Guo 2012).

21

22 The relationships between the normalized pumping pressure and the normalized height of the
23 geosynthetic tube are plotted in Figure 6 for different fills and friction conditions. The height
24 of the tube is affected by the height of the consolidated soils, among other factors. The higher
25 the height of the normalized consolidated soils, H_s/L , the lower the normalized height of the

1 geosynthetic tube for a given normalized pumping pressure, $p_0/\gamma_w L$. The highest normalized
2 height of the cross-section, H/L , occurs when the tube is filled by liquid only. This is
3 consistent with the observation made in Figure 5. When $H_s/L = 0.0$, i.e. no solids are in the
4 tube, the friction components have no influence on the height of the cross-section. This is
5 because the friction is transmitted through the solids. When the height of the consolidated
6 soils increases, the effect of the coefficient of lateral earth pressure becomes significant. Take
7 the case when $H_s/L = 0.2$, $p_0/\gamma_w L = 0.02$, $\mu = 0.5$ in Figure 6, for example: H/L decreases by
8 22.3% from 0.148 to 0.115 when k varies from 0.65 to 3.0. Figure 7 shows the relationship
9 between the pumping pressure and the normalized area of the cross-section, A/L^2 , for
10 different p_0 , μ , k and H_s/L values. It is shown again that the normalized area of the cross-
11 section will reduce when the height of the consolidated soils increases.

12

13 Figure 8 depicts the effect of $p_0/\gamma_w L$, μ , k and H_s/L on the relationships between the
14 normalized width of the cross-section, B/L , and the normalized pumping pressure, $p_0/\gamma_w L$. It
15 can be seen that B/L decreases with increasing $p_0/\gamma_w L$. The value of B/L is the smallest when
16 the fill is only slurry. With the increase in the height of the consolidated soils, B/L increases
17 to 0.39 for $H_s/L = 0.2$, $k = 3.0$, $\mu = 0.5$ and $p_0/\gamma_w L = 0.3$ or an increase of 10% compared with
18 the case $H_s/L = 0$. This amount of difference needs to be considered when both slurry and
19 consolidated soils are used to fill geosynthetic tubes. The effects of $p_0/\gamma_w L$, μ , k and H_s/L on
20 the relationship between the normalized contact width with the ground, b/L , and the
21 normalized pumping pressure, $p_0/\gamma_w L$, are shown in Figure 9. Similar observations as for B/L
22 presented in Figure 8 can be made.

23

24 The normalized pumping pressure versus the normalized maximum tensile force $T_{max}/\gamma_w L^2$ is
25 plotted in Figure 10 for different fill and friction conditions. It can be seen that the

1 relationship is also unique. In other words, the $T_{max}/\gamma_w L^2$ value is only affected by the
2 normalized pumping pressure and is not affected by whether the tube is filled with liquid or
3 liquid and consolidated soil. Therefore, the maximum tensile force along the tube can be
4 calculated using the theory of a geosynthetic tube inflated by slurry only. As mentioned
5 before, the normalized minimum pumping pressure, $T_{min}/\gamma_w L^2$, is also affected by the fill and
6 friction conditions as shown in Figure 11. For comparison, a curve for $T_{max}/\gamma_w L^2$ as shown in
7 Figure 10 is also plotted in Figure 11. It can be seen that the maximum difference between
8 the maximum and minimum tensile forces is $0.048\gamma_w L^2$ or 27.7% of $T_{max}/\gamma_w L^2$. However, this
9 difference may not be considered in the design as the geosynthetic tube has to be inflated by
10 slurry alone at least for the first time. The tensile strength of the geosynthetic sheet is still
11 controlled only by the pumping pressure.

12

13 4 Conclusions

14 A new analytical solution was derived in this paper to analyze geosynthetic tubes inflated by
15 slurry and consolidated soils left from previous pumping. Parametric studies were also
16 carried out to evaluate the major factors affecting the tensile stresses and geometries of the
17 tubes and the differences in the design for geosynthetic tubes inflated by slurry only and
18 those by slurry and consolidated soils.

19

20 For geosynthetic tubes inflated by both slurry and consolidated soils, the tensile forces along
21 the cross-section are not constant but have the maximum value occurring at the top of the
22 tube and the minimum value at the center of the base section in contact with the subgrade.

23 For geosynthetic tubes inflated with slurry alone, the tensile force along the cross-section
24 above the ground surface is uniform and the value is about the same as the maximum tensile
25 force in the geosynthetic tubes inflated with both slurry and consolidated soils. The

1 maximum difference between the maximum and minimum values of tensile force is about
 2 27.7%. As a geosynthetic tube has to be inflated with slurry alone when the tube is inflated
 3 for the first time, the tensile force calculation can be made using the solution for slurry filled
 4 geosynthetic tubes irrespective of the types of fill used. On the other hand, if the solution for
 5 liquid filled geosynthetic tubes is used for those filled with liquid and consolidated soils, the
 6 height of the geosynthetic tube will be overestimated by up to 18.4%, but the width
 7 underestimated by up to 10%. For these cases, the solution for geosynthetic tubes filled with
 8 slurry and consolidated soil should be used.

9

10 5 Notations

11	A	Area of cross-section
12	b	Contact width with subgrade
13	B	Width of cross-section
14	H	Height of cross-section
15	H_s	Height of the consolidated soil
16	k	Coefficient of lateral earth pressure
17	L	Perimeter of cross-section
18	p_0	Pumping pressure
19	r	Radius of the infinitesimal element
20	T	Tensile force along the geosynthetic tube per unit length
21	T_{max}	Maximum tensile force along the cross-section
22	T_{min}	Minimum tensile force along the cross-section
23	W	Total weight of the filling material
24	μ_1	Friction coefficient between consolidated soil and tube
25	μ_2	Friction coefficient between tube and subgrade
26	α	Non-dimensional parameter with its value of 0 or 1
27	γ'_s	Effective unit weight of consolidated soil
28	γ_L	Unit weight of filling slurry
29	γ_s	Unit weight of consolidated soil
30	γ_w	Unit weight of water
31	θ	The angle between x axis and the tangential direction at a point

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6 References

Box, M.J., 1965. A new method of constrained optimization and comparison with other methods. *Computer Journal* 8 (1), 42-52.

Cantré, S., 2002. Geotextile tubes--analytical design aspects. *Geotextiles and Geomembranes* 20 (5), 305-319.

Cantré, S., Saathoff, F., 2011. Design method for geotextile tubes considering strain - Formulation and verification by laboratory tests using photogrammetry. *Geotextiles and Geomembranes* 29 (3), 201-210.

Christiansen, J., 1970. Numerical solution of ordinary simultaneous differential equations of the 1st order using a method for automatic step change. *Numerische Mathematik* 14 (4), 317-324.

Chu, J., Guo, W., Yan, S.W., 2011. Geosynthetic tubes and geosynthetic mats: analyses and applications. *Geotechnical Engineering* 42 (1), 56-65.

Chu, J., Yan, S. W., Li, W., 2012. Innovative methods for dike construction– An overview. *Geotextiles and Geomembranes* 30, 35-42.

Ghavanloo, E., Daneshmand, F., 2009. Two-dimensional analytical analysis of equilibrium shape of inflated geomembrane tube resting on rigid foundation with arbitrary shape. *Geotextiles and Geomembranes*, 27 (2), 99-106.

Gughelmetti, J.L., Koerner, G.R., Battino, F.S., 1996. Geotextile reinforcement of soft landfill process sludge to facilitate final closure: An instrumented case study. *Geotextiles and Geomembranes* 14 (7-8), 377-391.

Guo, W., Chu, J., Yan, S.W., 2011. Effect of subgrade soil stiffness on the design of geosynthetic tube. *Geotextiles and Geomembranes* 29 (3), 277-284.

Guo, W., 2012. Geosynthetic tubes and mats: experimental and analytical studies. PhD thesis, Nanyang Technological University, Singapore.

- 1 Guo, W., Chu, J., Yan, S.W., Nie, W., 2013. Geosynthetic mattress: Analytical solution and
2 verification. *Geotextiles and Geomembranes* 37, 74-80.
- 3 Kazimierowicz, K., 1994. Simple analysis of deformation of sand-sausages. Fifth
4 International Conference on Geotextiles, Geomembranes and Related Products, Hydraulic
5 Applications and Related Research, Singapore 2, 775-778.
- 6 Lawson, C.R., 2008. Geotextile containment for hydraulic and environmental engineering.
7 *Geosynthetics International* 15 (6), 384 – 427.
- 8 Lee, E.C., Douglas, R.S., 2012. Geotextile tubes as submerged dykes for shoreline
9 management in Malaysia. *Geotextiles and Geomembranes* 30, 8-15.
- 10 Leshchinsky, D., Leshchinsky, O., Ling, H.I., Gilbert, P.A., 1996. Geosynthetic tubes for
11 confining pressurized slurry: some design aspects. *Journal of Geotechnical Engineering*
12 122 (8), 682-690.
- 13 Lipson, S.L., Gwin, L.B., 1977. The complex method applied to optimal truss configuration.
14 *Computers & Structures* 7 (3), 461-468.
- 15 Lukehart, P.M., 1963. Algorithm 218. Kutta Merson. *Comm. Assoc. Comput. Mach.* 6, 737-
16 738.
- 17 Malik, J., Sysala, S., 2011. Analysis of geosynthetic tubes filled with several liquids with
18 different densities. *Geotextiles and Geomembranes* 29 (3), 249-256.
- 19 Moo-Young, H.K., Tucker, W.R., 2002. Evaluation of vacuum filtration testing for geotextile
20 tubes. *Geotextiles and Geomembranes* 20 (3), 191-212.
- 21 Muthukumar, A.E., Ilamparuthi, K., 2006. Laboratory studies on geotextile filters as used
22 in geotextile tube dewatering. *Geotextiles and Geomembranes* 24 (4), 210-219.
- 23 Plaut, R., Suherman, S., 1998. Two-dimensional analysis of geosynthetic tubes. *Acta*
24 *Mechanica* 129 (3-4), 207-218.

1 Plaut, R.H., Stephens, T.C., 2012. Analysis of geotextile tubes containing slurry and
2 consolidated material with frictional interface. *Geotextiles and Geomembranes* 32, 38-43.

3 Press, W., Teukolsky, S., Vetterling, W., Flannery, B., 2007. Section 17.1 Runge-Kutta
4 Method, *Numerical Recipes: The Art of Scientific Computing* 3rd ed. Cambridge
5 University Press, New York.

6 Szyszkowski, W., Glockner, P.G., 1987. On the statics of large-scale cylindrical floating
7 membrane containers. *International Journal of Non-Linear Mechanics* 22 (4), 275-282.

8 TenCate, 2010. Seaming of geosynthetics, TenCatTM Geosynthetics North America,
9 Pendergrass, GA, <http://www.tencate.com>.

10 Worley, J.W., Bass, T.M., Vendrell, P.F., 2008. Use of geotextile tubes with chemical
11 amendments to dewater dairy lagoon solids. *Bioresource Technology* 99 (10), 4451-4459.

12 Xu, S.L., 1995. *C-algorithms commonly used procedures set* (2nd edition). Tsinghua
13 University Press, Beijing, China, (In Chinese).

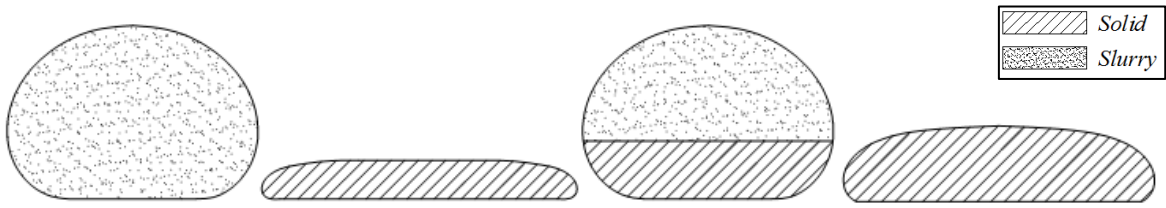
14 Shin, E.C., Oh, Y.I., 2007. Coastal erosion prevention by geotextile tube technology.
15 *Geotextiles and Geomembranes*, 25 (4-5): 264-277.

16 Yan, S.W., Chu, J., 2010. Construction of an offshore dike using slurry filled geotextile mats.
17 *Geotextiles and Geomembranes* 28 (5), 422-432.

18 Yee, T.W., Lawson, C.R., Wang, Z.Y., Ding, L., and Liu, Y., 2012. Geotextile tube
19 dewatering of contaminated sediments, Tianjin Eco-City, China. *Geotextiles and*
20 *Geomembranes* 31, 39-50.

21 Yee T. W., Lawson C. R., 2012. Modelling the geotextile tube dewatering process.
22 *Geosynthetics International* 19 (5), 339 –353.

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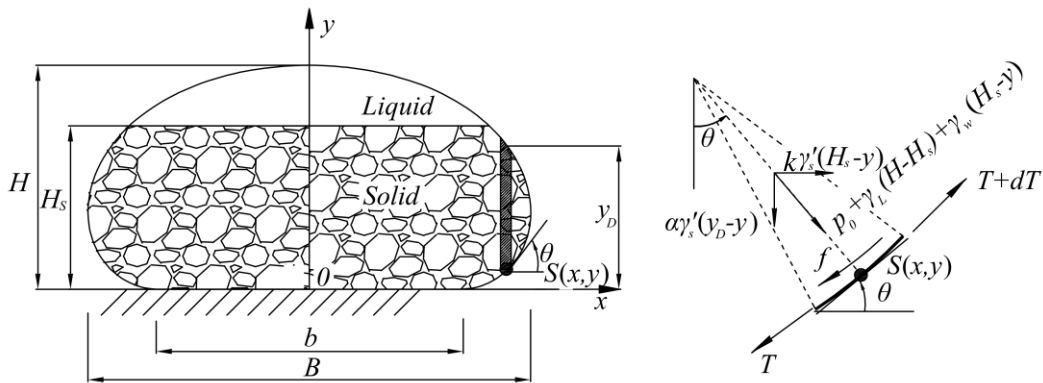
(a) 1st inflation (b) Dewatering after 1st inflation (c) 2nd inflation (d) Dewatering after 2nd inflation

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Figure 1 Inflation process of the permeable geosynthetic tubes

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a) Cross-section of geosynthetic tube (b) Free body diagram of infinitesimal element

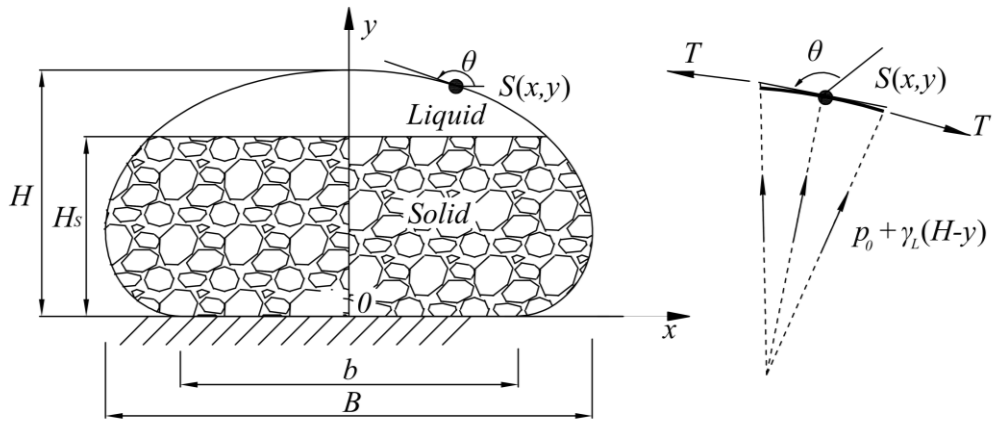
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Figure 2 Analytical model for geosynthetic tube inflated with liquid and consolidated soil

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when the infinitesimal element is below the surface of consolidated soils

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2 a) Cross-section of geosynthetic tube

b) Free body diagram of infinitesimal element

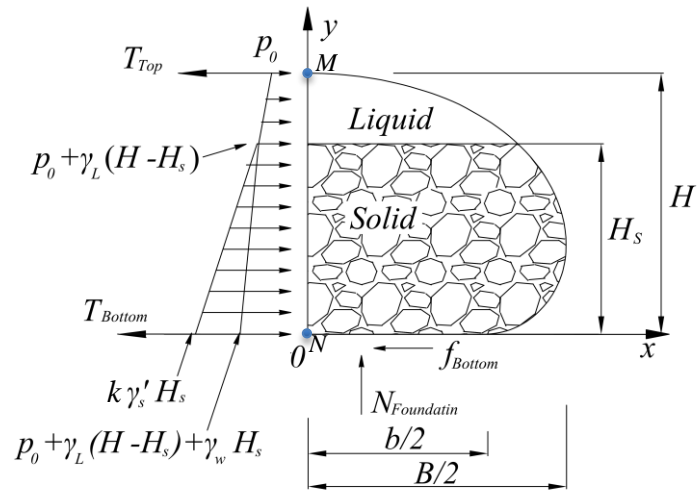
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4 Figure 3 Force equilibrium analysis for geosynthetic tube when the infinitesimal element

5 is above the surface of consolidated soils

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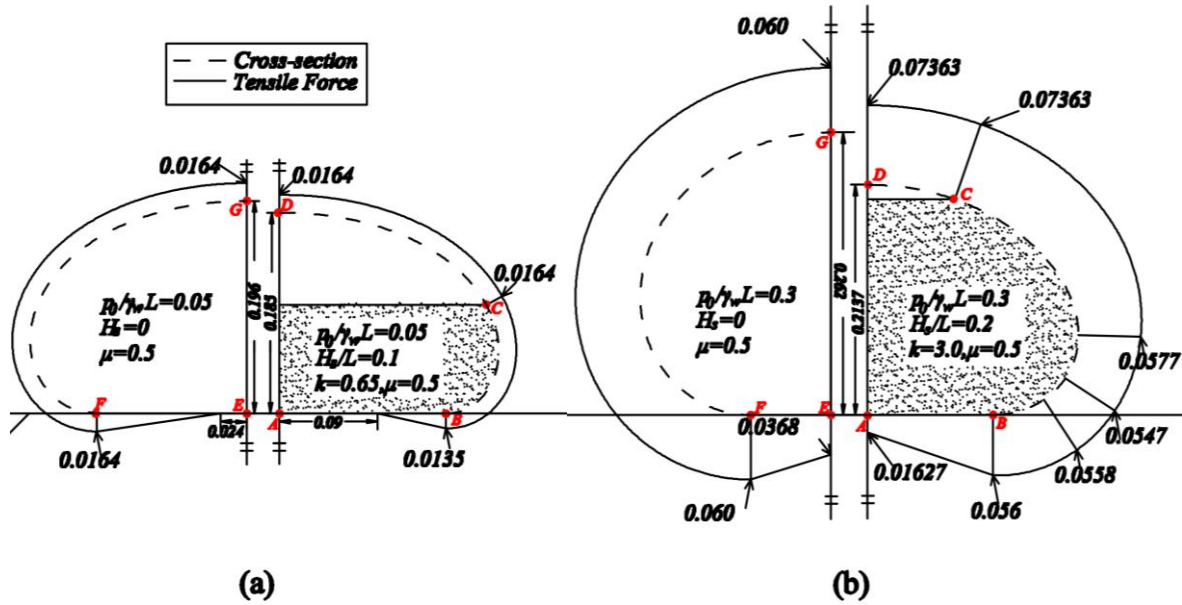


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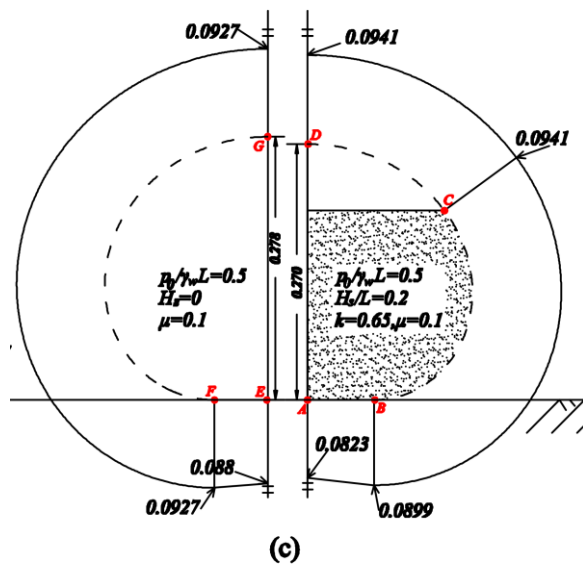
2 Figure 4 Force analysis for a cross-section along the vertical centerline

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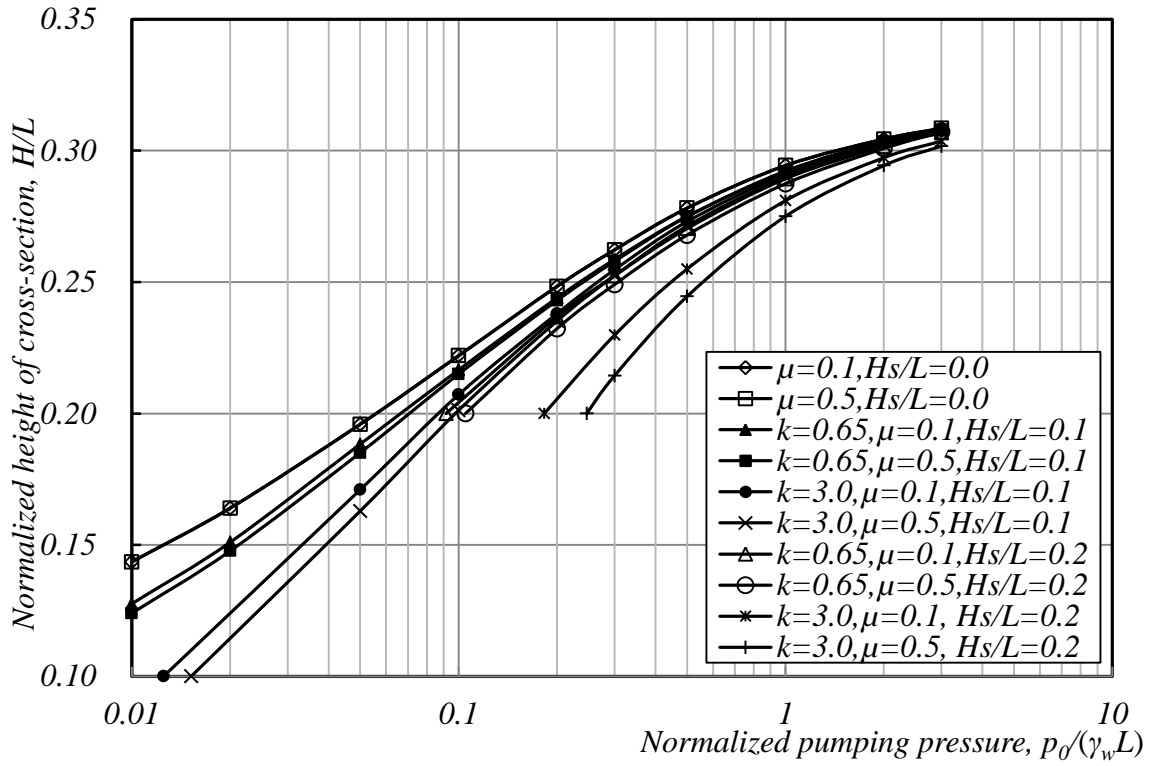
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4 Figure 5 Comparisons of cross-section and tensile force of geosynthetic tube inflated by
 5 slurry (left-hand-side) and that by slurry and consolidated soils (right-hand-side) under
 6 different conditions: (a) $p_0/\gamma_w L=0.05$, $H_s=0$, $\mu=0.5$ (left) and $H_s/L=0.1$, $k=0.65$ (right); (b)
 7 $p_0/\gamma_w L=0.3$, $H_s=0$, $\mu=0.5$ (left) and $H_s/L=0.2$, $k=3.0$ (right); (c) $p_0/\gamma_w L=0.5$, $H_s=0$, $\mu=0.1$ (left)
 8 and $H_s/L=0.2$, $k=0.65$ (right)

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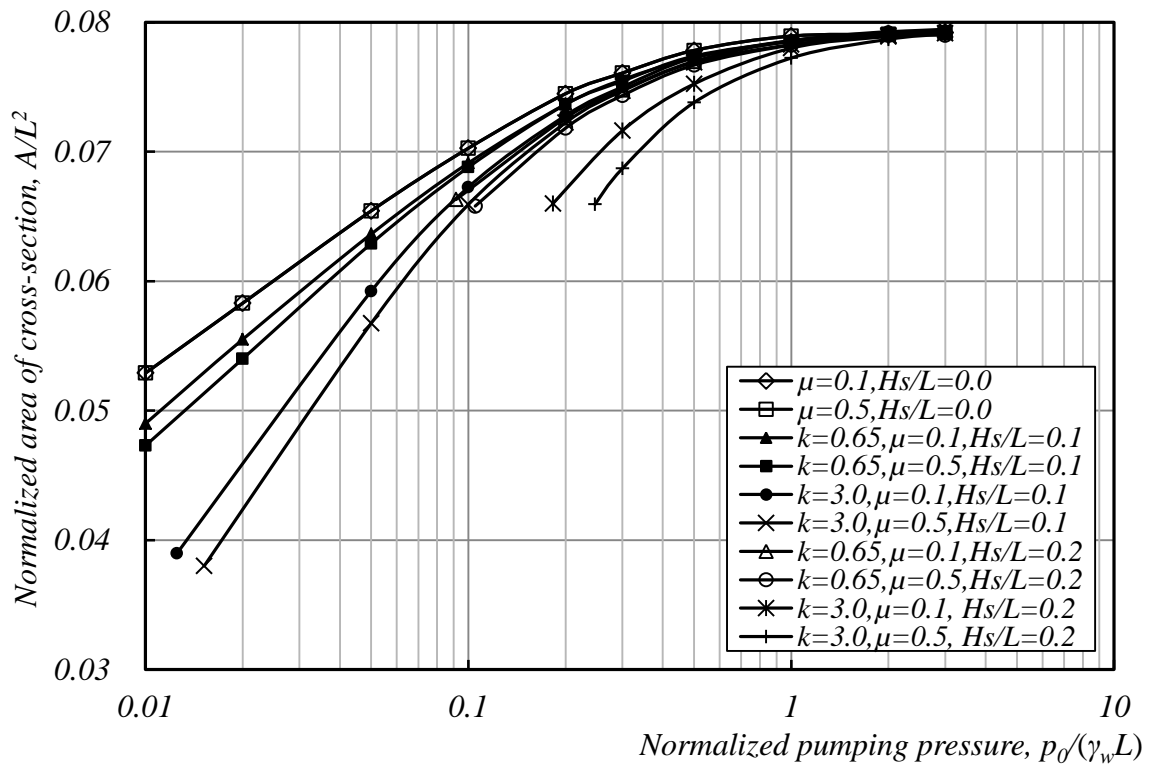
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4 Figure 6 Normalized height of cross-section vs. normalized pumping pressure for

5 different conditions

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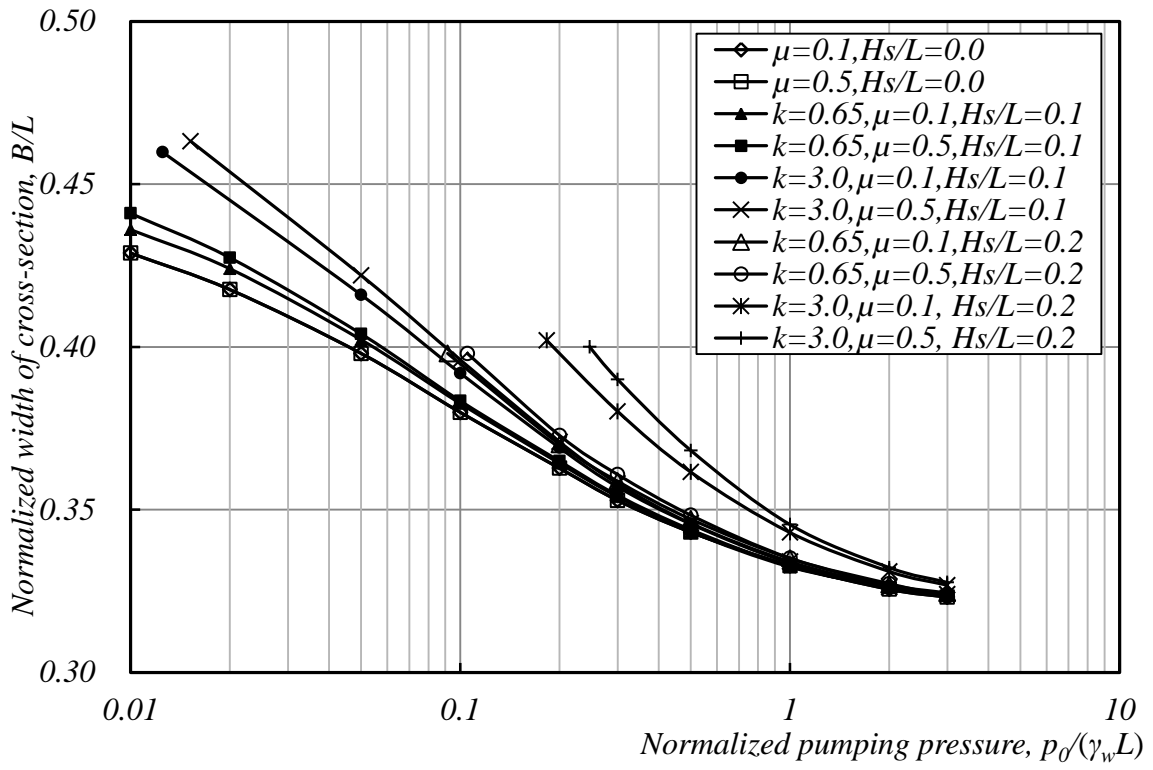
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Figure 7 Characteristics of normalized area of cross-section vs. pumping pressure

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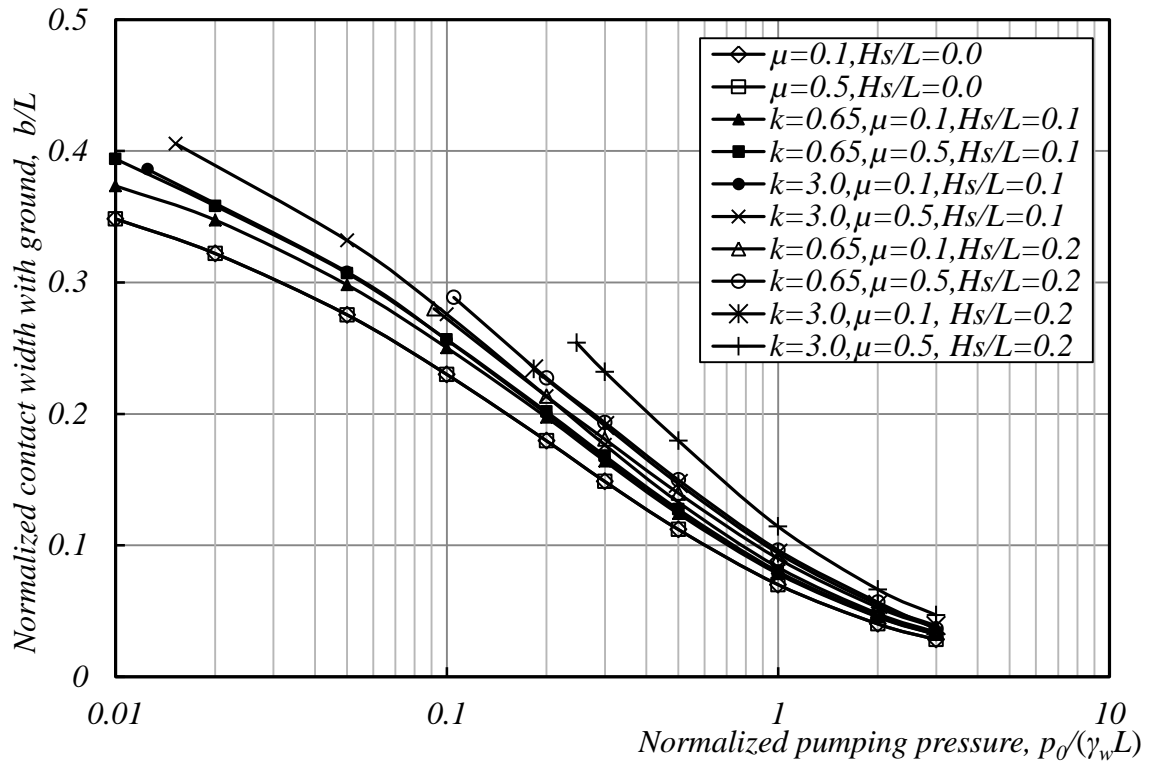


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Figure 8 Characteristics of normalized width of cross-section vs. pumping pressure

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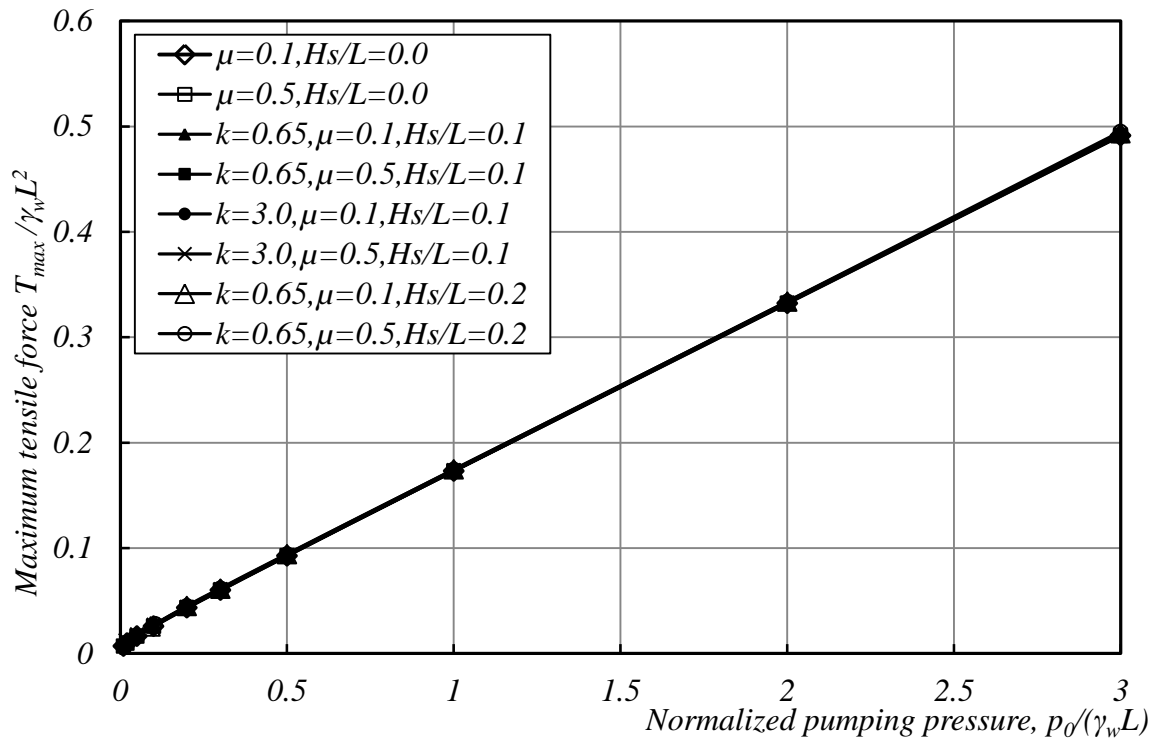


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Figure 9 Characteristics of normalized contact width with ground vs. pumping pressure

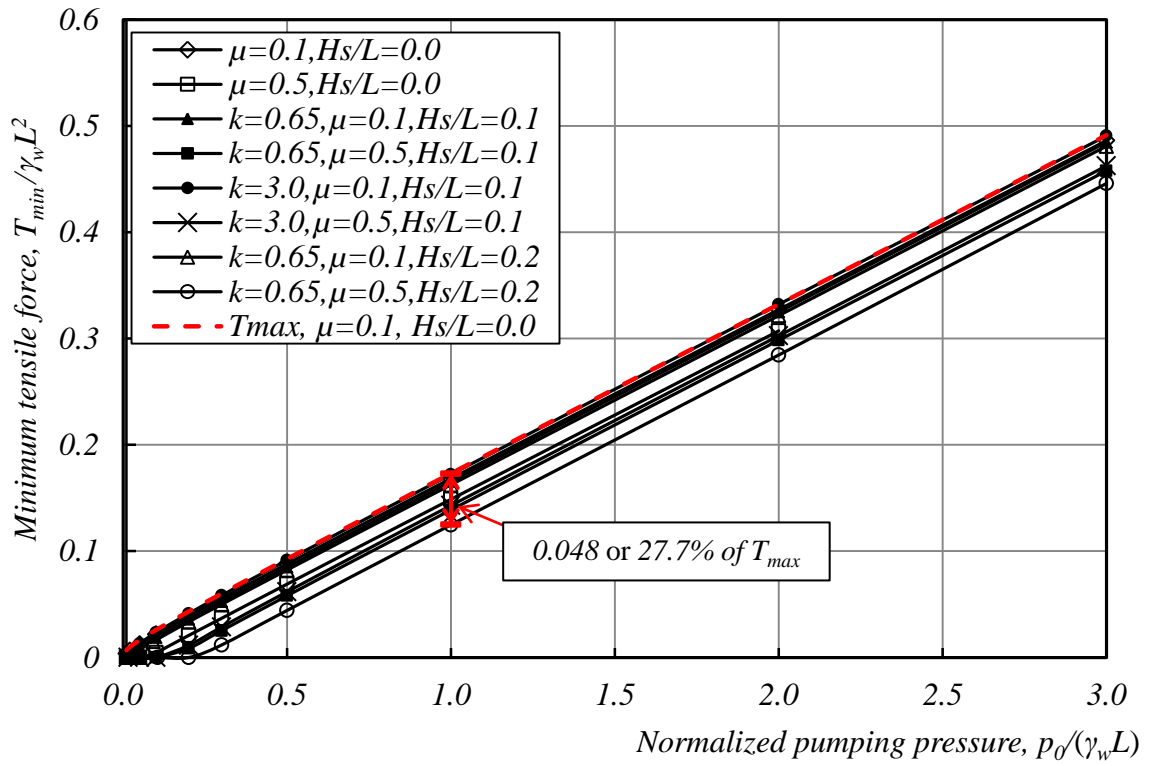
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2 Figure 10 Characteristics of normalized T_{max} vs. pumping pressure

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Figure 11 Characteristics of normalized T_{min} vs. pumping pressure