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<td><strong>Author(s)</strong></td>
<td>Bose, Sumanta; Fan, W. J.; Chen, J.; Zhang, D. H.; Tan, Chuan Seng</td>
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Strain Profile and Size Dependent Electronic Band Structure of GeSn/SiSn Quantum Dots for Optoelectronic Application

Presenter
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Presentation ID
S4D.3

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Part 1:

*Background and algorithm of atomistic quantum dot simulation.*

Part 2:

*Towards Si photonics: GeSn/SiSn – our system. Strain, gain & energy profile result*
Part 1:
Background and algorithm of atomistic quantum dot simulation.
What are Quantum Dots?

“Man-made nanoscale structures in which electrons can be confined in all 3 dimensions”

- Electron energy is quantized -> artificial atoms (coupled QD->molecule)
- Contains a countable number of electrons

Quantum dots are artificial atoms that can be custom designed for a variety of applications

M. Usman, Multi-million Atom Electronic Structure Calculation for Quantum Dots, PhD thesis (online nanoHUB)
Quantum Dots devices & applications

Laser

Photo-detector/Amplifier

Quantum Computation

World's First Semiconductor Optical Amplifier with Signal Waveform Re-shaping Function at 40Gbps

March 4, 2005

March 4, 2005

M. Usman, Multi-million Atom Electronic Structure Calculation for Quantum Dots, PhD thesis (online nanoHUB)

Quantum Information Science is rapidly progressing, and Quantum Dot based optical devices are approaching the market!
How Can Theory, Modelling, and Computation Help?

• Why Theory, Modeling and Computation?
  ✓ Modeling can provide essential insight into the physical data
  ✓ Obtain information where experimental data is not readily available
  ✓ Can help experimentalists to design their experiments

• Quantum dots grow in different shapes and sizes
• PL intensity is measured to determine light spectrum
• Experimentalists need to understand the PL spectrum

M. Usman, Multi-million Atom Electronic Structure Calculation for Quantum Dots, PhD thesis (online nanoHUB)
Atomistic simulation of QDs

Features:
- Calculates eigenstates of arbitrarily structures
- Strain: Valence force field (VFF)

Already used in simulating:
- QDs & Aligned QDs
- Long range strain effects on QDs
- Effects of wetting layer
- Piezo-electric effects in QDs
- QD nuclear spin interactions
- Impurities in QDs

3D wave-function of QD
Energy States
Absorption / Emission Spectra

M. Usman, Multi-million Atom Electronic Structure Calculation for Quantum Dots, PhD thesis (online nanoHUB)
Capabilities:

- Arbitrary shape/size of quantum dot
- Long range strain, piezoelectric fields
- Atomistic representation of alloy
- External Electrical/Magnetic fields
- Zincblende/Wurtzite crystals

M. Usman, Multi-million Atom Electronic Structure Calculation for Quantum Dots, PhD thesis (online nanoHUB)
Presentation Outline

• Part 1: Background and algorithm of atomistic quantum dot simulation.

• Part 2: Towards Si photonics: GeSn/SiSn – our system. Strain, gain & energy profile result
Part 2:
Towards Si photonics: GeSn/SiSn – our system.
Strain, gain & energy profile result.
INTO SILICON PHOTONICS
  Group IV compatibility with Si CMOS fab
  Integration of optical and electronic components onto a single microchip
  Providing faster optical data transfer between and within microchips.

CHOICE OF STRUCTURE/MATERIAL
  Quantum Dot (QD) based optoelectronic devices: a key enabler in this domain
  This work: Self assembled Ge$_{0.5}$Sn$_{0.5}$/Si$_{0.5}$Sn$_{0.5}$ QDs.

COMPUTATION METHODS
  Valence force field (VFF) using Keating potential estimates strain profile
  Electronic band structure calculation using 8 band $k \cdot p$ method

STUDY & IMPACT
  Strain profile & contour
  Energy band structure
  QD size effect on the fundamental transition energy.
The effect of tensile strain on the band structure of Ge.

**Fig a**, Schematic of how the band diagram changes as biaxial tensile strain is applied.

**Fig b**, Plot of the bandgap energies for the $\Gamma$ ($E_g(\Gamma)$) and $L$ ($E_g(L)$) bands as a function of tensile strain.

Figure (a) Band structure of bulk Ge, showing a 136 meV difference between direct & indirect BG
(b) the difference between direct & indirect BG can be decreased by tensile strain
(c) the rest of the difference between direct & indirect BG in tensile strained Ge can be compensated by filling electrons into the L valleys via n-type doping.

*Photonics 2014, 1(3), 162-197*
Our QD geometry: Pyramidal
Pyramidal QD grows along $+z$ direction, the base and wetting layer in the $x$-$y$ plane.

QD Height ($h$) = (6 to 18) $\times a_0$ and base ($2h$) = (12 to 36) $\times a_0$.

The entire system's height is $3h$ and the length/width is $4h$.

---

**Fig. 1.** Front view schematic of our pyramidal QD

**Fig. 2.** 3D schematic of our pyramidal QD

**Fig. 3.** Top view schematic of our pyramidal QD
Valence Force Field Strain Calculation

- Valence Force Field (VFF) method with Keating potential
- Calculate the strain energy, \( E_{\text{strain}} \) expressed in terms of the bond lengths and bond angles as:

\[
E_{\text{strain}} = \frac{1}{2} \sum_{i(j)} \frac{3 \alpha_{i-j}}{8 d_{0,i-j}^2} \left( \left| x_i - x_j \right|^2 - d_{0,i-j}^2 \right)^2 + \sum_{i(j)} \frac{3 \beta_{i-j-k}}{8 d_{0,i-j} d_{0,i-k}} \left[ \left| x_i - x_j \right| \left| x_i - x_k \right| + \frac{1}{3} d_{0,i-j} d_{0,i-k} \right]^2
\]

\( x_i \) is the position vector of the \( i^{th} \) atom.
For \( i-j \) bond, \( d_{0,i-j} \) & \( a_{0,i-j} \) are strain free bond length & lattice constant respectively. \( \alpha_{i-j} \) & \( \beta_{i-j-k} \) are bond stretching & bond bending force constant.

\( E_{\text{strain}} \) is minimized to attain a stable state by allowing each atom to vibrate and settle. Force on the \( i^{th} \) atom is \( F_i = -\nabla_i (E_{\text{strain}}) \).
Compare final & initial atom position to compute strain profile.
8 band $k.p$ calculation

✓ Use the 8 band $k\cdot p$ method to calculate the electronic band structure.

✓ 6 band $k\cdot p$ method does not consider the CB-VB interaction.
✓ The Hamiltonian for the strained QD can be simply written as

$$
[H = H_k + V_\Gamma(z) + H_s]
$$

✓ $H_k$ stands for the kinetic 8-band effective-mass Hamiltonian (incorporating the CB-VB/spin-orbit interaction).
✓ $V_\Gamma(z)$ accounts for the band offset effects
✓ $H_s$ stands for the strain induced Hamiltonian.
Results and Discussion

$\text{Ge}_{0.5}\text{Sn}_{0.5}/\text{Si}_{0.5}\text{Sn}_{0.5}$
Strain Profile along [001]
Strain Profile along [100]
Strain Profile $\varepsilon_{xx}$ in (001) plane, $z=0$
Strain Profile $\varepsilon_{yy}$ in (001) plane, $z=0$
Strain Profile $\varepsilon_{zz}$ in (001) plane, $z=0$
How Strain Changes the Electronic Spectra?

Strain has a very important role in QD energy, gain and optical performance.
Energy Profile

(h/a = 6)

System: Ge$_{0.5}$Sn$_{0.5}$/Si$_{0.5}$Sn$_{0.5}$

$E_1 - H_1 = 1079.27$ meV
Gain Profile
(h/a = 6)

System: Ge$_{0.5}$Sn$_{0.5}$/Si$_{0.5}$Sn$_{0.5}$

Gain vs. Energy for varying carrier concentration

Energy (meV)
Energy Profile
(h/a = 12)

System: Ge_{0.5}Sn_{0.5} / Si_{0.5}Sn_{0.5}

E1 - H1 = 511.34 meV
Energy Profile
(h/a = 18)

System: $\text{Ge}_{0.5}\text{Sn}_{0.5}/\text{Si}_{0.5}\text{Sn}_{0.5}$

Energy (in meV)

Count of energy states (50 for e$^-$ in CB & 50 for h$^+$ in VB)

$E_1 - H_1 = 414.19$ meV
Gain Profile
(h/a = 18)

System: Ge$_{0.5}$Sn$_{0.5}$/Si$_{0.5}$Sn$_{0.5}$

Gain vs. Energy for varying carrier concentration

Gain (cm$^{-1}$)

Energy (meV)
Size dependency of Band Gap of QD (inversely proportional to dimension²)

<table>
<thead>
<tr>
<th>(h/a)</th>
<th>BG (meV)</th>
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<tr>
<td>6</td>
<td>1079.27</td>
</tr>
<tr>
<td>7</td>
<td>891.70</td>
</tr>
<tr>
<td>8</td>
<td>667.96</td>
</tr>
<tr>
<td>10</td>
<td>538.59</td>
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<tr>
<td>11</td>
<td>521.54</td>
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<tr>
<td>12</td>
<td>511.34</td>
</tr>
<tr>
<td>15</td>
<td>451.57</td>
</tr>
<tr>
<td>18</td>
<td>414.19</td>
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Model: Inverse square relation

Equation: 

\[(E1-H1) = [27.07499 \ (h/a)^2 + 0.3077] \text{ eV}\]

Reduced Chi Sqr: 0.00139  
Adj. R-Square: 0.97473

Red shift pattern
✓ Studied GeSn/SiSn QDs for their strain profile and electronic band structure...
✓ ...using valence force field method and 8 band \( k \cdot p \) method.

✓ Strain profile was studied in fair depth for the [001] direction and (001) plane...
✓ ...with distinct identification of zones of compressive and tensile strain.

✓ Size effect on the fundamental transition energy was studied...
✓ ...which is an essential tuning factor in optoelectronic device designs.
✓ Selective gain curves was studied.

✓ Observed that it predominantly varies inversely with the second power of QD height.
Acknowledgement

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References (as used in the paper)

Thank you!

... for your patience and time...