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Taylor Rule and Discretionary Regimes in the United States: Evidence from a k-state Markov regime switching model.

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Taylor Rule and Discretionary Regimes in the US

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Abstract

We examine US monetary policies from 1973 to 2014 with the Taylor rule as a benchmark by utilizing a k-state Markov regime switching model in which the number and the periods of the regimes are endogenously determined. The model relates the federal funds rate with real time output gaps and inflation forecast. It endogenously identifies the periods of Taylor rule regime and discretionary regimes consistent with the US experience. The Taylor rule regime also coincides with periods of lower variability in inflation and in real GDP growth.

Keywords: Markov model, Taylor rule
1. **INTRODUCTION**

To assess monetary policy particularly in the United States, the Taylor rule (1993) has been used as a benchmark. The Taylor rule prescribes increasing the policy rate whenever inflation increases over the target inflation rate and output increases over potential output. A large body of literature examines whether the Fed followed or deviated from the Taylor rule during the past decades. The early literature on the matter exogenously determines the various US monetary policy regimes according to the duration of the terms of the chairmen of the Federal Reserve Bank. Taylor (1999) and Clarida, Gali and Gertler (2000) use revised data to examine Fed policies during the pre-Volker and Volker-Greenspan eras and they find that the Taylor principle holds only during the Volker-Greenspan era. Orphanides (2004) uses real time data available to policy makers when they make decisions and he finds that the Taylor principle is satisfied during the pre-Volker and the Volker-Greenspan eras.

More recent literature uses models that endogenously determine the periods when the Taylor principle holds. Boivin (2006) uses real time data and the time varying parameter (TVP) model on a forward-looking Taylor rule. He finds that the response of US monetary policy to forecast inflation was strong from 1970 until 1973, declined drastically from 1974 until 1982, and was strong again in mid-1980 through 1990s. In contrast, he finds that response of monetary policy to real economic activity weakened in the 1970s through the 1980s. His evidence suggests the Taylor rule may not hold from 1974 to 1982. Kim and Nelson (2006) use ex-post data and the TVP model and also find that the policy response to forecast inflation was weak in the 1970s but strengthened from the early 1980s to the 1990s. They also find that the response of federal funds rate to real GDP gap was significantly positive from 1974 to 1979 even though its response was not significantly different from zero in the 1980s.
Davig and Leeper (2006, 2011) use a Markov switching Taylor rule specification that includes the inflation, the output gaps and the variance in which four regimes are allowed namely, active monetary policy (the inflation coefficient is greater than one) with high and low variances and passive monetary policy (the inflation coefficient is less than one) with high and low variances. They use ex-post data for the United States from 1948 to 2008 and find monetary policy to be passive from 1948 to 1979 except from 1959 to 1960 and active from 1980 to 2008 except for 1991-1994 and 2001-2008. Castelnuovo, Greco and Raggi (2014) consider at two-state Markov-switching regime model with a Taylor rule specification with a time-varying inflation target. Using revised data, they identify the 1960s, 1980s and mid-1990s to 2007 as active monetary policy regimes and the 1970s and early 1990s as passive monetary policy regimes.

Murray, Nikolsko-Rzhevskyy and Papell (2015) estimate a two-state Markov-switching regime model for a forward-looking Taylor rule using real time inflation forecast and real time output gaps from 1965Q4 to 2007Q4. They find that the Taylor rule did not hold during 1973Q1-1975Q1 and 1979Q4-1985Q1, but it holds during 1965Q4-1972Q4, 1975Q2-1979Q3 and 1985Q2-2007Q4. Nikolsko-Rzhevskyy, Papell and Prodan (2013) [henceforth, NPP (2013)] also use a two-state Markov switching model on deviations from Taylor rule in which the deviations are defined as the absolute value of the difference between the federal funds rate and the implied interest rate of the Taylor (1993) rule. The two states in the Markov switching model are the high and low deviations from the Taylor rule with the former implying that the Taylor rule does not hold and the latter implying that it holds. They find the Taylor rule regime holds during 1965Q4 to 1974Q3, 1986Q2 to 2001Q1 while the discretionary regime holds during 1974Q4 to 1986Q1, 2001Q1 to 2006Q2 and 2008Q1 to 2008Q4.
We contribute to the literature by determining endogenously the United States monetary regimes from 1973Q3 to 2014Q1 with the Taylor rule as a benchmark. We utilize a $k$-state Markov regime switching model which relates the federal funds rate with real time output gaps and the real time GDP deflator inflation forecast. More specifically, for a given value of $k$, we estimate the maximized log-likelihood, the value of Schwarz (1978) criterion, and the parameters of the model. Then, we use the Schwarz criterion to choose the number of regimes, $k$, of the Markov regime switching model. The Schwarz criterion leads to the three-state Markov regime switching model with one of the three regimes specified as the forward looking Taylor (1993) rule in which the target interest rate equals one plus 1.5 times inflation forecast plus 0.5 times output gaps. In contrast, the other two regimes have inflation forecast and output gap coefficients estimated by the Markov regime switching model based on the observed data. The model identifies one of the three regimes for a given period based on the highest value of the smoothing probabilities among the three regimes. Furthermore, the estimates of the conditional variances of the federal funds rate and the plots of the implied interest rates of the other two regimes that deviate from the Taylor rule show that one regime with lower and the other regime with higher conditional variances and implied interest rates than the corresponding figures of the Taylor rule. Hence, we refer to the three regimes as the ‘Taylor rule’ regime (regime 1), the ‘low’ discretionary regime (regime 2) and the ‘high’ discretionary regime (regime 3).

We consider two commonly used measures of the output gaps from 1973Q3 to 2014Q1 in examining monetary policy regimes in the United States. The first measure calculates output gaps as percent deviations of real time GDP from its quadratic trend (‘quadratic’ output gaps). The second measure combines data of output gaps calculated from its quadratic trend, data from the Federal Reserve’s Greenbook (GB) database and data of
output gaps calculated as deviations from Congressional Budget Office (CBO) estimates of potential output (‘quadratic+GB+CBO’ output gaps).

Using the ‘quadratic’ output gaps and inflation forecast as regressors, the three-state Markov regime switching model determines 1973Q3 to 1980Q3 to be mostly low discretionary regime except for 1973Q3 to 1974Q3 and 1979Q4 to 1980Q1 when Taylor rule holds, 1980Q4 to 1986Q4 to be high discretionary regime, 1987Q1 to 1992Q1 as Taylor rule regime, 1992Q2 to 1994Q1 as low discretionary regime, 1994Q2 to 2001Q1 as Taylor rule regime, 2001Q2 to 2005Q4 as low discretionary regime, 2006Q1 to 2007Q4 as Taylor rule regime and 2008Q1 to 2014Q1 as low discretionary regime. We identify mostly the same periods of the Taylor rule regime as NPP (2013) except 1986Q2-1986Q4, which we identify as high discretionary regime and 1991Q2-1994Q1 which we identify as low discretionary regime. While NPP (2013) identify the non-Taylor regime periods as high-deviation discretionary periods, we identify these periods either as low discretionary regime (1974Q4 to 1979Q3, 1980Q3 to 1980Q3, 2001Q2 to 2005Q4 and 2008Q1 to 2008Q4) or high discretionary regime (1980Q2 to 1986Q1). They also identify 1979Q4 to 1980Q1 as high-deviation discretionary period but we identify the same period as Taylor rule period.

Using the ‘quadratic+GB+CBO’ output gaps and inflation forecast as regressors, the three-state Markov regime switching model determines the same regimes from 1973Q3 to 1986Q4 mentioned above for the specification with quadratic output gaps and inflation forecast as regressors. For period 1987Q1 to 2008Q1, the results of the Markov regime switching model show that the high discretionary regime holds until 1989Q4 (from 1980Q4) followed by the Taylor rule regime from 1990Q1 to 2008Q1. The results also show that the low discretionary regime holds from 2008Q2 to 2014Q1. In contrast, Murray, Nikolsko-Rzhevskyy and Papell (2015) find a ‘destabilizing’ Taylor rule from 1979Q4 to 1985Q1 and a ‘stabilizing’ Taylor rule from 1985Q2 to 1989Q4. Our findings are broadly consistent with
the findings of Boivin (2006) and Kim and Nelson (2006) using forward looking TVP models. To reiterate, Boivin finds a strong US monetary policy response to inflation until 1974, a weak response from 1974 to 1982, and a strong response again from the mid-1980s through the 1990s but a weak monetary policy response to real economic activity from 1970s through the 1980s. Kim and Nelson find a weak monetary policy response to expected inflation with significantly positive effect of the federal funds rate on real GDP gap in the 1970s but a strong response to expected inflation with insignificant effect of federal funds rate on real GDP in the 1980s.

With the regimes determined from the model, we calculate the average inflation variability and real GDP growth variability of the three regimes. We find that the average inflation and real GDP growth variability are lower during the Taylor rule regime compared with the two discretionary regimes.\(^5\)

The paper is organized as follows: Section 2 discusses the \(k\)-state Markov regime switching model, the estimation methods and the data; Section 3 discusses the empirical results and Section 4 gives the conclusions.

2. METHODOLOGY AND DATA

2.1 Markov regime switching model

The monetary rule for central banks proposed by Taylor (1993) is specified as:

\[
i_t = \pi_t + \phi(\pi_t - \bar{\pi}) + \gamma y_t + r^*\tag{1}\]

where \(i_t\) is the target short term interest rate, \(\pi_t\) is the inflation rate, \(\bar{\pi}\) is the target inflation rate, \(y_t\) is the output gap and \(r^*\) is the equilibrium real interest rate. The output gap is the actual real GDP minus its estimated potential real GDP over potential real GDP multiplied by 100. Inflation is the year-on-year percentage change in aggregate prices. The target short term interest rate is equal to the actual short term interest rate assuming the central bank achieves its target interest rate within the period. According to Taylor (1993), \(\phi = \gamma = 0.5\) and \(\bar{\pi} = r^*\)
= 2% for the United States. Furthermore, since the Fed is assumed to be forward looking, we adopt the forward-looking Taylor rule so Equation (1) becomes:

$$i_t = 1 + 1.5E_t \pi_{t+h} + 0.5y_t$$

(2)

where $E_t \pi_{t+h}$ is the expectation at $t$ of the inflation at $t+h$.

Whether or not the Fed follows the Taylor rule at time $t$ depends on the economic conditions at that time. As the economic conditions change over time, the Fed may deviate from the Taylor rule so the nominal interest rate is no longer determined by Equation (2). Hence, in the $k$-state Markov regime switching model, let the indicator $S_t$ represent the state of the monetary policy at time $t$ with $S_t = 1$ for the state in which the Fed implements the Taylor rule and with $S_t = j$ ($j > 1$) for the state in which the Fed deviates from the Taylor rule. The nominal interest rate is determined by:

$$i_t = \beta_{0,S_t} + \beta_{1,S_t} E_t \pi_{t+h} + \beta_{2,S_t} y_t + \varepsilon_t$$

(3)

where $(\beta_{0,S_t}, \beta_{1,S_t}, \beta_{2,S_t}) = (1, 1.5, 0.5)$ if $S_t = 1$, otherwise $(\beta_{0,S_t}, \beta_{1,S_t}, \beta_{2,S_t}) \neq (1, 1.5, 0.5)$; and $\varepsilon_t | S_t = j \sim N(0, \sigma_j^2)$. The dynamics of the state is governed by a $k$-state first-order Markov chain with transition probabilities defined by:

$$P(S_t = j | S_{t-1} = i) = p_{ij} \text{ where } i, j \in \{1, \ldots, k\}.$$

(4)

Under the above setup, the $k$ possible states (or regimes) of the monetary policies are characterized by the $k$ possible specifications that relate the interest rate to inflation forecast and output gaps, each corresponding to a particular state of monetary policy. If $k=1$, the regression coefficients $(\beta_{0,1}, \beta_{1,1}, \beta_{2,1})$ are estimated instead of fixed at $(1, 1.5, 0.5)$. If $k>1$ and the Fed employs the Taylor rule in a period, the interest rate for that period is expected to be determined by Equation (2); and if the Fed deviates from the Taylor rule, the interest rate is expected to relate to the inflation forecast and output gaps with the regression coefficients different from Equation (2). However, at any point in time, the Fed does not reveal to the
public whether or not it follows the Taylor rule so the public could only make inferences regarding the state or regime of monetary policy at time $t$ based on observed information. Hence, the state variable $S_t$ is a latent variable in the Markov regime switching model.

We implement our method in two steps. First, for a given value of $k$, we obtain the maximized log-likelihood, the value of the Schwarz (1978) criterion for model selection, as well as the maximum likelihood estimates of the model parameter vector

$$\theta = \{\beta_{0,j}, \beta_{1,j}, \beta_{2,j}, \sigma^2_j, \theta_{ij}; i, j = 1, \ldots, k\}$$

with quarterly data $Z^T = \{(i_t, \pi_t, y_t), i; 1 \ldots T\}$ via the EM algorithm using the method described in Hamilton (1994, Chapter 4). Second, we determine the number of regimes, $k$, by the Schwarz criterion defined as $-2 \log (L) + n \log(T)$ where $L$ refers to the likelihood under the fitted model, $T$ is the total number of observations, and $n$ is the number of free parameters to be estimated in the model. Note that $n = 4, 7, 15$ and 25 for $k = 1, 2, 3,$ and 4, respectively. As shown in Leroux (1992), the maximum likelihood estimates derived from the two-step estimation procedure are consistent and asymptotically normal.6

Based on the selected model, we then carry out inference about the state variable $S_t$ for each quarter $t$ with the smoothing probability defined by:

$$P(S_t = j | Z^T, \hat{\theta}), j = 1, \ldots, k \text{ and } t = 1, 2, \ldots, T. \quad (5)$$

Specifically, quarter $t$ is identified with regime $j$ if the smoothing probability at time $t$ for regime $j$ has the highest value among the $k$ smoothing probabilities for that quarter. For example, quarter $t$ is identified with the Taylor rule regime if the probability of being in that regime, $P(S_t = 1 | Z^T, \hat{\theta})$, exceeds the smoothing probability for any other regime, i.e., $P(S_t = 1 | Z^T, \hat{\theta}) > P(S_t = j | Z^T, \hat{\theta})$ for any $j > 1$.

Under the Taylor rule, the nominal interest rate is expected to respond to divergences of actual inflation rates from target inflation rates and of actual real GDP from potential real
GDP as specified by Equation (2). This may suggest an association between monetary regimes and the variability of inflation or of real GDP growth. Thus, we calculate and compare the average variability of inflation and of real GDP growth for each regime. We use two measures of inflation: GDP deflator inflation, as defined above, and consumer price index (CPI) inflation, which is the year-over-year percentage change in quarterly CPI. Real GDP growth is calculated as the quarterly change in real GDP. We measure inflation (real GDP growth) variability for quarter \( t \), denoted as \( \nu_t \), as \[ \nu_t = \frac{(r_{t-1}^2 + r_{t-2}^2 + r_{t-3}^2 + r_{t-4}^2)}{4}, \] where \( r_t \) is the change in inflation (real GDP growth) from quarter \( t-1 \) to quarter \( t \). The average variability for a particular regime is the average of \( \nu_t \) over the periods of the regime.

### 2.2 The Data

Data on output gap, inflation and effective federal funds rate are downloaded from Alex Nikolsko-Rzhevskyy’s website. We use from the dataset two measures of the output gap: the real time ‘quadratic’ output gap and the real time ‘quadratic+GB+CBO’ output gap. The ‘quadratic’ output gap is the percentage deviation of real time GDP from its the quadratic trend. As discussed in NPP (2013), the quadratic trend is estimated beginning in 1947Q1 until the vintage year. The first vintage year is 1965Q4 and the last vintage year is 2010Q2 so ‘quadratic’ output gap data from the dataset are from 1965Q4 to 2010Q2. Following this procedure and using up-to-date real time GDP data from the Fed, we extend the ‘quadratic’ output gap series to 2014Q1.

The ‘quadratic+GB+CBO’ output gap series augments the output gaps from Federal Reserve Bank’s Greenbook dataset which only covers 1987Q1 to 2007Q4, with output gap estimates based on quadratic detrending of real time real GDP from 1965Q4 to 1986Q4 and with estimates based on the potential real GDP published by the Congressional Budget Office (CBO) from 2008Q1 to 2010Q2. We extend the ‘quadratic+GB+CBO’ output gap series to
2014Q1 using recently available real time real GDP data from the Fed and the potential real GDP data from the CBO.

We also use from the Nikolsko-Rzhevskyy’s dataset the real time GDP deflator inflation forecast and the effective federal funds rate. We only consider the real time GDP deflator inflation forecast and not real time GDP deflator inflation because of the common belief that the Fed is forward looking in formulating monetary policies. Real time GDP deflator inflation forecast data are averages of four consecutive quarters of the inflation forecast from the Greenbook database (1973Q3 to 2007Q4) and Survey of Professional Forecasters (SPF) (2008Q1-2010Q2) database.\(^{11}\) We update the data on GDP inflation forecast and effective federal funds rate to 2014Q1 using data from Federal Reserve Bank websites.

We use real time ‘quadratic’ output gaps and the ‘quadratic+GB+CBO’ output gaps to consider the possibility of spurious evidence of regime switches arising from splicing of the data.\(^{12}\) As mentioned above, the ‘quadratic+GB+CBO’ output gaps are spliced from real time quadratic output gaps (1965Q4-1986Q4), the Greenbook output gaps (1987Q1-2007Q4) and the CBO output gaps (2008Q1-2014Q1). In contrast, the real time quadratic output gap data—which has the same output gap observations from 1965Q4 to 1986Q4 as the ‘quadratic+GB+CBO’ output gaps—are continuous estimates using the quadratic trend of real time GNP/GDP from 1965Q4 to 2010Q2 extended to 2014Q1 using NPP’s (2013) procedure. In addition, the real time GDP deflator inflation forecast data are continuously available at the Greenbook dataset from 1973Q3 to 2007Q4 and spliced only with data from SPF from 2008Q1 to 2014Q1. To examine the possibility of spurious evidence of regime switches from spliced data, we compare the periods of the regime switches using the two measures of output gaps from 1973Q3 to 2007Q4.\(^{13}\)
For comparisons of variability of inflation and real GDP growth among the various regimes, we use quarterly revised data on percentage changes over the corresponding quarter of the previous year of the GDP deflator and of the CPI (all items) and on percent changes in real GDP obtained from the International Financial Statistics.

3. EMPIRICAL RESULTS

We endogenously determine the Federal Reserve Bank’s monetary policy regimes from 1973Q3 to 2014Q1 using the \( k \)-state Markov regime switching model with two datasets. The first dataset includes quarterly values of the real time ‘quadratic’ output gap together with quarterly federal funds rates and real time GDP deflator inflation forecasts, while the second dataset replaces the data of output gap in the first dataset by the data of the real time ‘quadratic+GB+CBO’ output gaps.

For each value of \( k (>1) \), we fit each of the two datasets to the \( k \)-state Markov regime switching model to obtain the maximized log-likelihood and the value of the Schwarz criterion. For \( k=1 \), we fit the data to the linear regression model to estimate the coefficients \((\beta_{0,1}, \beta_{1,1}, \beta_{2,1})\) from Equation (3). Table 1 reports the results for \( k=1, 2, 3, \) and 4 of the two data sets. For both datasets, the Schwarz criterion decreases from \( k=1 \) until \( k=3 \) and then rises at \( k=4 \). Since the Schwarz criterion begins to increase after \( k=3 \), we consider only up to \( k=4 \). Hence, the Schwarz criterion leads to the selection of the three-state Markov regime switching model as it has the smallest value for the criterion among the four models.

Insert Table 1 here

The parameter estimates of the three-state Markov regime switching model run on the first dataset (real-time inflation forecast and quadratic output gaps) and on the second data set (real time inflation forecast and ‘quadratic+GB+CBO’ output gaps) are shown in Table 2 and Table 3, respectively. Table 2 and Table 3 show quantitatively similar results. For regime 2, the inflation coefficients are between one and 1.5 and significant at the 1% level (1.21 in
Table 2 and 1.27 in Table 3) and the output gap coefficients are significant at the 5% level and less than 0.5 (0.27 in Table 2 and 0.14 in Table 3). The constants are negative and significant at the 5% level (-0.34 in Table 2 and -1.22 in Table 3). The results for regime 2 of Table 1 and Table 2 show the inflation forecast coefficients, output gap coefficients and constants are less than the Taylor rule weights of 1.5, 0.5, and 1.0 respectively, at the 1% level of significance.\textsuperscript{14}

\textbf{Insert Table 2 here}

\textbf{Insert Table 3 here}

For regime 3, the inflation forecast coefficients are 1.52 and 1.60 in Table 2 and in Table 3, respectively, at the 5% significance level. These coefficients are close to the weight of 1.5 of the benchmark Taylor-rule regime. The output gap coefficients are -0.05 in Table 2 and -0.08 in Table 3 and insignificant at the 10% significance level. The constants are 3.14 and 2.39 in Table 2 and in Table 3, respectively, and significant at the 1% level. Compared to the Taylor rule, the inflation forecast coefficients are not significantly different from 1.5 at the 10% level of significance, while the coefficients of output gaps are significantly different from 0.5 and the constants are significantly different from one at the 5% and higher levels of significance.\textsuperscript{15} Since the constants for regime 2 and 3 in both Table 2 and Table 3 are significantly different from 1, this suggests that the equilibrium real interest rate and/or the target inflation rate may vary over time.

Table 2 and Table 3 also show the conditional variances of the Federal funds rate and the transition probabilities. The results in both tables are quantitatively similar. Table 2 (Table 3) shows conditional variances are 0.48 (0.55) for the Taylor rule regime, 0.40 (0.33) for the regime 2, and 1.69 (1.57) for the regime 3 at the 5% and higher levels of significance. The results show that the conditional variances of regime 2 are less than the conditional variances of the Taylor rule regime while the conditional variances of regime 3 are greater
the Taylor rule regime. In addition, Table 2 and Table 3 show the estimated transition probabilities \( P(S_t = j | S_{t-1} = i) = p_{ij} \) that if the Fed is in a particular monetary regime \( i \) for a quarter, the Fed will either remain in the same regime \( (i=j) \) or switch to another monetary regime \( j \) \((i\neq j)\) for the next quarter. In particular, the transition probabilities of remaining in the same regime over two quarters are over 90\% for all the three regimes \( (p_{11}=0.92 \ (0.96), \ p_{22}=0.94 \ (0.95) \ \text{and} \ p_{33}=0.96 \ (0.97) \) in Table 2 (Table 3)). Hence, it implies that each of the three regimes is persistent, suggesting that the Fed likely follows or deviates from the Taylor rule for several quarters.

The last three rows of Table 2 and Table 3 show the average variability of the CPI inflation, of GDP deflator inflation and of real GDP growth for each of the three regimes. The tables clearly show that on average, the variability of CPI inflation, of GDP deflator inflation and of real GDP growth in regime 1 (Taylor rule regime) are less than the variability of regime 2 or regime 3. Hence, the Taylor rule regime may be associated with lower variability of inflation and real GDP growth while the discretionary regimes may be associated with higher variability of inflation and output growth.

We calculate the implied interest rates based on the fitted model for the three regimes and plot them in Figure 1 for the first dataset and Figure 2 for the second dataset where the light solid line, the dotted line, and the dashed line represent the interest rates implied by Taylor rule regime (regime 1), the low discretionary regime (regime 2), and the high discretionary regime (regime 3), respectively. Figure 1 and Figure 2 show that the implied interest rate of regime 2 is less than the implied interest rate of the Taylor rule regime (except for three to four quarters in 2009), while the implied interest rate of regime 3 is greater than the implied interest rate of the Taylor rule regime. This suggests that when the Fed deviates from the Taylor rule, the interest rate could be expected to be either lower or higher than the rate implied by the Taylor rule.
Since we find lower (higher) conditional volatility and implied interest rates in regime 2 (regime 3) compared to those of the Taylor regime (regime 1), we refer to regime 2 and regime 3 as ‘low’ and ‘high’ discretionary regimes, respectively.

Figure 1 and Figure 2 also show the classifications of the three regimes based on the largest estimated smoothing probability among the three regimes. The unshaded areas correspond to the Taylor rule regime while the shaded areas correspond to the regimes that deviate from the rule, with the light (dark) shaded areas indicating regime 2 (regime 3). As mentioned above, the implied interest rates of regimes 1, 2, and 3 are indicated by the dashed-and-dotted line, the dotted line, and the dashed line, respectively. In addition, the effective federal funds rate are indicated by the solid line.

Figure 1 and Figure 2 show similar results from 1973Q3 to 1986Q4 and 2008Q2 to 2014Q1. Both figures show regime 1 (Taylor rule) holds during 1973Q3-1974Q3 and 1979Q4-1980Q1; regime 2 (low discretionary regime) holds during 1974Q4-1979Q3, 1980Q2-1980Q3 and 2008Q1-2014Q1 while regime 3 (high discretionary regime) holds during 1980Q4-1986Q4.

The differences between Figure 1 and Figure 2 occur from 1987Q1 to 2007Q4. Figure 1 shows that regime 1 or Taylor rule holds during 1987Q1-1992Q1 and 2006Q1-2007Q1 and regime 2 or the low discretionary regime holds during 1992Q2-1994Q1 and 2001Q2-2005Q4. In contrast, Figure 2 shows that the high discretionary regime (regime 3) extends to 1989Q4 (from 1980Q4) followed by a periods in which the Taylor regime or regime 1 hold from 1990Q1 to 2008Q1. These differences also coincide with the use of output gaps estimated from the quadratic trend in Figure 1 and of the output gaps estimated from Greenbook dataset of the Fed in Figure 2. We plot the ‘quadratic’ output gaps and ‘quadratic+GB+CBO’ output
gaps in Figure 3, which shows that the output gaps measured from the quadratic trend are greater than the output gaps from the Greenbook dataset. Hence, this leads to estimates of the interest rate implied by the Taylor rule to be greater in Figure 1 than in Figure 2 from 1987Q1 to 2007Q4.

Insert Figure 3 here

While the differences between Figure 1 and Figure 2 are in the periods 1987Q1 to 2007Q4, we note that before 2007Q4, the changes in regimes in both figures do not coincide with the 1986Q4-1987Q1 in which the data on ‘quadratic’ output gaps (1965Q4-1986Q4) were combined with the data on Greenbook output gaps (1987Q1-2007Q4). However, the regime switch from Taylor rule regime (regime 1) to low discretionary regime (regime 2) occurred in 2007Q4-2008Q1 when the inflation forecast data from Greenbook and SPF, and output gaps data from the Greenbook and the CBO, were combined to construct the respective series until 2014Q1.

The implications of the differences in Figure 1 and Figure 2 for 1990Q1 to 2008Q1 are that Figure 2 shows the Fed followed the Taylor rule if the implied rates are calculated using GDP inflation forecast and output gaps from the Greenbook dataset but Figure 1 shows two periods of low discretionary regimes during 1992Q2-1994Q1 and 2001Q2-2005Q4. Therefore, the results of the three-state Markov regime switching model with Greenbook data (Figure 2) would show support to Bernanke’s (2010) argument that the Fed followed the Taylor rule in the mid-2000 rather than Taylor’s (2008) argument that the Fed deviated from the Taylor rule and caused the housing price bubble. The reverse would be the case if the inflation forecast and quadratic output gaps (Figure 1) are used as regressors in the Markov regime switching model.

As mentioned above, both Figure 1 and Figure 2 show that the low discretionary regime holds from 2008Q2 to 2014Q1. In both cases, the implied rates of the low
discretionary regime and the Taylor regime from 2009Q1 to 2014Q1 may be negative from one to eight quarters but they are not significantly different from zero.\textsuperscript{16}

4. CONCLUSIONS

We examine US monetary policies from 1973 to 2014 using a $k$-state Markov regime switching model in which the number of regimes is determined using the Schwarz (1978) criterion and the periods of the regimes are endogenously determined from the data. The model presents a unified and simplified framework with the results consistent with the experience of the United States in the Fed’s conduct of monetary policies. Using the Taylor rule as a benchmark, we find the low discretionary regime holds in the 1970s, which could be interpreted as too stimulative even though the low discretionary regime has a coefficient on inflation forecast greater than one. This finding is consistent with Nikolsko-Rzhevskyy and Papell’s (2012) conclusion that the Taylor rule was destabilizing and too stimulative, contrary to Orphanides’s (2003a,b) claim that the Fed followed a stabilizing Taylor rule in the 1970s.

We also find the high discretionary regime holds in the 1980s, which could be considered too restrictive using the Taylor rule as a benchmark. Our findings from the mid-1990 to 2008 differ depending on the measures of the output gap. Using the ‘quadratic’ output gaps, the high discretionary regime that began in 1980 ended in 1986. From 1987 to 2008, the Taylor rule regime mostly holds, except from 1991 to 1992 and from 2001 to 2005 when the low discretionary regime holds. These findings support Taylor’s (2008) argument that the Fed deviated from the Taylor rule and caused the housing price bubble. However, using the output gaps from the Federal Reserve’s Greenbook dataset, we find that the high discretionary regime ended in 1989 followed by the Taylor rule regime until 2008. Therefore, the Fed’s own estimates of the output gaps support Bernanke’s (2010) contention that the Fed followed the Taylor rule in the 2000s and could not have caused the housing price bubble. Hence, we show that the Taylor (2008) and the Bernanke (2010) disagreement could not only
be due to differences in measures of inflation or the use of either inflation or inflation forecast as discussed in Bernanke (2010) and Nikolsko-Rzhevskyy and Papell (2013), but also differences in the estimates of the output gaps.

For both measures of the output gaps, we find that the low discretionary regime holds from 2008 to 2014 with implied interest rates negative for up to eight quarters but not significantly different from zero. Hence, neither the low discretionary regime nor the Taylor rule offers justification for the Fed’s quantitative easing conducted by the Fed during the 2008 financial crisis. These findings are consistent with the conclusions of Nikolsko-Rzhevskyy and Papell (2013).

We also observe that the variability of CPI inflation, GDP deflator inflation and real GDP growth are lower during the Taylor regime compared the two discretionary regimes. However, our coefficient estimates of the discretionary regimes (regimes 2 and 3) show that the coefficients of inflation forecast in the Taylor rule specification to be greater than one. This implies that if the interest rates were valid targets of Fed’s policies, interest rates responded more than one-for-one to the inflation forecast so that the Taylor principles held even in periods during the “low” and “high” discretionary regimes. Therefore, our results show that inflation variability could be substantially higher even when discretionary monetary policy seemingly adheres to the Taylor principle.

NOTES

1 Murray, Nikolsko-Rzhevskyy and Papell (2015) use data on inflation forecast taken from the Fed’s Greenbook (GB) dataset updated with data from the Survey of Professional Forecasters (SPF) and two measures of real time output gaps: the first measure is taken from Orphanides (2004) based on Council of Economic Advisers (CEA) estimates updated with output gaps calculated using Congressional Budget Office (CBO) potential output; and the
second measure is calculated by taking the deviations of real time real GNP/GDP from its quadratic trend.

2 NPP (2013) use real time inflation rates calculated as the year-on-year change of the GDP deflator, and real time output gaps calculated as percentage deviations from the quadratic trend of real GDP. In addition to the two regime Markov switching model, they examine endogenously the periods of the occurrences of high and low deviations from Taylor rule using linear regressions with multiple breaks.

3 We are aware only of Nikolsko-Rzhevskyy and Papell (2013), who studied the post 2008 financial crisis period (2009-2011) in the context of Taylor rule. They compare specifications of the original and modified versions of the Taylor rule during various recessions in the past decades including the post 2008 crisis.

4 Our paper differs from NPP (2013) as follows: 1. Our Markov regime switching model endogenously determines the number of different monetary regimes, $k$, based on the Schwarz criterion with $k$ determined at three and the first regime restricted to the specification of the Taylor rule. In contrast, NPP’s Markov regime switching model assumes two monetary regimes defined as large and small deviations measured by the absolute difference between the Fed funds rate and the rate implied by the Taylor rule; and 2. Our model allows for the different coefficients of inflation and output gaps and for different conditional variances of the federal funds rates among different monetary regimes.

5 Real GDP volatility and inflation volatility are often considered in examining the Great Moderation in G-7 countries from the 1980 to 2007. While the ‘Great Moderation’ is beyond the scope of the paper, we would like to examine if and how variability in real GDP and in inflation are likely associated with a particular monetary regime. Clark (2009) and Benati and Surico (2009) give a short review of the literature on the Great Moderation.
Tests for the number of regimes under Markov regime switching models are typically difficult to carry out because they do not follow standard distributions. For instance, under the null of a single regime versus the alternative of two regimes, the parameters of the alternative regime are not identified. This means conventional likelihood ratio tests are not asymptotically chi-square distribution. Several researchers have addressed this issue only for certain types of Markov regime switching models, particularly for testing two regimes such as Garcia (1998). However, our study considers Markov regime switching models with more than two regimes and as far as we know, there are no available tests for models with more than two regimes. In contrast, model selection criteria such as the Schwarz criterion are commonly used in various applications to estimate the number of regimes for Markov regime switching models (e.g., Wang and Puterman 1999; Haas, Mittnik and Paolella, 2004). As pointed out by Rydén (1995), the Schwarz criterion in the limit never underestimate the number of regimes in Markov regime switching models.

Revised real GDP growth and changes in CPI are used as measures of output growth and inflation, respectively, in the literature on the ‘Great Moderation.’ As a comparison, we also consider revised GDP deflator inflation to measure inflation variability consistent with our measure of inflation using real time data.

The website, https://sites.google.com/site/alexrzhevskyy/files/data_rules_discretion.zip, is mentioned in NPP (2013). The dataset has quarterly data from 1965 Q4 to 2010 Q2 with six measures of real-time output gaps namely, quadratic gap, linear gap, window output gap, HP gap and two output gap measures that augment the Federal Reserve Bank’s Greenbook dataset which only covers 1987 Q1 to 2007 Q4. It also has data on real-time GDP deflator inflation, GDP deflator inflation forecast and effective federal funds rate. The original data used in the construction of the real time output gaps, real time inflation and real time inflation
forecast are from the Federal Reserve Bank of Philadelphia and the effective federal funds rate are from the Federal Reserve Bank of St Louis.

9 Two other popular measures of the output gaps use linear detrending and the Hodrick-Prescott (HP) filter. However, NPP (2013) recommend using the ‘quadratic’ output gaps instead of ‘linear detrending’ output gaps and ‘HP filter’ output gaps. Their recommendation is based on their assessment of the three measures of the output gaps which considered the real time unemployment rates and the estimates of the natural rate of unemployment and of the Okun’s law coefficient for the United States.

10 Details of the construction of real time output gaps in Nikolosko-Rzhevskyy website are discussed in NPP (2013) (output gap estimates using quadratic trends) and Nikolosko-Rzhevskyy and Papell (2013) (output gap estimates from the Greenbook dataset augmented with estimates using potential output data from the CBO).

11 The construction of the real time GDP deflator inflation forecast is discussed in Murray, Nikolosko-Rzhevskyy and Papell (2015). This series matches the four-quarter averages of median growth of the GDP deflator forecast from the SPF database accessed from the Federal Reserve Bank of Philadelphia website. Data on real time GDP deflator inflation forecast are available without missing observations from 1973Q3 onwards.

12 This possibility is pointed out by NPP (2013).

13 Among others, Nikolsko-Rzhevskyy and Papell (2013) and Murray, Nikolsko-Rzhevskyy and Papell (2015) use inflation forecast and Greenbook output gaps in examining Taylor rules.

14 We use the t-test to determine if the coefficients of regime 2 are significantly different from the corresponding weights suggested by the Taylor rule as follows: (coefficient of the variable in regime 2 – corresponding weight of the variable in Taylor rule)/ standard error of coefficient of the variable in regime 2. The standard errors of the weights of the Taylor rule
are assumed to be zero. For a comparison with coefficients of regime 2 and Taylor rule regime in Table 2, the t-statistics for inflation forecast coefficient, output gap coefficient and the constant of regime 2 compared with 1.5, 0.5 and 1.0 are -9.67, -11.5 and -8.93, respectively. From Table 3 for regime 2, the t-statistics for inflation coefficient, the output gap coefficient, and the constant compared to 1.5, 0.5 and 1 are -5.4, -9, and -6.52, respectively. The critical values are ±1.645, ±1.96 and ±2.326 at the 10%, 5% and 1% levels of significance, respectively.

15 We also use the t-test in comparing if the coefficients of regime 3 are significantly different from the weights of 1.5, 0.5 and 1 of the Taylor rule. For regime 3 versus Taylor rule regime of Table 2, the t-statistics for the inflation forecast coefficient, the output gap coefficient and the constant compared with 1.5, 0.5, and 1 are 0.125, -4.58 and 2.08, respectively. For regime 3 versus Taylor rule regime of Table 3, the t-statistics for the inflation coefficient, the output gap coefficient and the constant compared with 1.5, 0.5 and 1 are 0.76, -5.8 and 1.93, respectively. The critical values are ±1.645, ±1.96 and ±2.326 at the 10%, 5% and 1% levels of significance, respectively.

16 From Figure 1 and Table 2, the implied rates of the lower discretionary regime from 2009Q1 to 2014Q1 are -0.44, -0.55, -0.58, -0.45, -0.28, -0.09, -0.22, -0.12, -0.08, 0.15, 0.18, 0.11, 0.23, 0.47, 0.30, 0.41, 0.38, 0.44, 0.38, 0.47 and 0.43 with a standard error of 0.63 and the implied rates of the Taylor rule are 0.66, -0.43, -0.65, -0.42, -0.07, 0.22, 0.14, 0.31, 0.58, 0.30, 0.38, 0.30, 0.89, 1.16, 0.95, 1.02, 0.98, 1.29, 1.38, 1.70 and 1.47 with a standard error of 0.69. From Figure 2 and Table 3, the implied rates of the lower discretionary regime from 2009 Q1 to 2010 Q2 are 0.22, -0.25, -0.56, -0.35, -0.06, 0.17, 0.00, 0.20, 0.14, 0.25, 0.33, 0.29, 0.28, 0.51, 0.36, 0.44, 0.50, 0.54, 0.55, 0.73 and 0.61 with a standard error of 0.57 and the implied rates of the Taylor rule are 1.31, 0.30, -0.30, 0.05, 0.50, 0.83, 0.61, 0.93, 0.86,
0.80, 0.93, 0.90, 0.92, 1.21, 1.02, 1.10, 1.23, 1.32, 1.41, 1.73, 1.49 with a standard error of 0.74.
REFERENCES


### Table 1: Maximized log-likelihood and Schwarz criterion

<table>
<thead>
<tr>
<th>k</th>
<th>Maximised log-likelihood</th>
<th>Schwarz criterion</th>
<th>k</th>
<th>Maximised log-likelihood</th>
<th>Schwarz criterion</th>
</tr>
</thead>
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<tr>
<td>1</td>
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<td>732.6</td>
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<td>-351.5</td>
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<td>2</td>
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<td>-294.3</td>
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<tr>
<td>3</td>
<td>-214.3</td>
<td><strong>504.9</strong></td>
<td>3</td>
<td>-214.1</td>
<td><strong>504.6</strong></td>
</tr>
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<td>4</td>
<td>-208.0</td>
<td>543.3</td>
<td>4</td>
<td>-200.3</td>
<td>528.0</td>
</tr>
</tbody>
</table>

Notes: ‘quadratic’ in ‘Real time quadratic output gap’ refers to the use of the quadratic trend in the calculation of the output gap which is percent deviation of the actual real time GDP from the quadratic trend. ‘Quad+GB+CBO’ refers to the output gap from quadratic trend estimates (1965Q4 – 1986Q4), from the Greenbook (GB) (1987Q1 – 2007Q4) and from Congressional Budget Office (CBO) potential output estimates (2008Q1-2014Q1).

### Table 2: Parameter estimates and standard errors (in brackets) for the three-state Markov regime switching model (Sample period: 1973Q3 – 2014Q1)

<table>
<thead>
<tr>
<th>Variable (real-time data)</th>
<th>Regime 1 (Taylor rule)</th>
<th>Regime 2 (low discretionary regime)</th>
<th>Regime 3 (high discretionary regime)</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Constant</td>
<td>1</td>
<td>-0.34 (0.15)</td>
<td>3.14 (1.03)</td>
</tr>
<tr>
<td>GDP deflator Inflation forecast</td>
<td>1.5</td>
<td>1.21 (0.03)</td>
<td>1.52 (0.17)</td>
</tr>
<tr>
<td>Real time quadratic output gap</td>
<td>0.5</td>
<td>0.27 (0.02)</td>
<td>-0.05 (0.12)</td>
</tr>
<tr>
<td>$\sigma_j^2$</td>
<td>0.48 (0.11)</td>
<td>0.40 (0.07)</td>
<td>1.69 (0.79)</td>
</tr>
<tr>
<td>$p_{1j}$</td>
<td>0.92</td>
<td>0.08</td>
<td>0.00</td>
</tr>
<tr>
<td>$p_{2j}$</td>
<td>0.05</td>
<td>0.94</td>
<td>0.01</td>
</tr>
<tr>
<td>$p_{3j}$</td>
<td>0.04</td>
<td>0.00</td>
<td>0.96</td>
</tr>
</tbody>
</table>

**Average variability for a regime**

<p>| | | | |</p>
<table>
<thead>
<tr>
<th></th>
<th></th>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>CPI inflation variability</td>
<td>0.348</td>
<td>0.819</td>
<td>0.935</td>
</tr>
<tr>
<td>GDP deflator inflation variability</td>
<td>0.101</td>
<td>0.202</td>
<td>0.266</td>
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<tr>
<td>Real GDP variability</td>
<td>0.938</td>
<td>1.037</td>
<td>1.852</td>
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</table>

***, **, * indicate 1%, 5% and 10% levels of significance respectively. ‘quadratic’ in ‘Real time quadratic output gap’ refers to the use of the quadratic trend in the calculation of the output gap which is percent deviation of the actual real time GDP from the quadratic trend. GDP deflator inflation forecast data are from the Greenbook (1973Q3-1987Q4) and Survey of Professional forecasters (1988Q1-2014Q1). Data until 2010Q2 are downloaded from https://sites.google.com/site/alexrzhevskyy/files/data_rules_discretion.zip. We extend to 2014 the data on inflation forecast using data from the Survey Professional Forecaster (SPF) and the data on real time quadratic output gap using data on real time GDP calculated following Nikolosko-Rzhevskyy, Papell and Prodan (2013). SPF and real time GDP data are from the Federal Reserve Bank of Philadelphia website. Quarterly CPI inflation, GDP deflator inflation and real GDP data are obtained from the International Financial Statistics.
Table 3: Parameter estimates and standard errors (in brackets) for the three-state Markov regime switching model (Sample period: 1973Q3 – 2014Q1)

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<tr>
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<th>Regime 3 (high discretionary regime)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Constant</td>
<td>1</td>
<td>-1.22***</td>
<td>2.39***</td>
</tr>
<tr>
<td>GDP deflator Inflation</td>
<td>1.5</td>
<td>1.27***</td>
<td>1.60***</td>
</tr>
<tr>
<td>forecast</td>
<td>(0.34)</td>
<td>(0.05)</td>
<td>(0.13)</td>
</tr>
<tr>
<td>Output gap</td>
<td>0.5</td>
<td>0.14**</td>
<td>-0.08</td>
</tr>
<tr>
<td>(Quad+GB+CBO)</td>
<td></td>
<td>(0.04)</td>
<td>(0.10)</td>
</tr>
<tr>
<td>$\sigma_j^2$</td>
<td>0.55***</td>
<td>0.33***</td>
<td>1.57***</td>
</tr>
<tr>
<td></td>
<td>(0.09)</td>
<td>(0.08)</td>
<td>(0.50)</td>
</tr>
<tr>
<td>$p_{1j}$</td>
<td>0.96</td>
<td>0.04</td>
<td>0.00</td>
</tr>
<tr>
<td>$p_{2j}$</td>
<td>0.03</td>
<td>0.95</td>
<td>0.02</td>
</tr>
<tr>
<td>$p_{3j}$</td>
<td>0.03</td>
<td>0.00</td>
<td>0.97</td>
</tr>
</tbody>
</table>

Average variability for a regime

<table>
<thead>
<tr>
<th></th>
<th>Regime 1</th>
<th>Regime 2</th>
<th>Regime 3</th>
</tr>
</thead>
<tbody>
<tr>
<td>CPI inflation variability</td>
<td>0.299</td>
<td>1.178</td>
<td>0.781</td>
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<tr>
<td>GDP deflator inflation variability</td>
<td>0.091</td>
<td>0.292</td>
<td>0.203</td>
</tr>
<tr>
<td>Real GDP variability</td>
<td>0.821</td>
<td>1.297</td>
<td>1.575</td>
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***, **, * indicate 1%, 5% and 10% levels of significance respectively. ‘Quad+GB+CBO’ refers to the output gap from quadratic trend estimates (1965Q4–1986Q4), from the Greenbook (GB) (1987Q1–2007Q4) and from Congressional Budget Office (CBO) potential output estimates (2008Q1-2010Q2). GDP deflator inflation forecast data are from the Greenbook (1973Q3-1987Q4) and Survey of Professional forecasters (1988Q1-2014Q4). Data until 2010Q2 are downloaded from https://sites.google.com/site/alexrzhevskyy/files/data_rules_discretion.zip. We extend to 2014 the data on inflation forecast using data from the Survey Professional Forecaster (SPF) and the data on real time ‘quadric+Greenbook+CBO’ output gap, using data on potential real GDP from the Congressional Budget Office (CBO) website and real time GDP from the Federal Reserve Bank of Philadelphia website, calculated following Nikolosko-Rzhevskyy and Papell (2013). Quarterly CPI inflation, GDP deflator inflation and real GDP data are obtained from the International Financial Statistics.
Figure 1 - Conditional means and fund rate based on three-Markov regime switching model (real time GDP deflator Inflation forecast and real time quadratic output gap)
Figure 2 - Conditional means on three-state Markov regime switching model
(inflation forecast from Greenbook & SPF and output gap from quadratic trend, Greenbook & CBO)
Figure 3: Output gaps

- Real-time Quadratic Gap
- Real-time Output Gap (Quadratic & GreenBook & CBO) t-1/t