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Circuit and System Design for Optimal Lightweight AES Encryption on FPGA

Ming Ming Wong, M. L. Dennis Wong, Cishen Zhang and Ismat Hijazin

Abstract—The substitution box (or commonly termed as S-Box) is a non-linear transformation, and known as the bottleneck of the overall operation in AES cipher. Due to recent emergence of high performance and lightweight applications, the required optimum AES cipher has to be both hardware cost effective and computationally efficient. In this study, we implemented various S-box architectures in AES encryption in order to perform an in-depth hardware analysis on FPGA platform. These architectures are the hard-coded LUT S-box, the pure combinatorial S-box using composite field arithmetic (CFA), the pipelined version of CFA S-Box, the CFA AES S-box using direct computation and Linear Feedback Shift Register (LFSR) based S-Box. As a result, a total of six AES ciphers with different S-box architectures are synthesized and implemented on FPGA platform. Considering both the hardware size (total Logic Elements (LE)) as well as the performance (throughput (Mbps)) the optimum AES cipher implementation is derived in this work. The presented implementation is proven lower in hardware area occupancy and higher in computational speed compared to the existing works.

Index Terms—Advanced Encryption Standard (AES), AES S-box, Lightweight Cipher, Composite Field Arithmetic (CFA), Pipeline, Linear Feedback Shift Register (LFSR).

I. INTRODUCTION

EVOLUTION of ubiquitous computing has led to the rise of Internet of things since the early twentieth century. As a result, large amount of digital data are constantly exchanged between various embedded devices over the internet. Therefore, ciphers are widely used to ensure the security of these digital data [1]–[3].

In November 2001, National Institute of Standards and Technology (NIST) has chosen Rijndael block cipher as the Advanced Encryption Standard (AES) [4]. Since then, AES has gradually replaced the Data Encryption Standard (DES) and eventually becoming one of the most preferred symmetric cryptographic protocols. Due to its increasing popularity in area-constrained applications, such as the embedded systems, the need of compact AES cipher implementation became more important than ever before [5], [6]. Later, the advent of NFC has redefined the optimality of AES cipher in lightweight applications. These features are not only small in hardware size but also fast in speed performance.

Among the four key AES operations, the SubBytes transformation (S-box) is recognized as the bottleneck of the entire AES encryption process. The transformation computes the most resource demanding multiplicative inversion operation in finite field arithmetic. To deal with the complex computation problem, various design techniques have been proposed in order to achieve low hardware cost (area and power consumptions) and high speed performance in AES S-box implementation. It is also noted that, optimization in the MixColumn transformation gained a considerable amount of research interest which is the second most resource consuming operation after SubBytes Transformation [7].

The focus of this paper is on the S-box design for AES cipher. In order to achieve the optimum features required in the recent lightweight applications, this work aims to design AES ciphers with the minimum hardware cost. This is achieved by a series of optimizations to reduce the critical path and hence enhance the speed performance.

The contribution of this work is twofold. First, it conducts a thorough design analysis and hardware review on different type of S-boxes. The S-boxes will be classified into several categories according to the nature of their architecture design. Furthermore, the Linear Feedback Shift Register (LFSR) based S-Box in AES cipher, which is relatively new in the research area is included in the implementation benchmarking analysis.

Second, the S-box selected from each category is adopted in full AES encryption and implemented on FPGA platform. The hardware AES cipher with various S-box designs is evaluated in terms of its hardware size and speed performance. Further optimization in algorithmic and architectural levels are employed in our the circuit design. Based on the synthesis and implementation results, the best AES cipher that is most suitable for lightweight applications is identified.

The remainder of this paper is organized as follows: Section II briefly the operations in the AES encryption process. Existing works in AES S-box hardware optimization methodologies are reviewed in Section III. The optimized S-box implementations adopted from our previous studies can be categorized into four different major designs which will be presented in Section IV. The FPGA implementations of AES cipher with various S-box architectures and their hardware analysis will be evaluated in Section V. Finally, the conclusion and future work are drawn in Section VI.

II. ADVANCED ENCRYPTION STANDARD (AES)

AES is a symmetric block cipher that process data blocks of 128-bits with different key lengths; 128, 192 and 256 bits and resulting in 10, 12 or 14 computation round respectively. Therefore, there are three AES variants based on the key-lengths which are namely the AES-128, AES-192 and AES-256. In this study, we focus only on encryption process of AES-128, which requires key lengths of 128-bits and 10 computation rounds.
The encryption begins by copying the input to an array, termed as State. The State is an array of 16 bytes arranged in four rows and four columns (4 x 4). Hence the transformations will be performed on each of the blocks of byte in the State, which are represented as finite field elements of \( GF(2^8) \) with the specified field polynomial \( q(x) = x^8 + x^4 + x^3 + x + 1 \). The initial key is then added to the input value in the initial round. Next, the consecutive identical 9 rounds take place and end with a slightly modified final round. The normal computation round (9 rounds) in AES consists of four transformations in the following orders; SubBytes, ShiftRows, MixColumns and AddRoundKey. The final round is the normal round without the MixColumns transformation.

Symmetry key cryptography such as the DES and AES ciphers utilizes a substitution box (S-box) to provide the substitution-permutation mechanism to achieve both diffusion and confusion properties in their block ciphers. For AES, the S-box is performed in the first transformation, i.e. SubBytes transformation which consists of two main operations. First, each of the data byte is substituted by its multiplicative inversion in \( GF(2^8) \) over the field polynomial, \( q(x) = x^8 + x^4 + x^3 + x + 1 \). The operation is relatively expensive in term of hardware and is therefore identified as the bottleneck in achieving compact and fast AES cipher implementation. Second, bit scrambling is performed using affine transformation over \( GF(2) \).

The second transformation, the ShiftRows transformation cyclically shifts each row of the State by certain offset. To be precise, while the first row remained unchanged, the second row is shifted by one, the third row by two and the fourth row by three bytes to the left. This computation is simple in hardware as no additional hardware is required for shifting. Unlike any other transformation, the third transformation, MixColumns transformation, processes one column of the State at a time. This transformation basically involves matrix multiplication. Each byte is interpreted as the coefficients of four-term polynomial over \( GF(2^4) \), the column is then multiplied with a fixed polynomial \( a(x) = \{03\}x^3 + \{01\}x^2 + \{01\}x + \{02\} \) and modulo \( x^4 + 1 \).

The fourth transformation, the AddRoundKey is a simple addition between the RoundKey and the 128-bit State. Note that the addition operation in finite field arithmetic is realized using logical gate XOR in hardware. The required RoundKey is generated from another operation, called the KeyExpansion. The KeyExpansion uses the initial key to generates all the 10 RoundKey that are required in every computation round in AES.

Further details of AES transformation are also available from the original source by Daemen and Rijmen in [8]. The algorithm structure is also as illustrated in Figure 1.

### III. LITERATURE REVIEW

As reviewed in Section II, in AES, the SubBytes transformation (S-box) involves the computation of the most resource consuming operation in finite field arithmetic, which is the multiplicative inversion. The conventional and the most straightforward implementation approach is by the means of hard-coded memory through LUT. The LUT contains the permutation of all 256 possible 8-bit values. Hence, the tedious computation in AES S-box is simplified for mapping each individual input byte to a new output byte through the table. Such implementation often results in high-speed circuitry but is very expensive in terms of the hardware cost as each of the LUT S-box requires 2,048 memory bits. Furthermore, in a high-speed design of AES-128 cipher, 16 parallel LUT S-box modules are needed for a single round.

Back in the early 20th century, with the rise of computers and Internet, cryptography algorithms began to play a vital role in several communication applications. Subsequently, dedicated hardware with high speed performance were needed to handle the complex computations in the ciphers. In order to fulfill these requirements, several efficient and high throughput AES hardware implementations were proposed such as that in [9]–[17].

The need of cryptography algorithms was then further extended to the resource-constrained applications due to the rapid emergence of lightweight embedded systems in the 21st century. Therefore, various area efficient implementations of AES S-boxes using composite field arithmetic (CFA) [18]–[20] were introduced.

These results derived equivalent computation in smaller fields such as \( GF((2^4)^2) \) [21]–[24] or \( GF(((2^2)^2)^2) \) [25]–[32].

On the other hand, the CFA approach generally results in complex circuitry with long critical path. This prevented efficient pipelining to be performed, leading to low performance in hardware implementation. In other words, there exists a significant trade-off between the hardware cost and the performance in CFA AES S-box implementation.
In addition to the pure combinatorial circuitry mentioned above, several other area efficient AES S-boxes that utilized dedicated Block RAMs available in FPGA platform were reported in [33]–[38]. However, these techniques may not be an attractive solution in terms of ASIC implementation.

Several other methodologies have been introduced in the literature to design low power AES hardware circuitry [39]–[43]. Among all these low-power techniques, the decoder-permute-encoder structure (Decoder Switch Encoder (DSE) architecture) proposed by Bertoni et al. consumed the least power for AES S-box implementation [43]. The structure of the circuit is short in critical path architecture and induces minimal signal activity within the circuit when the input changes. Though the design resulted in low power consumption, its size is about three times as large as that of the pure CFA work [44].

In recent years, a new approach using the maximum length Linear Feedback Shift Register (LFSR) to compute the multiplicative inversion has been investigated and implemented in the AES S-box. LFSR is often used in cryptographic implementations such as the hash functions, pseudorandom number generators (PRNGs) and stream ciphers. However, it is considerably new in block cipher implementation and is yet to be commonly applied to AES S-box in comparison to the CFA approach. To our best knowledge, LFSR based multiplicative inversion customized for AES cipher was only reported in [45]–[48]. These works managed to produce low hardware cost AES S-box comparable with that implemented using CFA approach.

In general, several different S-box architectures have been proposed in the literature in an attempt to optimize the non-linear transformation in AES cipher in terms of hardware size, speed and power consumption. With an aim of implementing a small hardware size AES cipher with high computation efficiency, our work shall focus on the CFA approach for S-box and followed by optimization works in algorithm and architectural levels. Meanwhile, the extended CFA AES S-boxes with various pipeline stages employed to minimize the long critical path in the complex circuits have been proposed in our previous studies [49]–[51]. With the shorter critical path (reduced due to the insertion of pipelines), our works effectively produces CFA AES S-box designs with higher speed performance and smaller dynamic power consumption at the cost of a slight increment in the hardware cost.

It is noted that, the detailed hardware analysis of the effectiveness and the efficiency of each S-box in AES cipher has not been evaluated in the literature. As an extension of our previous works, this study will therefore, benchmark the cost and the performance of various S-boxes in AES cipher implemented on FPGA platform.

IV. AES S-BOX DESIGNS

In this section, four different major designs of AES S-box will be discussed and evaluated in details. These are namely the pure composite field arithmetic (CFA) S-box (Section IV-A), the pipelined version of CFA S-box (Section IV-B), S-box using direct computation (Section IV-C) and linear feedback shift register (LFSR) based S-box (Section IV-D).

A. Composite Field Arithmetic (CFA) AES S-box

As opposed to the conventional method that utilized LUT, Rijmen [52] was the first to propose an alternative solution by employing CFA [18]–[20], [53] to compute the multiplicative inversion over $GF((2^8)^8)$ in AES S-box. In CFA, finite field elements are represented in its equivalent composite field, i.e $GF((2^8)^8) \equiv GF((2^{8n})^8)$, where $l = n\cdot i$. The composite field is built iteratively from its lower order fields, allowing the actual mathematical manipulation to be performed in the lower fields instead of its original higher field order. Subsequently, in AES S-box, the element in $GF((2^8)^8)$ can be mapped to its subfield and this will yield less complexity in the multiplicative inverse. The following summarizes the steps in performing multiplicative inversion using CFA:

1) Map all elements of field $A$ to a composite field $B$ using isomorphism function; $b = f(a) = \delta \times a$.
2) Compute the multiplicative inverse over $B$, $x = b^{-1}$ (except if $b = 0$, then $x = 0$).
3) Remap the computation results to $A$, using the inverse isomorphism function; $a = f(x) = \delta^{-1} \times x$.

Complexity of a field is heavily dependent on several factors: field of mapping, representations of the field elements, (i.e. field polynomials and the basis representations used) and isomorphic mapping chosen for the representation. Thus, one can conveniently take the advantage of the isomorphism to map a computation from one field to another to search for the most efficient implementation. Mapping the finite field from $GF(2^8)$ to $GF(((2^2)^2)^2)$ requires three stages of isomorphism and field polynomials which are listed (in a general form) below:

\[
\begin{align*}
    r(y) &= \ y^2 + \tau y + \nu \\
    \text{(isomorphism for } GF((2^8)/GF(2^4)) \text{)} &\quad (1) \\
    s(z) &= \ z^2 + Tz + n \\
    \text{(isomorphism for } GF((2^4)/GF(2^8)) \text{)} &\quad (2) \\
    t(w) &= \ w^2 + w + 1 \\
    \text{(isomorphism for } GF(2^8)/GF(2) \text{)} &\quad (3)
\end{align*}
\]

Generally, multiplicative inverse over the composite field $GF(((2^2)^2)^2)$ can be performed with respect to either polynomial basis or normal basis. The computations are also determined by the coefficients of their respective field polynomials; (1), (2) and (3). Hence, the coefficients in the field polynomials have a direct influence towards the computation complexity. As $w^2 + w + 1 = 0$ is the only irreducible polynomial of degree 2 over $GF(2)$, there is no other candidate coefficient for (3). For (1) and (2), there are several possible coefficients of $\nu, \tau, N$ and $T$ in both normal and polynomial bases. In order to promote simplicity in CFA, one could either have the trace or the norm of $r(y)$ and $s(z)$ equal to unity but not both.

To our best knowledge, most studies such as reported in [23], [25], [26], [28], [31], [52], [54] attempted the optimization with traces of field polynomials equal to unity using polynomial basis representation. Similar case reported in [27] used normal basis representation instead. On the other hand, our previous works have chosen the norms ($\nu$ and $N$) of the field polynomials to be unity for both polynomial
and normal bases [29], [30]. As a result, three CFA S-box constructions (listed as below) were derived. Theoretical and empirical results showed that Case C (see Figure 2) successfully strikes a balance between the total number of gate counts (area) and its respective critical path (speed) in comparison with the conventional CFA selections reported in [25]–[28], [54].

1) Case A: Using polynomial basis representation with field polynomials’ norms equal to unity (both $\nu$ and $N$ in (1) and (2) equal to unity).

2) Case B: Using normal basis representation with field polynomials’ norms equal to unity (both $\nu$ and $N$ in (1) and (2) equal to unity).

3) Case C: Using normal basis representation with $\tau$ in (1) and $N$ in (2) equal to unity.

Due to its promising implementation results, the S-box from Case C is chosen to be deployed in AES encryption. The implementation and the in-depth hardware evaluation of the cipher on FPGA platform will be presented in details in Section V. Meanwhile, further optimizations in architectural and algorithmic levels are presented next in Section IV-B and Section IV-C respectively.

### B. Pipelined CFA AES S-box

CFA offers an effective solution to deduce a pure combinatorial AES S-box using the composite field $GF((2^4)^2)$. Without the need of LUT, the mathematical manipulations can be performed through three isomorphism levels, involving several complex sub-operations modules of different complexities. For this reason, several studies have also verified that the resultant circuit tends to have relatively long critical path [55]. Besides such a complex signal path, the circuit might produce massive dynamic hazards propagation and lead to high power dissipation. In order to curb the problems, our previous works in [49], [50] have attempted to equalize the amount of signal transitions within every clock cycle. This can be done by careful placement of pipelines in the circuit such that the signal arrival times from each parallel path is consistent.

Due to the complicated crossing and branching in the composite field S-box, pipelining alone is insufficient to ensure complete consistency within the circuit. Therefore, prior to pipelining, pre-processing procedure is required i.e. to convert the complicated circuit into several logical expressions without altering the functionality of the original circuit. The computation is expressed using the Algebraic Normal Form (ANF), consisting of only AND gates and XOR gates. Hence the sub-operations which include the 4-bit adders, square-scaler, $GF(2^4)$ multiplier and $GF(2^4)$ inverter (refer to Figure 2) will be first translated into ANF expressions. Next, these sub-operations are merged to form three main computation modules in $GF(2^8)$ inversion circuit, together with isomorphism and inverse isomorphism plus affine transformation respectively. All the five ANF modules in the AES S-box are listed in the following.

1) Isomorphism
2) Two 4-bit adders, a square-scaler and a $GF(2^4)$ multiplier.
3) $GF(2^4)$ inverter
4) Two $GF(2^4)$ multipliers
5) Inverse isomorphism plus affine transformation

With the operations in the $GF(2^8)$ multiplicative inverter is derived using pure logic equations, pipelines can be applied at ease in the next step. Note that the position and the number of the pipeline will effect the overall hardware cost and speed performance. One of the earlier works that attempted 3-stage pipelining was reported in [55]. On the other hand, our work in [49] employed 7-stage pipelining; with one pipeline stage for each ANF modules and additional sub-pipelines in both of the $GF(2^4)$ multipliers. The aim of the sub-pipelining is to further shorten the critical path in the multiplier. Based on the hardware analysis in Table I, the design results in high performance and also increase in the number of hardware resources.

In a separate work, another compact and well-transformed three-level isomorphism CFA S-box was reported in [50]. The work presented a highly modular design, which allows efficient 5-stage pipelining. Not only that, the logic equations were arranged in tree structures that the common factors can be eliminated using subsharing factorization. The block diagram for the pipelined CFA AES S-box presented in [49], [50], [55] are as illustrated in Figure 3. Table I shows the comparison in terms of the hardware requirements and performance for three AES S-box designs on Cyclone III EP3C5F256C6 device.

Based on the hardware results, the works in [49], [55] require 24 pipeline registers for 3-stage pipelining and 90 pipeline registers for 7-stage pipelining respectively. On the other hand, the work in [50] only requires 36 pipeline registers for 5-stage pipelining. Not only that, its speed performance is comparable with the circuit in [49] but also has considerably lower power dissipation. Hence, it can be concluded that S-box in [50] is a better selection in term of the hardware cost and performance efficiency.

### C. Direct Computation CFA AES S-box

As discussed in the previous section, the exploitation of pipelining is capable of altering the hardware cost and the performance of the CFA AES S-box. A separate study reported in [51] has applied direct computation to produce an alternative architecture that further extend the benefits of pipelining in CFA AES S-box design. The work derived three main computational modules which are namely the adder (4-bit XOR) and the square-scaler $\nu^2$ (labeled as M1), $GF(2^4)$ multiplier (labeled as M2) and $GF(2^4)$ inverter (labeled as M3), which are shown in Figure 4. In the first step of the algorithmic optimizations, the computational modules (M1, M2 and M3) are merged and reduced into new boolean modules; P1(square-scaler merged with multiplier), P2 and P3(inverter merged with multiplier). The block diagram of the resultant circuit is as shown in Figure 4. The new $GF(2^8)$ inverter is now comprised of only three modules; P1, P2 and P3, with several repetitive common sub-expressions in their boolean functions.

1) Module P1: Modules M1 (adder and square-scaler) and M2 ($GF(2^4)$ multiplier) are merged to produce a new module, P1. The derivation of the new module P1 is expressed in boolean functions with respect to input $\gamma_1 = \{a, b, c, d\}$ and $\gamma_0 = \{x, y, w, z\}$. 

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Fig. 2. Multiplicative Inverse over Field $GF(2^8)$

Fig. 3. Pipelined CFA AES S-box
γ to the input cost reduction. The common sub-expressions with respect individual operator are factorized and eliminated for further bits (the tap position, determined by primitive polynomial) high potential in achieving low hardware cost. LFSR uses much logical gates, the approach is simple and exhibits pure combinatorial circuitry. However, without requiring D. Linear Feedback Shift Register Based AES S-box in details in Section V.

--- | --- | --- | ---
Total LE (5136 LEs) | 95 | 71 | 66
Combinational Functions (5136 LEs) | 75 | 68 | 66
Dedicated Logic Registers (5136 LEs) | 90 | 24 | 36
Total Register (5136 LEs) | 90 | 32 | 36
Fmax (MHz) | 380.66 | 170.44 | 346.26
Dynamic Thermal Power Dissipation (mW) | 2.26 | 0.15 | 1.84

2 Module P2: Module P2 is a result of combining modules M2 (GF(2^4) multiplier) and M3 (GF(2^4) inverter). Its boolean functions are expressed as functions of input \( \gamma_0 = \{x, y, w, z\} \) and the output from module P1, \( P_1 = \{k, l, m, n\} \). It is noted that the input \( \gamma_0 \) is obtained from the four least significant bits of the input to the \( GF(2^8) \) finite field inverter, as shown in Figure 4. The output of P2 will serve as the four most significant bits of the output of \( GF(2^8) \) finite field inverter, \( \delta_1 \).

3 Module P3: Similar to module P2, module P3 is a combination of module M2 (GF(2^8) multiplier) and module M3 (GF(2^8) inverter), with a different set of input data. For module P3, the respective inputs are \( \gamma_1 = \{a, b, c, d\} \), which are the four most significant bits of the input to the \( GF(2^8) \) finite field inverter (refer in Figure 4) and the output from module P1, \( P_1 = \{k, l, m, n\} \). Meanwhile, the output of P3 will serve as the four least significant bits of the output of \( GF(2^8) \) finite field inverter, notated as \( \delta_0 \).

Next, the common sub-expressions identified from each individual operator are factorized and eliminated for further cost reduction. The common sub-expressions with respect to the input \( \gamma = \{i, j, \gamma_0\} \) and the output from module P1 are as depicted in Figure 5. Effective elimination of these common sub-expressions promotes significant amount of resource sharing and hence leads to efficient computational cost reduction. The mathematical deductions of all the modules M1, M2 and M3 as well as P1, P2 and P3 can be found in details in the original paper [51].

As an extension of the above-mentioned work in [51], 4-stage pipelining is further employed in the design. In this study, the newly derived S-box, together with work from [49] and [50] (discussed in Section IV-B) are also implemented in AES cipher. These implementations and their in-depth hardware evaluations on FPGA platform will be presented in details in Section V.

D. Linear Feedback Shift Register Based AES S-box

In recent years, cryptographic researchers have considered the feasibility of deploying the Linear Feedback Shift Register (LFSR) to perform the multiplicative inversion in the AES S-box. Unlike CFA, the approach is unable to achieve pure combinatorial circuitry. However, without requiring much logical gates, the approach is simple and exhibits high potential in achieving low hardware cost. LFSR uses registers (or flip flops), simple XOR operation of particular bits (the tap position, determined by primitive polynomial) and a shifting operation to generate a collection of cyclic binary states. LFSR updates the current state through direct computation of its predecessor.

In mathematical sense, LFSR transformation at any \( p \) cycle is performed as \( S(t+p) = TP \cdot S(t) \) where \( T \) is the LFSR transformation matrix, \( S(t) \) is the state of the LFSR at the \( t^{th} \) instant time or the initial seed and \( S(t+1) \) is the state of the LFSR at \( (t+1)^{th} \) time instant, i.e. the next clock cycle [46], [47]. With that, multiplicative inversion can be computed with LFSR running with a particular initial seed until the LFSR state matches the given input and the total number of clock cycles lapse is recorded. Next, the LFSR is re-initiated with the same initial seed and continues to run for the remaining cycles. The total number of cycles in both runs ought to be 255 (for the 8-bit element). Upon arriving at this point, the LFSR will then produce the multiplicative inverses of the given input.

Alternatively, our previous study (in [48]) has proposed a different LFSR based multiplicative inverter that is comprised of two identical 8-bit LFSRs and constructed using primitive polynomial \( \{x^8 + x^4 + x^3 + x^2 + 1\} \). There are three non-zero feedback taps, with each implemented using XOR gate. Both LFSRs are loaded with the initial seed (or initial state) \( \{00000001\}_2 \) and run in parallel but in opposite directions; forward and reverse. With the initial state notated as \( S(t) \), the forward LFSR will run continuously in \( S(t+i) \) direction, and the reverse LFSR will run simultaneously in \( S(t+255−i) \) direction with \( i \in \{1, 2, 3...127\} \). Within \( i \) clock cycles, when the input matches the current state in either LFSR, the current state of the other LFSR will be the corresponding multiplicative inverse. The block diagram of our LFSR based AES S-box is as depicted in Figure 6.

Sourav Das has also presented two new designs for LFSR based multiplicative inversion that are also applicable to AES S-box hardware implementation [46], [47]. In their work, only one set of 8-bit LFSR is used, which is however constructed using 2-input FFs for reloading is required in their methodology. In order to speed up the overall performance, the computation is split into several stages and a complex mapping function is involved to maneuver the entire procedure.

On the contrary, our work in [48] uses two parallel 8-bit LFSRs. Each of them is constructed using 1-input FFs and hence is smaller in size. Moreover, the need of mapping function is not required. Therefore, the work is implemented in AES encryption for further investigation. The feasibility of LFSR based S-box in comparison to the commonly deployed CFA S-box in AES cipher will be analyzed and evaluated in terms of their hardware size and performance. These will be reported in Section V.

However, as LFSR based stream cipher are susceptible towards cache timing attack, there are chances that the proposed LFSR based S-box may cause vulnerability of the
Fig. 4. (a) $GF(2^8)$ finite field inverter with its inner modules denoted as M1, M2 and M3. The inner modules are defined over finite field $GF(2^4)$. (b) Block diagram of the proposed $GF(2^8)$ finite field inverter after merging.

Fig. 5. (a) Common sub-expressions with respect to the input $\gamma; \gamma_1 = \{a, b, c, d\}$ and $\gamma_0 = \{x, y, w, z\}$. (b) Common sub-expressions with respect to the output from module $P1 = \{k, l, m, n\}$.
cipher towards the side-channel attack as well.

V. AES CIPHER IMPLEMENTATIONS AND RESULTS

Various AES S-box architectures presented in previous sections are implemented in full AES cipher in order to search for the smallest hardware area occupancy AES with optimum speed performance. These include the S-box realized using LUT (pure hard-coded memory), pure combinatorial circuit through CFA, enhanced version of CFA AES S-box with different number of pipelining stages and followed by algorithmic optimization, as well as the LFSR based implementation.

As a result, a total of six implementations of AES cipher with different S-box architectures (Case I-VI) listed in the following are presented in this section. Furthermore, for fair benchmarking among the various S-box designs, all the other transformation rounds (ShiftRow, MixedColumn, AddRoundKey and KeyExpansion) shall remain unchanged for all implementations.

1) Case I: LUT-based AES S-box
2) Case II: CFA AES S-box [29]
3) Case III: 7-stage pipelined CFA AES S-box [49]
4) Case IV: 5-stage pipelined CFA AES S-box [50]
5) Case V: 4-stage pipelined CFA AES S-box [51]
6) Case VI: LFSR-based AES S-box [48]

These AES ciphers are implemented in Cyclone IVE EP4CE30F29C6 using Quartus II 11.1. Having the architectures clocked at 250MHz, 125MHz and 100MHz, the timing analysis of the architectures are deduced using TimeQuest Timing Analyzer. Table II presents the comparison in terms of the hardware requirements and performance specifications of these six implementations.

The results in Table II reflected that AES cipher in Case I requires the least LE but large hard-coded ROM for the LUT-based S-box. In terms of speed analysis, the result further showed that architectural optimization (pipelining) in CFA AES S-box (in Cases III-V) has effectively enhanced the speed performance of the overall AES cipher implementation.

It can be seen that, pipelining is indeed an effective measure to reduce the critical paths in the complicated CFA S-box circuitry. Note that additional pipeline may contribute to an increase in hardware occupancy. For instance, the cipher has an increase of 5.4% and 5.9% of total LE in Case III and Case IV respectively compared to the pure CFA AES S-box in Case II. However, the effect can be minimized with proper planning during pipeline placement (refer Section IV-B) as well as algorithmic optimizations employed in design (refer Section IV-C). This is proven in Case V where the 4-stage pipelined AES S-box resulted in a reduction of implementation size by 23.7% in the AES cipher.

Among all the cases presented, the AES cipher in Case V strikes a balance in hardware area and performance efficiency. The architecture has the smallest number of LE and its resultant speed performance is better than the pure combinatorial counterpart. It is therefore a suitable candidate for compact AES cipher implementation with high performance.

For detailed verification, the derived best case (AES cipher in Case V) is benchmarked with the related works reported in recent literature and the comparisons are as summarized in Table III. The synthesis results show that our implementation uses a total of 2059 LEs (no LUTs required) and has a throughput of 575 Mbps. The works presented by Chodowiec...
et al. in [33] and McMillan et al. in [38] utilized minimal amount of LEs (a total of 444 LEs and 480 LEs) but both architectures utilized hard-coded memory blocks with 12,288 bits and 32,768 bits respectively.

Another architecture reported in [56] Case A required 1818 LEs without involving LUTs. However, our architecture is able to achieve approximately 3 times the throughput performance with just a slight addition of LEs. Various pipelined architectures were proposed in [34], [35], [37], [56] in order to achieve throughput enhancement. It is worth noting that our implementations performance level is on par with the architectures presented in [56] Case C and [34] but with much smaller hardware circuit.

The above results can verify that our proposed work is able to meet the stringent requirement of lightweight implementation of AES cipher in terms of the low hardware area occupancy. Furthermore, our compact cipher also offers high throughput performance, which is also highly demanded in lightweight applications.

VI. CONCLUSION AND FUTURE WORK

This study presented a detailed overview of the various design of AES S-boxes, which are classified as the hard-coded LUT S-box, the pure combinatorial S-box using composite field arithmetic (CFA), the pipelined version of CFA S-Box, the AES S-box using direct computation and Linear Feedback Shift Register (LFSR) based S-Box. As a result, using various S-box architectures, six full AES cipher (Case I-VI) implementations on FPGA were derived and evaluated in details in terms of hardware cost and speed performance. Based on the synthesis result, the AES encryption from Case V, which employed both architectural and algorithmic optimization, was proven to have low hardware area occupancy and high computational speed. Thus, it is able to fulfill the demand of optimum lightweight cipher for high speed and area-constrained applications.

For future work, we shall look deeper into the algorithmic optimization in the finite field sub-circuit. The recent work reported by Ueno et. al has proven that finite field arithmetic using different field and basis representations will have a great impact in the computation gate counts and its critical path [21]. In addition, another work by Boyar et al. has presented a new technique for combinatorial logic optimization which effectively simplifies the operations in the subfield \(GF(2^4)\). Referring to these results, we shall extend our work by employing computation optimization in \(GF(2^4)\) inversion and multiplications in order to achieve further hardware cost reduction.

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