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<td>Author(s)</td>
<td>Ma, Kaixue; Ma, Jianguo; Yeo, Kiat Seng; Do, Manh Anh</td>
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A Compact Size Coupling Controllable Filter With Separate Electric and Magnetic Coupling Paths

Kaixue Ma, Member, IEEE, Jian-Guo Ma, Senior Member, IEEE, Kiat Seng Yeo, and Manh Anh Do

Abstract—This paper presents the characteristics of a miniaturized microstrip filter, which has two separate coupling paths: electric coupling path and magnetic coupling path between two resonators. Either magnetic coupling or electric coupling in two paths can be dominant in the total coupling coefficient of the inter-stage resonators with the similar configuration, but different positions of transmission zero points (ZPs). Based on the proposed filter topology, second- and fourth-order filters have been designed and fabricated for the first time. Advantages of using this type of filter are not only its low insertion loss and much more compact size, but also its controllable transmission ZPs.

Index Terms—Bandpass filter (BPF), odd and even mode, separate electric and magnetic coupling paths (SEMCPs), zero point (ZP).

I. INTRODUCTION

A S ONE of the key components in RF front-ends, filters with compact size, good performance, and low cost are highly demanded. Planar filters have great advantages over other types as regards these aspects and, thus, draw much attention. In order to reduce the size of the planar filter without sacrificing performance, many techniques have been reported in the literature (e.g., see [1]–[13]). For instance, instead of using a dual-mode half-wavelength resonator [1]–[4] or ring resonator [5]–[7], a quarter-wavelength resonator has been used [9]–[13], which can also provide a wider stopband.

It is desirable to design a filters in which extra transmission zero points (ZPs) can be generated without sacrificing the passband response [8], [13], [14]. For example, the extra ZPs of the filter can be adjusted to reject possible interferences and to improve stopband rejection. Thus, a low-order filter with the help of extra ZPs can meet the stopband requirements that are usually achieved by high-order filters. It is also known that the lower order filters generally have smaller sizes and lower insertion loss compared with the high-order filters. To generate more expected ZPs, the coupling mechanism must be investigated clearly. There are many papers in the literature that have paid attention to the coupling mechanism. Source–load coupling or cross-coupled topologies of elliptical filters are widely adopted [8], [11], [13]. The general coupling matrix is used to represent the coupling relationship for filter synthesizing [15]–[18], [21]. It can be seen that only one coupling parameter exists between any two adjacent resonators in the coupling matrix. For the inter-stage coupling of the quarter-wavelength filter, the inter-stage coupling in these reports can be classified as electric coupling, magnetic coupling, or mixed coupling (both electric and magnetic coexist, but cannot be separated in space due to distributed effects). The inter-stage coupling of most reported quarter-wavelength filters has one physical coupling path with one of these three coupling types between two adjacent resonators. The filters in [20] achieved good performances by using a suspended stripline quarter-wavelength stepped-impedance resonator (SIR) and generating additional ZPs by coexisted the electric and magnetic coupling.

In this paper, a filter topology and configuration (see Fig. 1), which provide two controllable separate electric and magnetic coupling paths (SEMCPs), are proposed. The characteristics of the microstrip filters, based on the SEMCP configuration using modified uniform quarter-wavelength resonators, have been investigated theoretically and experimentally. The size reduction, frequency-dependent coupling canceling, and additional ZP generation are demonstrated. The filters, with additional ZPs in low, upper stopband, or both, corresponding to electric, magnetic, or both dominant conditions, have been designed. The general topology and configuration of high-order filter are also given.

This paper is arranged as follows. In Section II, the SEMCP configuration by using lump coupling loading and topology are introduced. Odd- and even-mode analysis is used to investigate the coupling characteristics, external quality factors and transmission responses. In Section III, second-order bandpass filters
(BPFs) with distributed SEMCPs are characterized, designed, and verified by the experiment. In Section IV, the high-order SEMCP filter topology is proposed and a fourth-order BPF with a distributed loading SEMCP is designed and fabricated. A conclusion is given in Section V.

II. ANALYSIS OF FILTERS WITH SEMCP

Fig. 1(a) shows the configuration of a second-order SEMCP filter loaded with lump coupling elements ($L_m$ and $C_m$). Two sections of transmission lines are connected in series by a lump capacitor $C_m$, which is called an electric coupling path. Meanwhile, a lump inductor $L_m$ is shunted along the other two ends of two transmission lines, which is called a magnetic coupling path. The coupling relationships and resonators are illustrated in the filter topology of Fig. 1(b). As in Fig. 1(a), the I/O ports and physical structure are symmetrical with respect to the reference plane $AA'$. An odd- and even-mode analysis [22] is adopted to analyze this structure. From the mechanism of the resonator resonance, the structure is resonant when its input admittance is zero for both the even and odd modes, i.e.,

$$Y_{even} = Y_{odd} = 0. \tag{1}$$

For the even-mode case, the equivalent-circuit representation of the resonator when the magnetic wall is applied at the $AA'$ plane is demonstrated in Fig. 2(a). The even-mode input admittance is derived as

$$Y_{even} = jY_c \left[ \frac{2\omega_c L_m Y_c \tan \beta l_2 - 1}{2Y_c \omega_c L_m + \tan \beta l_2} \right]. \tag{2}$$

where $\beta_c$ is the propagation constant at the even-mode resonance angular frequency $\omega_c$, and $Z_c = 1/Y_c$ is the characteristic impedance of the resonator.

Using (1) and (2), we have

$$\frac{2L_m \omega_c}{Z_c} = \frac{1}{\tan \beta_c (l_1 + l_2)}, \tag{3}$$

For a small $L_m$, $l_1 + l_2 \approx \lambda_0/4$, the right-hand side of (3) can be expanded by using Taylor expansion at $l_1 + l_2 = \lambda_0/4$. By omitting the high-order terms, (3) can be written by

$$\frac{2L_m \omega_c}{Z_c} + \beta_c (l_1 + l_2) = \frac{\pi}{2}. \tag{4}$$

Since

$$\beta_c = \frac{\omega_c \sqrt{\varepsilon_{RE}}}{c},$$

where $c$ is speed of the light in the free space.

The even-mode resonant angular frequency can be given by

$$\omega_e = \frac{\pi}{2(2L_m Y_c + A)} \tag{5}$$

where

$$A = \frac{\sqrt{\varepsilon_{RE}} (l_1 + l_2)}{c}.$$ 

For the odd-mode case, the equivalent-circuit representation of the resonator when the electric wall is applied at the $AA'$ plane is illustrated in Fig. 2(b). The odd-mode input admittance is

$$Y_{odd} = jY_c \left[ \frac{2\omega_c C_m + Y_c \tan \beta l_1}{Y_c - 2\omega_c C_m \tan \beta l_1 - \cot \beta l_2} \right]. \tag{6}$$

where $\beta_0$ is the propagation constant at the odd-mode resonance angular frequency $\omega_0$.

Using (1) and (6), it reads

$$\frac{2C_m \omega_0}{Y_c} = \frac{1}{\tan \beta_0 (l_1 + l_2)}. \tag{7}$$

For a small $C_m$, $l_1 + l_2 \approx \lambda_0/4$, the right-hand side of (7) can be expanded by using Taylor expansion at $l_1 + l_2 = \lambda_0/4$. By omitting the high-order terms, (7) can be written as

$$\frac{2C_m \omega_0}{Y_c} + \beta_0 (l_1 + l_2) = \frac{\pi}{2}. \tag{8}$$

Since

$$\beta_0 = \frac{\omega_0 \sqrt{\varepsilon_{RE}}}{c}.$$ 

The odd-mode resonant angular frequency can be determined by

$$\omega_0 = \frac{\pi}{2(2C_m Z_c + A)} \tag{9}$$

The center frequency of the BPF can be approximated by averaging the even- and odd-mode frequencies as

$$f_0 = \frac{1}{4\pi} (\omega_e + \omega_0) = \frac{1}{8} \left[ \frac{1}{2C_m Z_c + A} + \frac{1}{2Y_c L_m + A} \right]. \tag{10}$$

The coupling between two modes is characterized by the coupling coefficient $C$ [7], which can be computed from the knowledge of even- and odd-mode frequencies as

$$C = \frac{\omega_0^2 - \omega_e^2}{\omega_0^2 + \omega_e^2} = F(Y_c L_m - C_m Z_c) = M - E \tag{11}$$

where

$$F = \frac{4(A + Y_c L_m + Z_c C_m)}{(2Y_c L_m + A)^2 + (2Z_c C_m + A)^2}$$

and

$$E = F Z_c C_m.$$ 

From (11), the inter-stage couplings of the SEMCP are formed by two separate parts, i.e., electric ($E$) coupling and magnetic ($M$) coupling, as illustrated in the filter topology of Fig. 1(b). The couplings in two coupling paths are dependent and have the canceling effects for the total coupling coefficient $C$. 

The external quality factor [23] can be determined by averaging the external quality factor of the even and odd modes

\[ Q_e = \frac{1}{2} (Q_{e,e} + Q_{e,o}) \]

\[ = \frac{\pi Z_L}{4 Z_c} \left( \frac{1}{\sin^2 \left( \frac{\pi}{2} (l_2 + l_e) \right)} + \frac{1}{\sin^2 \left( \frac{\pi}{2} l_2 \right)} \right) \]  

(12)

where \( Z_L = 1/Y_L \) is the impedance at the I/O ports.

The transmission characteristic of the filter can be calculated from the odd- and even-mode input admittances [9] and is expressed as

\[ S_{21} = \frac{Y_{\text{odd}} - Y_{\text{even}}}{(1 + Y_{\text{odd}})(1 + Y_{\text{even}})} \]

(13)

where \( Y_{\text{even}} = Y_{\text{even}}/Y_L \) and \( Y_{\text{odd}} = Y_{\text{odd}}/Y_L \) are normalized even- and odd-mode admittances, respectively. MATLAB6.5 is used to discuss the following two useful conditions.

- **Magnetic coupling** \( M \) **dominant** \( (C > 0) \)

  Now \( Y_{L_e L_m} > C_m Z_c \), the operating frequency of the odd mode is higher than that of the even mode and the coupling in the bottom coupling path of Fig. 1(a) is dominant. For the same dimension of the transmission line and I/O ports, the effects of coupling elements \( (L_m \text{ and } C_m) \) in two coupling paths on filter performance are compared in Fig. 3. When \( C_m = 0 \), there is only one ZP generated in the high stopband due to the harmonic effects. While \( C_m > 0 \), there is an additional ZP generated in the high stopband and the filter demonstrates a good rolloff in the high stopband. If both \( L_m \) and \( C_m \) are increased, the operating frequency can be shifted down while keeping the coupling coefficient fixed. However, the rejection in stopband will be reduced. When \( L_m \) is fixed at \( L_m = 0.15 \) nH, the increased \( C_m \) (see \( C_m = 0 \) pF and \( C_m = 0.01 \) pF) can decrease the bandwidth of the filter by reducing the operating frequency of the odd mode.

- **Electric coupling** \( E \) **dominant** \( (C < 0) \)

  Now \( Y_{L_e L_m} < C_m Z_c \), the operating frequency of the even mode is higher than that of the even mode and the coupling in the upper coupling path of Fig. 1(a) is dominant. For the same dimension of the transmission line and I/O ports, the effects of coupling elements \( (L_m \text{ and } C_m) \) in two coupling paths on filter performance are compared in Fig. 4. When \( L_m = 0 \), no finite ZP can be generated in the stopband. When \( L_m > 0 \), there are two additional ZPs generated in the stopband and the filter demonstrates a good rolloff. When both \( L_m \) and \( C_m \) are increased, the operating frequency can be shifted down, while keeping the coupling coefficient fixed. However, the rejection in the stopband will be reduced. When \( C_m \) is fixed at \( C_m = 0.05 \) pF, the increased \( L_m \) (see \( L_m = 0.0 \text{ nH and } L_m = 0.05 \text{ nH} \)) can decrease the bandwidth of the filter by reducing the coupling coefficient \( C \) or the operating frequency of the even mode.

III. **SECOND-ORDER FILTER REALIZATION**

By comparing Fig. 3 with Fig. 4, it is interesting to note that, for the \( E \) and \( M \) dominant SEMCP filters with the same transmission line dimensions (the same width of \( W_0 \) and length of \( l_3 \) and \( l_2 \)), the filter response can be completely controlled by choosing a different dominant coupling path, as well as different coupling element values. The canceling effects of \( E \) and \( M \) couplings in two paths are helpful for a narrow bandwidth filter, where a smaller coupling coefficient is required [10]. One additional ZP, generated in either the low or upper stopband, can be used to improve the stopband performance.
increased as compared to Fig. 5(i). By properly choosing the dimensions of the coupling parts, either magnetic or electric coupling can be dominant. Fig. 5(iii) presents the structure where parallel coupling lines and a via ground are used. The RT/Duriod 6010 dielectric substrate with relative permittivity of $\varepsilon_r = 10.2$ and thickness of 0.635 mm and commercial EM software IE3D 9.0 are used in the following design and analysis. Fig. 6 demonstrates the conditions when the electric coupling is dominant. The length of $l_u$, which mainly determines the occupied area of the filter, is fixed. As expected, similar characteristics as the lump-element condition in Section II can be achieved. When the external quality factor is fixed, the increased magnetic and electric couplings cancel each other in the operating frequency range. Thus, the filter bandwidth, which is mainly determined by the inter-stage coupling coefficient $C$, changes very little, while the operating frequency is shifted down due to the increased loadings in two coupling paths. Fig. 7 gives the condition when magnetic coupling is dominant. The length of each resonator is fixed, and the filter of the SEMCP can generate additional ZP in the upper rejection band. The increased $E$ and $M$ couplings are also canceled by each other. Thus, the filter bandwidth can be maintained even when the electric and magnetic couplings are increased; while the operating frequency is shifted down by increased coupling in each path due to the loading effects in two coupling paths. In Fig. 8, results of a magnetic coupling dominant filter in Fig. 5(i) are compared. There are two finite transmission ZPs generated in the upper stopband. The first ZP, close to the operating frequency, is generated by canceling effects of the electric and magnetic coupling, and the generation of the second ZP is mainly due to the harmonic effects of the distributed transmission line [13].

In Fig. 9, simulated and measured results of the electric coupling dominant filter in Fig. 5(iii) are compared. The discrepancies in bandwidth and attenuation in low stopband between the measurement and simulation may come from the differences between the simulated and measured structure [20], which includes the fabrication errors in the single via ground and narrow coupling gap. The measured specifications of the filter are: 1) operating frequency of 2.4 GHz; 2) 1-dB bandwidth of 380 MHz; 3) the insertion loss of 0.85 dB; and 4) the occupied area (without considering the I/O feed lines) is only $0.065\lambda_0 \times 0.027\lambda_0$ ($\lambda_0$ is the free-space wavelength at operating frequency). The fabricated photograph of the second-order filters are illustrated in Fig. 10.

IV. HIGH-ORDER SEMCP FILTER

Fig. 11 demonstrates an $n$th-order SEMCP filter topology by using the SEMCP topology. The main differences of SEMCP fil-
coupling paths exist between some adjacent resonators canceling [refer to (11)].

To demonstrate the control and the inter-stage coupling is the result mm, denoted the electric coupling, as in (11). The dominant pair and one dominant pair are shown SEMCPs simultaneous, it is believed that the ZPs can be generated in the upper stopband, while the dominant magnetic coupling can be used to generate ZPs in the low stopband, while the dominant pair and one dominant pair are shown.

The configuration and topology of a fourth-order SEMCP filter are shown in Fig. 12(a) and (b), respectively. Two E dominant SEMCPs are introduced between resonators 1 and 2 as well as 3 and 4. Firstly, a filter with 17% fractional bandwidth (FBW) is designed. The total coupling coefficient $C$ is the result of coupling after $E$ and $M$ canceling [refer to (11)].

Fig. 9. Comparison of simulated and measured results of the second-order $E$ dominant SEMCP filter.

Fig. 10. Fabricated second-order SEMCP filter. (a) $M$ dominant. (b) $E$ dominant.

Fig. 11. Topology of the high-order SEMCP filter.

The configuration and simulation of the fourth-order $E$ and $M$ dominant SEMCP filter. Dimension [for both structures (a) and (b)]: $W_0 = 0.59$ mm, $l_E = 2.0$ mm, $l_M = 5.94$ mm, $l_J = 4.52$ mm $R_{\text{via}} = 0.1$ mm, $s_1 = 0.13$ mm, $s_2 = 0.9$ mm, $s_3 = 0.3$ mm, $l_B = 1.2$ mm, $w_B = 0.4$ mm (refer to Figs. 5 and 112).

The external quality factor $Q_e$ and the inter-stage coupling $C$ can be calculated from [9] and [10], and are $Q_e = 6.52$ and

$$C = \begin{bmatrix}
0 & -0.141 & 0 & 0 \\
-0.141 & 0 & 0.112 & 0 \\
0 & 0.112 & 0 & -0.141 \\
0 & 0 & -0.141 & 0
\end{bmatrix}$$

where the negative signs of coupling coefficients in the coupling matrix $C$ denote the electric coupling, as in (11). The optimized filter dimensions are $W_0 = 0.59$ mm, $l_E = 3.95$ mm, $l_M = 5.94$ mm, $l_J = 4.52$ mm, $s_1 = 0.09$ mm, $R_{\text{via}} = 0.2$ mm, and $s_2 = 0.6$ mm. To demonstrate the control of the ZPs both in the low and high stopband, the configurations and EM simulation results of the fourth-order SEMCP filters with one $E$ dominant pair and one $M$ dominant pair are shown in Fig. 13. Filters with inverted pairs and no-inverted SEMCP pairs have the same dimensions. Each filter generates additional...
of controlling the ZPs and inter-stage coupling and the possibility of achieving low insertion loss and compact size simultaneously. The photographs of an SEMCP filter and hairpin line filter are shown in Fig. 16. The size of the fabricated fourth-order SEMCP filter occupies an area as small as $0.06\lambda_0 \times 0.05 \lambda_0$ $0.82 \times 0.75 = 0.615 cm^2$, which is only one-third of that of the fabricated hairpin line filter (without considering the I/O feed lines, $1.26 \times 1.48 = 1.865 \text{cm}^2$).

V. CONCLUSION

In this paper, a novel SEMCP filter topology together with a configuration has been proposed. The characteristics of the $E$ dominant and $M$ dominant SEMCP filters have been investigated and the advantages such as compact size, sharp rolloff, and low loss have been demonstrated via simulation and experiment. The general high-order SEMCP filter topology has been introduced and the fourth-order $E$ dominant filter with compact size and low insertion loss has been implemented. It should be noted that, although the topology has been realized by using a microstrip line, it may be applicable to other transmission lines such as the coplanar waveguide (CPW) stripline. For example, if the CPW transmission line is used to realize the filter topology, the grounding via-hole can be replaced by a ground shunt.

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COMPACT SIZE COUPLING CONTROLLABLE FILTER WITH SEMCPs


