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A Unified Framework for Automated 3-D Segmentation of Surface-Stained Living Cells and a Comprehensive Segmentation Evaluation

Erland Hodneland, Nickolay V. Bukoreshtliev, Tilo W. Eichler, Xue-Cheng Tai, Steffen Gurke, Arvid Lundervold*, Member, IEEE, and Hans-Hermann Gerdes

Abstract—This work presents a unified framework for whole cell segmentation of surface stained living cells from 3-D data sets of fluorescent images. Every step of the process is described, image acquisition, prefiltering, ridge enhancement, cell segmentation, and a segmentation evaluation. The segmentation results from two different automated approaches for segmentation are compared to manual segmentation of the same data using a rigorous evaluation scheme. This revealed that combination of the respective cell types with the most suitable microscopy method resulted in high success rates up to 97%. The described approach permits to automatically perform a statistical analysis of various parameters from living cells.

Index Terms—Automated whole cell segmentation, level set, mathematical morphology, region differencing, segmentation evaluation, watershed.

I. INTRODUCTION

The study of organisms at the single-cell level has tremendously advanced our understanding of human physiology and pathology in recent years. In this respect, computer-assisted cell recognition obtained by image segmentation represents an important tool. Although humans are superior to computers in terms of shape detection and segmentation, they are inadequate to process vast amounts of data and to perform an objective evaluation of experiments. Therefore, automated cell segmentation is a growing field of interest with a wide range of applications [1]–[5], which permits the statistical analysis of various cell parameters and thereby has the potential to identify even subtle effects of drugs or toxins on cells.

A. Fluorescent Labeling of Cells

To fully benefit from the advantages of automated segmentation, a suitable cell targeting method must be chosen. In this respect, at least four different approaches have been published. First, several studies describe applications to perform cell segmentation on phase contrast images [6]–[9]. However, such images suffer from low contrast and uneven illumination. Second, numerous studies report on the segmentation of stained cell nuclei [3], [10]–[16]. This approach is able to identify the nuclei but does not delineate the outer border of the cell. Third, segmentation algorithms have been applied to cytoplasmically stained cells [2], [11], [17]–[20]. Although these algorithms detect the area covered by the cells, they often fail to outline the exact boundaries between attached cells, especially in large clusters of cells. Fourth, methods for segmentation of surface-stained cells are able to combine the strength of the two formerly mentioned methods by determining both the number of cells and their boundaries. This enables in particular the calculation of various cell parameters for whole cells to be computed, such as shape, volume and metabolism of cells in confluent cell cultures or tissue. To the best of our knowledge only very few studies have addressed the task of segmenting surface-stained cells. Notably, in these studies only fixed cells were used [13], [21]–[23]. The work in [13] was also restricted to 2-D since antibodies against integrin receptor subunits were used as surface marker, only labeling the cell membrane attached to the substrate.

To extend the existing methods toward a fully automated 3-D whole cell segmentation of surface stained living cells, we have developed versatile methods and also combined existing approaches which apply to images showing fluorescently labeled cell borders.

B. Preprocessing of Images

As an introductory step, a background subtraction is required if the images exhibit slowly varying background signals, which can severely compromise with for instance thresholding techniques. Malpica [14] used 25 empty control matrices for adjustment and Adiga [11] corrected the background by a sliding window. A top-hat filtering can also be used for background correction. In this work, the inhomogeneity of the background...
in the images was low, and we did not use background correction for the experimental part.

Normally, the quality of fluorescent images is reduced due to noise and other undesired influences. The undesired signals can be decreased but not fully excluded since they arise from normal cell processes like endo- and exocytosis, cell division, cell debris and accumulation of the fluorescent dye in other compartments of the cell than those of interest. Therefore, a proper filtering technique is advised prior to any image analysis, aiming at removing undesired signals and simultaneously preserving or even enhancing the signals from the objects of interest. In this work we have implemented and compared linear and nonlinear spatial filters such as the Gaussian, the median filter [24], and directional coherence enhancement filter [2], as well as iterative methods for filtering based on partial differential equations [25]–[29].

Moreover, the surface stained cells shown in this work express the plasma membrane as ridges, therefore it is reasonable and also necessary to perform a ridge enhancement as an additional filtering step prior to the segmentation. Existing methods include the Gabor filter banks [30] as well as the eigenvalue decomposition of the Hessian matrix [31]–[34]. The Hessian ridge enhancement takes advantage of the fact that the largest eigenvalue is significantly larger than the smallest eigenvalue on a ridge. Lindeberg [35] describes how the second derivatives can be used for ridge detection. In this study, we have improved existing methods for ridge enhancement.

C. Segmentation of Cells

For the main step in the processing chain for segmentation of surface stained cells, several options are available. Baggett et al. [21] implemented a semi-automated cell segmentation which is related to ridge following (see Section II-D-3). This approach was extended to 3-D in [22]. To trace the extensions of neurons, the neurites, Dima et al. [20] used a ridge following method based on the gradient points along the thin neurites. Al-Kofahi et al. [36], [37] used directional correlation kernels to trace neurites and replaced the average template response by the median response. We have implemented their method to demonstrate that ridge following can be used for 2-D cell segmentation by tracing the ridges displaying the cell borders (Section II-D-3).

We have chosen to thoroughly compare a marker controlled watershed segmentation with a level set model. The watershed method is widely described in the literature [18], [38]–[40]. Bengtsson et al. [17], [18], [41] obtained success rates of between 89% and 97% for segmentation of cells stained with calcein [17]. They used a labeling method to measure the amount of over- and under-segmented objects, but they were not able to measure the segmentation quality of the border lines between the watershed regions. Adiga [11] applied the watershed algorithm for segmentation of cell nuclei and an active surface model for further refinement, obtaining a deviation between \( \pm 2\% \) and \( \pm 5\% \) from the manual solution. In Adiga et al. [2] an automated seeding and a watershed-like region growing technique was applied to segment nuclei, followed by an iterative, controlled dilation, where all regions were blown up with the constraint that they should not touch their neighbors. Their quality measure, the percentage of symmetric difference, revealed high success rates between 87% and 95% and low false positive rates of between 5% and 16%. Malpica [14] describes the use of morphological watersheds for segmentation of clustered nuclei. They computed a distance transform to create markers for the watershed segmentation, resulting in success rates between 81.25% and 93.39% with an over-segmentation less than 4.67%. Dow [23] used a nucleus staining to obtain reliable markers for a watershed segmentation generating the boundaries of the nuclei. This approach for generating markers is very advantageous, but we have not followed this idea since the biological setup not always allows an additional nucleus staining. Our aim has therefore been to create a framework for segmentation only depending on a surface staining. The obtained boundaries in [23] represented an approximation to the cell surface and were used in the successive active contour to detect the cell surface. For the active contours, there are at least two different types of models, parameterized active contours and geometric active contours. Zamani et al. [16] used a gradient vector flow (GVF) snake to segment the nuclei of white blood cells, and they report a high success rate of about 95% for the segmentation of 40 cells. Solorzano et al. [13] describe a geometric active contour, a level set approach, for a successful segmentation of 19 lamin stained nuclei and a whole cell segmentation of 24 integrin lamin stained cultured cells and 23 integrin-stained cells in tissue. We have chosen to implement their level set segmentation as a comparative method to the watershed (Section II-D-2). The level set method is advantageous to watershed due to smoothing properties of the resulting segmentation. However, recent progress on the watershed approach has included a smoothing term into the models [38], [42]. Besides these improvements, the watershed algorithm is faster than the active contours, and in particular compared to the geometric active contours there is a significant reduction in computational speed.

D. Segmentation Evaluation

Finally, a quality measure is necessary to evaluate the performance of different segmentation methods, also referred to as segmentation evaluation. For cell segmentation, evaluation was in the past rarely performed using comparative criteria [2], [11], [14], [16]–[18], [41], which makes an interstudy comparison difficult. Therefore, we have in this work aimed at establishing a common framework for evaluation of cell segmentation, which takes into account over- and under-segmentation as well as misplaced boundaries. Within the area of image segmentation, numerous studies on segmentation evaluation have been reported. The surveys by Zhang [43], [44] classify the evaluation methods for segmentation into three groups: analytical, empirical goodness, and empirical discrepancy methods. A region differencing [45] belongs to the empirical discrepancy methods by comparing segmented objects with a set of reference objects. This approach enables the use of reference objects created from manual delineation, which is probably the best available solution. Therefore, we have used this evaluation method as basis for our segmentation evaluation. A similar approach was applied to cell segmentation in [2], where a percentage of symmetric difference represents the overlap between two objects.
The overall aim of the present work is to construct a unified framework for segmentation and quantification of surface stained living cells in 3-D, together with a logically linked quality assessment procedure. We have achieved this by combining prefiltering, ridge enhancement, automated marker construction, watershed segmentation, ridge following, level set segmentation, and a comprehensive segmentation evaluation. In particular, we have contributed in the development of a new methodological variant of ridge enhancement and segmentation evaluation.

II. METHODS

In this section, a unified framework for segmentation of surface stained cells is described. All compared methods except the ridge following method are applied to surface stained living cells in 3-D, displaying a pronounced signal of the plasma membrane. Consequently, the method of choice must aim at preserving ridges more than edges. In 3-D, the objects of interest are surfaces.

Fig. 1(a) shows two associated PC12 cells, and the intensity profile along the dashed line is plotted in Fig. 1(b) to emphasize the ridge property of the plasma membrane where the peaks of the ridges are indicated by arrows. Notably, inhomogeneous distribution of the dye in the membrane creates discontinuities. Inside the cells there are bright spots and regions, which derive from endocytosed membrane. Such effects represent more serious challenges to the segmentation protocol than the Gaussian white noise. To reduce the background a set of six filters were compared, among those three direct spatial filters and three partial differential equation (PDE)-based filters. All described filter techniques are implemented in true 3-D, and the conductivities are taken as described in [46].

- **Gaussian smoothing** [24] (Fig. 2(b), $\gamma = 9$, and $\sigma = 3$) is a traditional method for smoothing. $\sigma$ is the standard deviation of the Gaussian distribution.
- **Median filter** [24] (Fig. 2(c), $\gamma = 9$) is a powerful order-statistic filter method which preserves edges efficiently. In the median filter, each output pixel contains the median of the image values within $\gamma$. For the 3-D implementation, we used bilinear interpolation to extract the image values at different positions.

- **Directional coherence enhancement filter** [2] (Fig. 2(d), $\gamma = 15$) is a directional filter performing a texture analysis to remove noise. The method has a high noise tolerance due to a special averaging process called semi-Olympic averaging. Our 3-D implementation uses the principal and diagonal directions, and $\gamma$ was adjusted to the width of the given ridges.
• PDE-based edge enhancing diffusion [26], [27] (Fig. 2(e), $\delta t = 0.1$, 100 iterations, $k = 20$) performs a stronger smoothing along the edges than across in regions with a high gradient. Given the image $u$ and the diffusion matrix $D = R^T C R$, we solve

$$\frac{\partial u}{\partial t} = \nabla \cdot (D \nabla u).$$

(1)

$C$ is a diagonal matrix with the conductivities $c_i$, $i = 1, \ldots, 3$ along the principal diffusion directions. $R$ is the rotation matrix constructed from an orthonormal set of vectors, $R = [v_1 | v_2 | v_3]$, where $v_1 = \nabla u$.

• Coherence enhancing diffusion [27], [47] (Fig. 2(f), $\delta t = 0.1$, 50 iterations, $k = 1$) has proved to be successful for fingerprint images. The cell images presented here and fingerprint images have the common property that important structures are thin lines or ridges. The aim for both types of input image is to smooth along the ridges and not across them, and the diffusion is therefore directed along the eigenvectors of the structure tensor [27]. The eigenvectors were computed numerically in 3-D due to instability of the analytical approach.

• Inverse diffusion [48] (Fig. 2(g), $\delta t = 0.1$, 10 iterations, $k = 1$. $c_3 = \chi(0.4)$ is a method similar to coherence enhancing diffusion where the diffusion across the edge is reversed by reversing the sign of the conductivity along the principal variation. This is an inherently unstable process since the solution of the backward diffusion equation is normally ill-posed [49]. However, if the diffusion is limited to only a few iterations, the method can sharpen the ridges or edges of interest.

For segmentation, it is always recommended to acquire images of the highest possible quality. Despite this, a filtering can be advised to perform to improve the image quality even further. In this case a straightforward Gaussian filtering [Fig. 2(b)] can be sufficient to further improve the image quality. However, more advanced filters like the directional coherence enhancement filter [Fig. 2(d)], the coherence diffusion filter [Fig. 2(f)] or inverse diffusion [Fig. 2(g)] are normally preferred methods, at least if there exists a substantial degree of noise and if the structures of the image are characterized by severe discontinuities. These directional filters are able to close minor gaps in the structures along the principal flow direction. Among those, the directional coherence enhancement filter has higher computational performance than coherence enhancing diffusion and it is also easier to adjust than inverse diffusion due to the reversed diffusion process in the latter. Therefore, the directional diffusion filter is our choice of filtering method in the experimental part (Section III). The median filter [Fig. 2(c)] and the edge enhancing filter [Fig. 2(e)] are more edge preserving than the other filters, and are not well suited for ridge structures. However, the median filter or the edge enhancing filter are highly suitable for images of cytoplasmically stained cells, since the aim under these conditions would be to enhance the edges in the transition zone between cells and background (data not shown).

B. Ridge Enhancement

As a second preprocessing step, a ridge enhancement is recommended, especially for wide field images since light from surrounding pixels is detected as well as light from the center pixel. The ridge enhancement enhances the contrast of ridges compared to other structures, thus creating an image better suited for the cell segmentation and in particular for automated marker generation.

1) Hessian Ridge Enhancement: A convoluted Hessian matrix is given as

$$H_g = g * \begin{bmatrix}
(u_g)_{xx} & (u_g)_{xy} & (u_g)_{xz} \\
(u_g)_{yx} & (u_g)_{yy} & (u_g)_{yz} \\
(u_g)_{zx} & (u_g)_{zy} & (u_g)_{zz}
\end{bmatrix}$$

(2)

where $u_g$ is the normalized and Gaussian convolved image and $g(*)$ is an additional Gaussian convolution. The eigenvalues of the Hessian matrix are computed and every pixel is assigned a geometrical class according to the sign of the eigenvalues [34]. Across the cell boundary there is a large intensity variation, but the variation is small along the tangential plane of the plasma membrane. Therefore, the 3-D plasma membrane has the characteristic geometrical property of $\lambda_1 < 0$, $\lambda_2 \approx 0$, $\lambda_3 \approx 0$, where $\lambda_1$, $\lambda_2$, and $\lambda_3$ are the eigenvalues of the Hessian matrix in decreasing absolute values. To highlight the plasma membrane we choose among other possibilities the transfer function $u_H(\mathbf{x}) = -\lambda_1 - \lambda_2 - \lambda_3$ since it reduces the influence of $\lambda_2$ and $\lambda_3$. This is important since the ridge is seldom perfect and often contains local peaks that exhibit relatively large $\lambda_2$, $\lambda_3$. From $u_H$, the ridge enhanced image $u_H$ will take the largest values on the ridges compared to other geometrical classes, see an example of Hessian ridge enhancement in Fig. 3(b).

2) Ridge Enhancement by Curvature: The ridge enhancement by curvature is our extension to the Hessian ridge enhancement. Here, the ridge enhancement is given as the curvature in the principal direction of variation of the second derivative. Similar to the Hessian ridge enhancement, the eigenvalue decomposition of the Hessian matrix is computed. The purpose is to obtain the eigenvector $v_1$ with the largest modulus of eigenvalues, pointing perpendicular to the ridge. A twice differentiable function can be expressed using the canonical parameterization $\mathbf{r} = \mathbf{a} + f(\xi) \mathbf{j}$.

Consider the vector formula for the curvature of a parametrized curve in 1-D [50] and define a local orientation along $v_1$ for every pixel $\mathbf{x}$ in the image and compute the curvature (4) along $v_1$

$$\kappa(v_1) = \frac{|v_1 \times a|}{|v_1|^3} = \frac{|f''(\xi)|}{(1 + f'(\xi)^2)^{\frac{3}{2}}}$$

(3)

where the derivatives are

$$f'(\xi) = \frac{\partial u}{\partial v_1} \text{ and } f''(\xi) = \frac{\partial^2 u}{\partial v_1^2}$$

(4)

and $\xi$ is the argument along $v_1$. Thus, for any 2-D or 3-D image the problem is transformed into finding the local curvature of the image intensities along a 1-D line parallel to $v_1$ passing through $\mathbf{x}$. A three-point derivative was used to compute $f'(\xi)$ and $f''(\xi)$ along $v_1$

$$f'(\xi) = \frac{u_g(\mathbf{x} + h v_1) - u_g(\mathbf{x} - h v_1)}{2h}$$

(5)

and

$$f''(\xi) = \frac{u_g(\mathbf{x} + h v_1) - 2u_g(\mathbf{x}) + u_g(\mathbf{x} - h v_1)}{h^2}$$

(6)

for a stepsize $h$ approximately equal to half the width of the ridge. For our data a value of $h = 3$ pixels was appropriate. A linear interpolation scheme was applied to extract the correct
Fig. 3. Ridge enhancement. The 3-D raw image in (a) was used to compute a 3-D Hessian ridge enhancement (b) and a ridge enhancement by curvature (c), which is better than (b). A combination of directional coherence enhancement filter with ridge enhancement by curvature was performed in (d), producing the best results. Note that for simplicity only selected planes from the whole image stack is shown, and that all images were computed with equal settings for $\gamma = 9$ and $\sigma = 3$ in the Gaussian convolution.

values from $u_d$. The final ridge enhanced image by curvature is taken as $u_c(X) = \kappa$, an example is shown in Fig. 3(c). In Fig. 17, the ridge enhancement is shown from $x_2$ and $y_2$ views for a true 3-D stack of PC12 cells embedded in agarose.

Clearly, both methods for ridge enhancement [Fig. 3(b) and (c)] produce strong and well characterized ridge patterns, but the ridge enhancement by curvature creates ridges that are more distinct. Moreover, the filtering methods described in Section II-A improve the image quality, but they can not substitute the ridge enhancement. Preferably, the best results are obtained when combining the two steps, a filtering followed by a ridge enhancement, see Fig. 3(d), where the best visual result is achieved.

C. Segmentation and Cell Classification

In this section, three available methods for segmentation are presented, the watershed segmentation, level sets, and ridge following. First, the construction of markers is described, which is a method we have developed and which was shortly described in [42].

1) Creating Markers: To avoid serious over-segmentation we have chosen the use of markers or initialization regions. Still, a fragment merging is often required after the segmentation to remove false borders within objects, but the complexity of the merging is significantly reduced compared to a situation without the use of markers. The marker image is a binary image consisting of either single marker points or larger marker regions where each connected marker is placed inside an object of interest. For the watershed algorithm, each initial marker has a one-to-one relationship to the specific watershed region surrounded by the watershed surface. The level set can split into several regions or disappear around a marker. Both the watershed segmentation and the level sets are strongly influenced by the markers. This dependency is a consequence of both the one-to-one relationship as well as the size and position of the markers. Region-markers generally create results of higher quality than point-markers since their boundaries are closer to the desired boundaries. After segmentation, the boundaries of the detected regions are ideally arranged on the ridges, thus separating each object from its neighbors. The markers can be manually or automatically constructed, but high-throughput experiments often depend upon automatically generated markers to save human time and resources. For the current project, the markers were automatically generated as described in [42]. The image in Fig. 4(a) was used as input to demonstrate the creation of markers. Adaptive thresholding [24], [51] was used to automatically create binary marker regions from the filtered and ridge enhanced image [Fig. 4(b)]. Additionally, the image was scaled between [0, 1] to allow global thresholds for the adaptive thresholding. Specifically, the adaptive thresholding results in a binary image

$$u_d(x, y, z) = \begin{cases} 1, & \text{if } u(x, y, z) > \mu \max(u) + A_x(u, x, y, z) \\ 0, & \text{else} \end{cases}$$

of the high intensity structures of the raw image. $\mu$ is a user-defined scalar threshold with typical values of $0.01 \rightarrow 0.2$ and $\gamma$ is the filter dimension of the average filter $A_x(u, x, y, z)$ of $u$ in a $\gamma$-neighborhood around $(x, y, z)$. An adaptive thresholding has a much higher resistance against noise and inhomogeneous illumination compared to global thresholding for labeling of high intensity objects. Note that adaptive thresholding is not required due to the slightly varying background of the images, but rather because of inhomogeneous staining and endocytosis of the dye. Therefore, a correction of the background was not needed but adaptive thresholding was used to detect markers. The image in Fig. 4(c) is an example of adaptive thresholding applied to Fig. 4(b). Small objects were removed [Fig. 4(d)] and an iterative morphological closing was performed on the
image \( u_p \), where all pixels belonging to the same region have the same intensity value. Thus, every region in \( u_p \) is given as 
\[ R_i = \{ x | u_p(x) = i, i = 1, \ldots, n \} \]
where \( n \) is the number of markers. There are several choices of methods for segmentation, which are treated in more detail in Section II-D.

3) Fragment Merging: All three described segmentation methods, the watershed transform, the level sets and the ridge following can create an over-segmentation, which to a certain degree can be corrected by fragment merging. The underlying idea is to merge neighbor regions that fulfill given criteria [11]. Consider the piecewise constant image \( u_p \) resulting from segmentation and define neighbor regions to be all pairs of regions with a common border. Label the set of pixels in the border between region \( i \) and \( j \) as \( b_{ij} \), and let \( T_1, T_2, \) and \( T_3 \) be user-defined thresholds. We have in our simulations used three merging criteria. The first requires the relative mean intensity \( r_{ij} \) on the border to be above a certain threshold. This is reasonable since a weak border is probably false. The relative mean intensity is computed as the mean intensity on the border \( b_{ij} \) divided by the mean intensity of a bilateral structure \( bb_{ij} \) alongside, which is computed from dilation of the border using two structural elements \( se(\tau_1) \) and \( se(\tau_2) \) of different size, where \( \tau_1 = 2 \) pixels and \( \tau_2 = \tau_1 + 2 \) pixels. Thus, \( bb_{ij} = b_{ij} \cup se(\tau_2) \). The dilation operator \( b_{ij} \) and \( bb_{ij} \) are represented as binary images with “ones” on the given structure. Using a bilateral structure to obtain a control volume for intensities ensures local sensitivity, in contrary to a global measure. The mean intensity \( \mu(u_b) \) in \( u \) inside an object is given as the total intensity \( S(u_b) \) divided by the volume \( V(b) \), which is used to compute the relative mean intensity \( r_{ij} \) of \( bb_{ij} \).

\[
\mu(u_b) = \frac{S(u_b)}{V(b)} = \frac{\int_{\Omega} u_b(x) h(x) dx}{\int_{\Omega} h(x) dx}, \quad r_{ij} = \frac{\mu(u_b_{ij})}{\mu(u_{bb_{ij}})}.
\] (7)

If the border is not colocalizing with a true ridge, it probably implies \( r_{ij} < T_1 \) and the intensity criterion will facilitate merging.

The second merging criterion restricts the allowed difference in size of the two merging candidates. This requirement is necessary to prevent cell regions to become merged with background in images with low contrast ridges. Thus, a merging requires \( v_{ij} = V(R_i)/V(R_j) < T_2 \) where \( V(R_i) \geq V(R_j) \).

The third merging criterion requires an increase or stationary surface convexity in the case of merging. This criterion efficiently promotes merging when an over-segmented region is within a concavity, partly surrounded by another region. We let \( c(R_i) \) denote the convex hull [24] of region \( R_i \). Again, \( R_i \) is a binary image with “ones” on the given structure and “zeros” elsewhere. Then, the relative change of convexity after a possible merging of region \( i \) and \( j \) can be expressed as

\[
c_{ij} \equiv \frac{(V(R_i) + V(R_j))/V(c(R_i) + V(c(R_j)))}{V(R_i + R_j)/V(c(R_i + R_j))}. \] (8)

The merging procedure is executed by always picking the lowest intensity structure \( r_{ij} < T_1 \), and simultaneously checking whether the relative volume \( v_{ij} < T_2 \) and the relative change of convexity \( c_{ij} < T_3 \). If this holds, a merging is performed. The lowest \( r_{ij} \) is then removed from the queue and

---

**Fig. 4.** Automated construction of markers. The image (a) was used for ridge enhancement (b) to improve the signal intensity of the ridges. An adaptive thresholding was applied to detect the ridges and convert them into binary structures (c). The smallest objects were removed due their size (d) and a morphological closing was performed to close gaps in the binary structure (e). The closing was repeated iteratively with increasing radius \( r \) of the circular structural element \( se \), \( r_{se} < r_{se+1} \). A binary filling was computed at the closing at each iterative step (f) and all binary objects of the size within a user-defined interval were selected and used as marker regions. However, the objects were only selected if they had no intersection to previously selected objects. This enables larger marker regions with their boundaries closer to the true boundaries of the desired objects.
the procedure is repeated. The merging stops when $r_{ij} \geq T_3$ holds for every $r_{ij}$ in the queue. As an example, Fig. 5(a) shows a small selection of plane 15 of the filtered and ridge enhanced image stack in Fig. 8. In Fig. 8(b), a watershed segmentation is displayed for four regions, numbered from one to four. The common border $b_{23}$ and the bilateral structure $b_{23}$ for the pair of neighbor regions 2 and 3 are shown in Fig. 5(c) and (d), respectively. They are used to compute the relative intensity $r_{23} = 2.2$, relative volume $v_{23} = 1.0$ and relative convexity $c_{23} = 0.91$ that all facilitate merging according to empirically obtained thresholds of $T_1 = 2.5$, $T_2 = 10$ and $T_3 = 1$. These thresholds were found to be suitable when using the ridge enhanced image by curvature, $u_k$. However, the merging can also be accomplished using the Hessian ridge enhanced image $u_H$ or the original image, which requires another value for $T_3$. It is certainly possible to replace these merging criteria by others that are closely related to the image properties, and also accommodate new criteria on top of the existing.

4) Classification: After segmentation and fragment merging, the regions $R_i$ still remain to be classified as “background” or “cells.” One approach for classification is to design a neural network or a classification tree. We tried this in an early stage but it was abandoned due to lack of flexibility; some tasks require 2-D segmentation, others partly 3-D or even full 3-D. A neural network or a classification tree has to be trained on a large set of data, and due to nonlinearity between the networks, those obtained from a 2-D training set can not automatically be extended into 3-D. Instead, a set of requirements characterizing a typical cell was implemented. Every requirement has to be fulfilled in order for a region $R_i$ to be classified as a cell. We define reduced 3-D as the situation when the range of the original image is less than the range of a cell diameter. We use several requirements for classification of rounded-up cells into “cells” or “background,” with given user-defined thresholds $v_1$, $v_2$, $I_1$, $I_2$, $C_1$, and $C_2$.

1) Minimum and maximum volume. The volume of a cell must stay within the interval $v_1 < V(R_i) < v_2$ where $v_1 < v_2$.
2) Mean intensity. It is expected that a cell has higher mean intensities than background regions, $\mu(u, R_i) > I_1$.
3) Mean intensity on the boundaries. The boundary of a cell is assumed to be brighter than background regions, $\mu(u, \partial R_i) > I_2$, where $\partial R_i$ is the boundary of region $R_i$.
4) Convex volume. Cells are normally round-like and they are therefore expected to have a relatively high convexity. $V(R_i)/V(c(R_i)) > C_1$ where $c(R_i)$ is the convex hull of $R_i$.
5) Convex perimeter. It is also assumed that a large portion of the boundary of the cells have a convex surface, therefore, expecting that $V(\partial R_i \cap \partial c(R_i))/V(\partial c(R_i)) > C_2$.

$v_1$ and $v_2$ are directly given from the lower and upper expected volume of a cell. $I_1$ and $I_2$ should be normalized to the expected background intensity. For seeded cells, the background intensity can usually be estimated from the mean intensity of the largest watershed region that is too large to be a cell. If the cells are too dense to expect any free background, the background intensity can be estimated from a blank image. Moreover, an accumulated and highly reliable background intensity can be estimated as the mean intensity of large watershed regions from the whole experiment. $C_1$ and $C_2$ depend on the cell type [15], but $C_1 = 0.5$ and $C_2 = 0.5$ have successfully been applied to PC12 cells (see Section II-F), also between different experiments. The same settings are suitable for 2-D images as well as 3-D stacks, which is convenient and practical. An example of a classification is shown in Fig. 6 where the watershed lines in Fig. 6(a) delineate the boundaries of the segmented regions. The final classification is shown in Fig. 6(b) with background (black), cells (gray), and background.
boundaries around cells (white). Region 1 and region 8 are correctly classified as background, and the others as cells.

D. Comparing Methods for Segmentation

1) Watershed Segmentation: Watershed segmentation [18], [38]–[40], [52] is a method for segmentation belonging to the class of morphological operators. Among other applications, watershed has in the past been used for nuclei segmentation [14], [15]. In contrast to a surface staining, a nucleus staining provides an image which has more in common with a cytoplasmic staining in the way the objects are not necessarily local minima or maxima due to the continuous staining between cells or nuclei. To overcome this problem, the authors in [15] used a gradient-weighted distance transform to transform the original nucleus image into an image where each object was a regional minimum (or maximum). For the same task, a morphological gradient was used in [14] to create an image suitable for watershed segmentation. In contrast to the nucleus and cytoplasmic staining, the surface staining creates images which are directly suitable for watershed segmentation since the plasma membrane between the cells is already crest lines. Therefore, a transformation of the original image is not required and the watershed transform can be applied directly to the raw image.

In this study, we have used the watershed transform by immersion [40] with a 26-connected neighborhood in 3-D as one of the comparative approaches for cell segmentation. As an example, the marker image in Fig. 4(f) was used for the watershed segmentation, but an additional marker representing the background was added. The watershed transform itself was carried out on the filtered image, but the ridge enhanced image can also be used, especially for challenging images. Fig. 7(c) shows the watershed transform of the filtered and ridge enhanced image Fig. 7(a) where the image in Fig. 7(b) was used as marker image. The watershed algorithm was also applied to a full 3-D data set to demonstrate the properties in 3-D. Fig. 8 shows every fifth plane of the raw image (column 1), the ridge enhanced image (column 2), and the watershed segmentation (column 3) of a 3-D data set with 40 planes.

2) Level Set: The level set segmentation can also be used to detect cells. We have implemented a slightly different version of the method described in Solorzano [13]. In level sets, the interface is described implicitly by the zero level set of one or more higher-dimensional functions, the level set functions. By this method, one level set function is used for each marker. The marker image contains normally more than one marker, and one needs to take into consideration the conflict when interfaces of different level set functions meet since at most one level set function should be larger than zero in every point. To overcome this problem, the conflict measure as proposed in [13] was implemented. Fig. 7(d) shows the marker image used for the level set segmentation of Fig. 7(a). It is equal to the marker image used in the watershed except from the background marker. Fig. 7(e) shows the resulting level set segmentation resulting from the interfaces of the level set functions. A full 3-D segmentation using level sets is shown in Fig. 8, column 4.

3) Ridge Following: Also ridge following methods enable a whole cell segmentation, relying on a tracing of high intensity structures to accomplish the segmentation. A fully automated 2-D ridge following is described in [36], [37]. High intensity structures with higher values than their surroundings are then locally traced along a local path until a stop criterion is fulfilled. An example of this method is shown in Fig. 9(a) and (b) for the image in Fig. 7(a). To the best of our knowledge, a local ridge following in 3-D has not been published, and we have therefore not evaluated the method of [36] and [37] in Section III. The study of Baggett et al. [21] represents a different ridge following, finding the globally optimal path between two points in a transformed coordinate system. At least one interior point and one boundary point is needed, and the path from the boundary point to itself is found in the polar transformation around the interior point, using a gray-weighted distance transform. This method was extended to 3-D in [22]. We have downloaded and tried the software, which is well-functioning. However, since the method is semi-automated due to the user-defined input of the interior and boundary points, we have chosen to omit the method from the thorough segmentation evaluation in Section III.

E. Method for Segmentation Evaluation

Segmentation evaluation is a frequently debated and usually task-specific topic in computer vision and automated image analysis applications [43], [44]. The aim and purpose of segmentation differs significantly and it is therefore a challenging task to construct methods for segmentation evaluation that comprise numerous criteria of success. The variation may include different requirements regarding accuracy of boundaries, the use of landmarks, penalization of under- and over-segmented regions (including penalization of false negative and false positive objects), fuzzy versus binary (nonprobabilistic versus probabilistic) ground-truth and single versus multiple experts for manual delineation. Furthermore, certain segmentation projects require assignments of various weights within each separate region, depending on the local importance. Due to such complicating factors and also because little has been accomplished in the field of cell segmentation [6], a major focus in this work has been to further develop the region differencing method, a specific framework of the empirical discrepancy for segmentation evaluation in cell images. Our specific contribution is the combination of region differencing with a method to deal with over- and under-segmented regions.

In Zhang [43], empirical discrepancy methods can be decomposed into different classes where the discrepancy is based on
one or more of the following features: i) the number of missegmented pixels, ii) the position of missegmented pixels, iii) the number of false objects (false positive) in the image, and iv) feature values of segmented objects. Goumeidane et al. [53] proposed an empirical discrepancy method that relies on the position of missegmented pixels ii), but excluding the features i), iii), and iv). Still, they obtained a reasonable measure of discrepancy between a segmented region and a reference region by a spatial overlay of these. In [2], the discrepancy measure was defined by \((\{A_1 \cup A_2\} \setminus \{A_1 \cap A_2\}) / (\#A_1) \times 100\). \(A_1\) is the volume produced by manual segmentation and \(A_2\) is the corresponding volume resulting from the automated segmentation. Our method is a related region differencing approach comparing all pairs of segmented regions, one taken from the “true” manual segmentation \(P^m\) and the other from the automated segmentation.

Fig. 8. 3-D segmentation. From left to right, the original image, the filtered and ridge enhanced image, the watershed segmentation, and the level set segmentation.

Fig. 9. Ridge following for cell segmentation. The filled circles in (a) are automatically generated starting points for the ridge following, which was applied to the image in Fig. 7(a). The solid lines in (a) represent the binary segmentation resulting from the ridge following. Clearly, some lines are not part of the true cell border, but these are removed by morphological closing of each connected component in the black regions, resulting in the final segmentation (b).
(R^m), closely related to the framework of segmentation evaluation described earlier (e.g., Udupa et al. [54]). Our method incorporates criteria i) and iii), using the number of missegmented pixels and penalizing false positive and negative objects. To be more specific, let \( \Omega \) be the whole image region and denote by \( R^m \) the ground-truth segmented image obtained from manual delineation. Let \( R^m_i \) consist of \( I \) disjoint, constant valued regions \( \bigcup_{i=1}^{I} R^m_i \) taking pixel values \( f^m(x) = b_i \in \{0, 1\} \), \( \forall x \in R^m_i \) and \( f(x) = 0 \) if \( x \in \Omega \setminus \bigcup_{i=1}^{I} R^m_i \), i.e., background is assigned the value zero. In contrast to a binary function, this graded assignment allows the human expert to express a global degree of uncertainty into an identified object \( R^m_i \). Moreover, let \( \{R^m_i\}_{i=1}^{I} \) denote \( J \) disjoint regions in \( R^m \) obtained by the automated segmentation applied to the input image. Assume each pixel \( x \in R^m_i \) is mapped to a value \( f^a(x) \in \{0, 1\} \), allowing a probabilistic automated segmentation. Again, the background is assigned zero, i.e., \( f^a(x) = 0 \) if \( x \in \Omega \setminus \bigcup_{i=1}^{J} R^a_i \). Let \( O^m_i \) = \( R^m_i \cap R^a_j \) and \( U^m_i \) = \( R^m_i \cup R^a_j \) denote the region of overlap and union between \( R^m_i \) and \( R^a_j \), respectively. Let \( f^m(x) \equiv f^m(x) - f^a(x) \). We then define a \( I \times J \) similarity matrix \( A^\text{union} \) containing elements

\[
A^\text{union}_{ij} = \frac{\sum_{x \in O^m_i \cap O^a_j} (1 - f^m(x))}{\sum_{x \in R^m_i \cap O^a_j} f^m(x) + \sum_{x \in O^m_i \cap O^a_j} (1 - f^m(x)) + \sum_{x \in R^m_i \cap O^a_j} f^a(x)}, \tag{9}
\]

Note that \( A^\text{union} \in [0, 1] \). Each such element reflects the amount of agreement between a manual and an automated segmented region (see Fig. 10 for examples), where both degree of overlap and nonoverlap between region \( R^m_i \) and \( R^a_j \) are taken into account, as well as the degree of uncertainties of manual and automated segmentations. If \( R^m_i \) is well represented by \( R^a_j \), \( R^m_i \approx R^a_j \), then \( A^\text{union}_{ij} \rightarrow 1 \), else \( A^\text{union}_{ij} \rightarrow 0 \). There are other possible alternatives to \( (9) \). The denominator can for instance be scaled to the total intensity value of either the two regions \( R^m_i \) or \( R^a_j \),

\[
A^\text{union}_{ij} = \frac{\sum_{x \in O^m_i} (1 - f^m(x))}{\sum_{x \in R^m_i} f^m(x)} \quad \text{and} \quad A^\text{union}_{ij} = \frac{\sum_{x \in O^a_j} (1 - f^m(x))}{\sum_{x \in R^a_j} f^a(x)}, \tag{10}
\]

Assume \( f^a \) and \( f^m \) are nonprobabilistic, binary functions taking values in \( \{0, 1\} \), i.e., \( f^a \) and \( f^m \) are characteristic functions of \( R^a_i \) and \( R^m_i \), respectively. Then, \( (9) \) and \( (10) \) reduce to \( A^\text{union}_{ij} = |O^m_i|/|U^m_i| \), \( A^\text{union}_{ij} = |O^m_i|/|R^m_i| \), and \( A^\text{union}_{ij} = |O^m_i|/|R^m_i| \) which is a measure of the relative volume of overlap between the manually and automatically segmented regions.

\( A^\text{union}_{ij} \) and \( A^\text{union}_{ij} \) are jointly capable of distinguishing between under- and over-segmentation. In the case of over-segmentation, a situation that could imply \( R^m_i \subset R^a_j \), \( A^\text{union}_{ij} \rightarrow 1 \) but \( A^\text{union}_{ij} \) will obtain a significantly lower value. A similar argument holds for under-segmentation. Now, let \( A^\text{union}_{ij} \) represent our choice of similarity measure since it takes into account both under- and over-segmentation. An illustration of this approach is shown in Fig. 10. Each area (volume in 3-D) inside solid lines represents the reference solution \( R^m_i \) and the corresponding area (volume in 3-D) inside dashed lines denotes the automatically segmented region \( R^a_j \). Using \( (9) \), the segmentation in \( (c) \) attains the highest value of \( A^\text{union}_{ij} = 0.91 \) compared to \( (a), (b), \) and \( (d) \), in agreement with human perception. In the case of real cell images [Fig. 11(a)], automatically segmented regions (Fig. 11(b)–(f), white regions) and the ground-truth regions (Fig. 11(b)–(f), gray lines) are shown with their corresponding highest similarity measures. The similarity measure \( A^\text{union}_{ij} \) is calculated for all pairs of regions \( R^m_i \) and \( R^a_j \) in Fig. 11(b) and inserted into the 4 \( \times \) 5 similarity matrix \( A \), each row corresponding to a single region from the ground truth image, and each column representing one region from the automatically segmented image

\[
A = \begin{bmatrix}
0.007 & 0 & 0 & 0 & 0 \\
0 & 0.663 & 0 & 0 & 0 \\
0.003 & 0 & 0.861 & 0 & 0 \\
0 & 0 & 0 & 0.678 & 0.239
\end{bmatrix}. \tag{11}
\]

Evidently, the matrix \( A \) may consist of more than one nonzero entry per row and column. This is a problem that is related to degeneracy [45]. Furthermore, empty columns and empty rows represent over- and under-segmentation, respectively. Such situations must also be taken care of properly. The values typeset in bold denote those elements with higher values along each row and column, chosen to represent the evaluation in this case. However, in the general case of a similarity matrix \( A \), the choice of such elements might not be unique. We propose a solution to this problem, which would be to establish a one-to-one map between maximal subsets between \( \{R^m_1, \ldots, R^m_I\} \) and \( \{R^a_1, \ldots, R^a_J\} \) by creating a \( I \times J \) matrix \( B \) consisting of \( K = \min(I, J) \) nonzero entries \( A_{i_k, j_h} \) for \( k = 1, \ldots, K \) from \( A \) providing the highest Frobenius norm

\[
\max_{k=1,\ldots,K} \left\| B \right\|_F = \sqrt{\sum_{i_k, j_h} |B_{i_k, j_h}|^2} = \sqrt{\sum_{i_k, j_h} |A_{i_k, j_h}|^2} \tag{12}
\]
The desired one-to-one map must conform to the requirements that $B$ can have at most one nonzero entry per row and per column, thus coping with the problem of degeneracy. False objects will give rise to columns with zeros in $B$, accounting for criterion iii). The optimization in (12) is accomplished by first letting $B = A$, and then iterate through all elements in $B$ in decreasing order. For each iteration the element is removed if there exists a larger component in the same row or column. If not, the element remains unchanged. Then, by construction, the largest possible Frobenius norm of $B$ is obtained, satisfying the constraints. The optimization may create empty rows or columns in $B$, corresponding to under-segmentation and over-segmentation, respectively. The overall similarity measure for the image is obtained by summing all elements in the derived matrix $B$, after each of them has been scaled to $N = \max\{\sum_{i=1}^{J}|R_{i}^{m}|, \sum_{j=1}^{J}|R_{j}^{a}|\}$, i.e., the maximum number of pixels of the automated or the manual solution. This scaling is performed in order to ensure that large regions will influence our similarity measure $SM$ more than small regions. The final similarity measure $SM$ is calculated as the sum of $B_{ij}$, scaled by the relative number of pixels $\frac{N_i}{N}$ in each manually segmented region

$$SM = \sum_{i=1}^{M} B_{i} \cdot \frac{N_i}{N}. \quad (13)$$

By this definition, $0 \leq SM \leq 1$ where $SM \rightarrow 0$ indicates a poor segmentation and $SM \rightarrow 1$ denotes an excellent segmentation. The relations between $SM_{\text{man}}$, $SM_{\text{aut}}$, and $SM_{\text{union}}$ are capable to distinguish between over- and under-segmentation, summarized in Table I.

### F. Preparation of the Microscopic Images

The described automated cell segmentation method was tested on images of PC12 cells (rat pheochromocytoma cells, clone 251, Heumann et al. [55] and NRK cells (normal rat kidney cells, Mrs. M. Freshney, Glasgow, U.K.). PC12 cells were cultured as already described [56]. NRK cells were cultured in DMEM supplemented with 10% fetal calf serum. Transfection of NRK cells was accomplished by electroporation as described [56]. The PHD-YFP cDNA construct is described elsewhere [57]. For high-resolution fluorescence microscopy, cells were plated in LabTek chambered coverslips (Nalge Nunc International, Wiesbaden, Germany). For the experiments in which the effect of thymidine on cellular size and morphology was investigated, PC12 cell monolayers in LabTek chambers were maintained in growth medium containing 4 mM thymidine (Sigma) for 24 h (block of cell division), further incubated in medium without thymidine for 24 h (release of block) and finally imaged by wide field fluorescence microscopy (see below). In the control condition, fresh growth medium without thymidine was used for the blocking step. Cell monolayers were stained with wheat germ agglutinin (WGA) conjugated to Alexa Fluor dye. To obtain a 3-D matrix of cells, PC12 and NRK cells were embedded in agarose. Briefly, low melt agarose (Carl Roth GmbH) was prepared in a 2% (w/v) solution in DMEM 10% FCS and melted at 70 °C. The solution was allowed to cool down to 45 °C for 15 min. Pellets of approximately $4 \times 10^7$ or $4 \times 10^6$ of PC12 or NRK cells,
respectively, were loosely resuspended in 500 µl of growth medium supplemented with WGA-Alexa Fluor. In experiments in which transfected cells were analyzed, no WGA-Alexa Fluor was added to the cell suspension. 100 µl of the cell suspension were mixed with 100 µl of the molten agarose solution, the mixture was plated in a Labtek and incubated at 4°C for 5 min to let the agarose solidify. Imaging was performed immediately thereafter. Confocal microscopy was performed either with a spinning-disc imaging setup (PerkinElmer Ultra View TMRS Live Cell Imager, PerkinElmer Life and Analytical Sciences, Boston, MA) or with a Leica TCS SP5 confocal microscope (Leica Microsystems, Mannheim, Germany). Imaging by wide field fluorescence microscopy is described in [58]. For both the wide field and confocal imaging setups, the cells were analyzed in 3-D by acquiring single focal planes 300–500 nm apart from each other in the z-direction spanning the whole cellular volume.

III. RESULTS

The watershed segmentation and level set segmentation have been compared to a manual ground-truth to evaluate the segmentation quality. Several experiments were performed on two different cell lines, two types of cell surface staining were used and imaging was performed with three different kinds of microscopy. The experimental parameters used in each case are summarized in Table II, showing the experiment name, the cell type, the fluorescent marker used for plasma membrane labeling and the microscopy method is indicated. All manual and automated segmentation was performed in 3-D, as well as the segmentation evaluation.

<table>
<thead>
<tr>
<th>Experiment</th>
<th>Cell type</th>
<th>Fluorescent marker</th>
<th>Microscopy technique</th>
</tr>
</thead>
<tbody>
<tr>
<td>A</td>
<td>PC12</td>
<td>WGA-Alexa Fluor®</td>
<td>Widefield</td>
</tr>
<tr>
<td>B</td>
<td>NRK</td>
<td>WGA-Alexa Fluor®</td>
<td>Confocal spinning disc</td>
</tr>
<tr>
<td>C</td>
<td>NRK</td>
<td>WGA-Alexa Fluor®</td>
<td>Confocal</td>
</tr>
<tr>
<td>D</td>
<td>NRK</td>
<td>PHD-YFP</td>
<td>Confocal</td>
</tr>
<tr>
<td>E</td>
<td>PC12</td>
<td>PHD-YFP</td>
<td>Confocal</td>
</tr>
<tr>
<td>F</td>
<td>PC12</td>
<td>WGA-Alexa Fluor®</td>
<td>Widefield</td>
</tr>
</tbody>
</table>

A. Segmentation of WGA-Alexa Fluor Stained PC12 Cells Imaged by Wide Field Microscopy

PC12 cells were surface-stained with WGA-Alexa Fluor and imaged in 3-D by wide field microscopy. From most optical planes through the cell, images with sharp and distinct borders were obtained. Only those planes close to the top and the bottom of the spheroidal-shaped cells resulted in images with fuzzy cell boundaries. This is due to the fact that in these regions a large portion of the plasma membrane runs almost parallel to the optical plane [Fig. 12(a)]. The obtained cells exhibit challenging variations in shape and brightness and in some cases a discontinuous staining of the plasma membrane occurred. Furthermore, the displayed cells contain various amounts of punctuated, high intensity structures inside the cytoplasm as a result of endocytosed plasma membrane. These structures, known as endosomes, could be easily mistaken as cell border by the automated method (not shown). Representative images from one of the obtained 3-D-stacks at different z-elevations are shown in Fig. 12(a)–(c) together with corresponding slices taken from the 3-D watershed segmentation (d)–(f), the level set segmentation (g)–(i), and the manual solution (j)–(l). The segmentation quality is high, indicating that plasma membrane-stained PC12 cells, due to their spheroidal shape, are suitable for automated 3-D segmentation. The comparative results from the statistical analysis of 24 cells used for assessment are summarized in Table III, row A. High success rates of up to 96% and 92% work required for the manual delineation, approximately up to 20 cells were randomly chosen to represent each experiment (A-E) in the final segmentation evaluation. Every cell in the segmentation evaluation which had at least 10% of its border connected to the image border was removed from the analysis since those cells had a significantly corrupt shape. Experiments A and C were evaluated with nonprobabilistic characteristic functions \( f(x)^\text{A}, f(x)^\text{C} \in [0,1] \). Experiments B, D and E were evaluated using probabilistic functions \( f(x)^\text{B}, f(x)^\text{D}, f(x)^\text{E} \in [0,1] \) because the images of these experiments included a certain amount of apoptotic and possibly dead cells responsible for an uncertainty in the manual segmentation. Each image produced a separate set of similarity measures, \( SM_{\text{manual}}, SM_{\text{A}}, \) and \( SM_{\text{D}} \). To evaluate the whole experiment consisting of several images, each similarity measure was scaled by the relative number of manually detected cells in the image to which it belonged to, and then summed over all images in the experiment to obtain an overall similarity measure. Experiment F was performed to test whether the algorithm could detect small changes in cell size caused by a thymidine mediated block of the cell cycle [59]. No ground-truth was here constructed since this was a high-throughput experiment including as many as 1239 automatically segmented cells. All experiments were carried out on randomly chosen cells in order to be close to realistic experimental conditions. The program code used for segmentations was implemented in MATLAB, intensively vectorized to save computational time and executed on a Linux workstation. To avoid overoptimistic results, the method and parameter settings were developed on a separate data set not used for the final evaluation. (The code could be available upon request by contacting the corresponding author.)
Fig. 12. Segmentation of WGA-Alexa Fluor-stained PC12 cells imaged by wide field microscopy. Raw data (a)–(c), watershed segmentation (d)–(f), level sets (g)–(i), and manual segmentation (j)–(l). The images are shown at $z$-elevations of 75%, 50%, and 25%.

### TABLE III
NUMERICAL RESULTS FROM 3-D AUTOMATED DETECTION OF NRK AND PC12 CELLS. THE WATERSHED ALGORITHM AND THE LEVEL SETS BOTH OBTAINED HIGH SUCCESS RATES AND ARE THUS COMPARABLE

<table>
<thead>
<tr>
<th>Segmentation method</th>
<th>$n_{man}$</th>
<th>$n_{aut}$</th>
<th>$SM_{man} (%)$</th>
<th>$SM_{aut} (%)$</th>
<th>$SM_{union} (%)$</th>
</tr>
</thead>
<tbody>
<tr>
<td>A</td>
<td>Watershed</td>
<td>24</td>
<td>24</td>
<td>96</td>
<td>91</td>
</tr>
<tr>
<td></td>
<td>Level set</td>
<td>24</td>
<td>24</td>
<td>92</td>
<td>87</td>
</tr>
<tr>
<td>B</td>
<td>Watershed</td>
<td>24</td>
<td>22</td>
<td>91</td>
<td>88</td>
</tr>
<tr>
<td></td>
<td>Level set</td>
<td>24</td>
<td>23</td>
<td>93</td>
<td>87</td>
</tr>
<tr>
<td>C</td>
<td>Watershed</td>
<td>21</td>
<td>21</td>
<td>90</td>
<td>97</td>
</tr>
<tr>
<td></td>
<td>Level set</td>
<td>21</td>
<td>22</td>
<td>78</td>
<td>89</td>
</tr>
<tr>
<td>D</td>
<td>Watershed</td>
<td>24</td>
<td>21</td>
<td>79</td>
<td>85</td>
</tr>
<tr>
<td></td>
<td>Level set</td>
<td>24</td>
<td>20</td>
<td>79</td>
<td>70</td>
</tr>
<tr>
<td>E</td>
<td>Watershed</td>
<td>8</td>
<td>8</td>
<td>89</td>
<td>92</td>
</tr>
<tr>
<td></td>
<td>Level set</td>
<td>8</td>
<td>8</td>
<td>95</td>
<td>81</td>
</tr>
</tbody>
</table>

were obtained for the watershed and the level sets, respectively. Thus, the two methods were comparable for this experiment. $SM_{man} > SM_{aut}$ for both segmentation methods, arising from more over- than under-segmentation.

B. Segmentation of WGA-Alexa Fluor Stained NRK Cells Imaged by Confocal Spinning-Disc Microscopy

In contrast to spheroidal PC12 cells, NRK cells possess a broad and flat periphery surrounding the centered nucleus, which results in a protuberance of the plasma membrane (Fig. 13, drawing). Wide field microscopy of such cells results in images displaying blurred cell borders (not shown), inappropriate for automated segmentation. To overcome this problem, confocal imaging techniques were applied. In this way only light from the respective focal planes is recorded during image acquisition. Images taken from one stack at different $z$-elevations are shown in Figs. 13(a)–(c) together with corresponding slices from the watershed segmentation (d)–(f), the level set segmentation (g)–(i), and the manual segmentation (j)–(l). High success rates were achieved, up to 91% for the watershed and 93% for the level sets, see Table III, row B. Thus the two methods had comparable performance for this data set. The numbers indicate a higher amount of over- than under-segmentation since $SM_{man} > SM_{aut}$. The major segmentation errors occurred in the lower planes due to the flat morphology and weak signal of the NRK cells at this level, causing the automated methods to flood further down in the stack compared to the manual ground-truth, thus creating over-segmentation.

C. Segmentation of WGA-Alexa Fluor Stained NRK Cells Imaged by Confocal Point-Scanning Microscopy

In this experiment, 3-D image stacks of WGA-Alexa Fluor stained NRK cells were acquired by confocal point-scanning microscopy. The respective images display cells with distinct cell borders [Fig. 14(a)–(c)] which are suitable for automated segmentation in 3-D. A 3-D segmentation revealed high success rates of up to 97% for watershed segmentation and 89% for level sets, shown in Table III, row C. In this experiment, the watershed segmentation had a higher success rate than the level set approach. For both methods, $SM_{aut} > SM_{man}$, resulting from under-segmentation. Most under-segmentation occurred in the lower planes where the NRK cells exhibit fuzzy borders. This...
complicated the segmentation [Fig. 14(c)] in a similar way as for the images taken by the confocal spinning disc microscopy.

D. Segmentation of PHD-YFP-Expressing NRK Cells Imaged by Confocal Point-Scanning Microscopy

Surface-staining of cells with WGA-Alexa Fluor is only applicable for automated segmentation if the dye molecules have access to the plasma membrane of the cell. This may be problematic for tissue due to the limited diffusion of molecules through the extracellular matrix. Therefore, the use of genetically encoded fluorescent molecules would be advantageous. To address this issue, we expressed in NRK cells the pleckstrin-homology domain (PHD) of phospholipase C fused to the yellow fluorescent protein (YFP) and imaged them by confocal point-scanning microscopy. PHD-YFP is specifically targeted to the cell periphery after expression in mammalian cells [57], [60] and does not lead to fluorescent endocytic structures as in the case of WGA-Alexa Fluor. This revealed a prominent cell membrane labeling of PHD-YFP expressing cells (Fig. 15(a)–(c), slices from a 3-D stack). However, not all cells were transfected (not shown), and the expression level varied from cell to cell. The latter resulted in cells exhibiting weak signals (Fig. 15(c), compare the cells in this plane). Cells with low signal intensity represent a great challenge for any automated segmentation. Therefore, one should keep in mind that due to the variable degree of protein expression and the restricted dynamic range of the imaging system not all positive cells can be adequately segmented from a 3-D stack. The automated watershed segmentation of the images in Fig. 15(a)–(c) is shown in Fig. 15(d)–(f) and the corresponding images from the level sets and the manual segmentation are shown in Fig. 15(g)–(i) and (j)–(l), respectively.

A 3-D segmentation reveals success rates of up to $SM_{\text{aut}} = 85\%$ for watershed approach and $SM_{\text{man}} = 79\%$ for the level sets using probabilistic functions $f^m(\mathbf{x})$ and $f^a(\mathbf{x})$. The numerical results are shown in Table III, row D, revealing satisfying success rates and therefore indicating that the segmentation algorithms are also suitable for PHD-YFP expressing cells in addition to WGA-Alexa Fluor-stained cells and thus independent.
of the type of cell border labeling. The number of manually segmented cells (24) is larger than the number of automatically segmented cells (21 and 20), representing an under-segmentation. The current experiment had the lowest success rate in our work, probably due to a certain amount of weakly expressing cells.

E. Segmentation of PHD-YFP-Expressing PC12 Cells Embedded in Agarose and Imaged by Confocal Point-Scanning Microscopy

To create a tissue-like configuration we plated cells in agarose and tested whether the segmentation was capable of a tissue-like segmentation of cells with surface staining. The images in the first column of Fig. 16 show focal planes of z-heights 10%, 25%, 40%, 55%, 70%, and 85%. Fig. 17 shows the xz and yz views along the dashed lines in the original image (A) and the ridge enhanced image (B), respectively. Note how the ridge enhancement filter increases the contrast, even with a high degree of anisotropy with pixel dimensions of $0.096 \times 0.096 \times 1 \, \mu\text{m}^3$.

The watershed transform, the level set, and the manual ground-truth are shown in the second, third, and last column, respectively. The results from the segmentation evaluation are displayed in Table III, row E. Three-dimensional views of the watershed and level set segmentation are depicted in Fig. 18. Note that only a fraction of the cells were transfected in the agarose matrix, thus leading to a relatively sparse density of fluorescently labeled cells in 3-D. A higher density of fluorescently labeled cells can be expected in tissue from transgenic animals, along with a larger diversity of cells. Future experiments are therefore needed to explore the segmentation of real tissue.
more elongated upon a certain treatment, or the mean cell intensity could be measured in a second image channel to obtain the concentration of a certain drug or protein.

G. Comparing the Methods for 3-D Segmentation

For the cell segmentation we have thoroughly compared two entirely different methods for segmentation of surface stained cells, the watershed transform and a level set model. Five experiments were conducted for comparison, including two different cell types, three different microscopes, and two unlike methods for cell surface markers (Sections III-A–III-F). All experiments reveal high success rates above 70% for both methods, except from (D) where the level set had the lowest success rate of \( SM_{\text{union}} = 61\% \). Comparing \( SM_{\text{union}} \) for all experiments, the watershed algorithm has a slightly higher performance than the level set. This difference was mostly due to breakthrough of the level set in regions of weakly stained plasma membrane, thus flooding into the background. The amount of flooding can be adjusted in the setup, however, this may result in poor convergence inside the cells around the high-signaled, endocytosed plasma membrane, thus preventing the zero level set from reaching the plasma membrane. The watershed algorithm is normally also significantly faster than the level sets with a factor of \( \times 100 \). On the other hand, the level set model has a smoothing term, an important advantage compared to the standard watershed. Due to the preprocessing step of filtering in this work, the watershed algorithm did not suffer significantly from oscillating boundaries. It is also possible to combine the watershed algorithm and level sets by initializing the level set by the watershed regions, thus saving computational time and at the same time avoiding oscillating boundaries.
IV. DISCUSSION AND CONCLUSION

Automated segmentation methods become increasingly important in cytometry and permit high-throughput analysis of cells. In this way statistically relevant information of biological processes occurring at the single cell level can be obtained. In the past, whole cell segmentation has mainly been performed in 2-D and was applied to fixed cells [13], [21], [23]. Automated segmentation of living instead of fixed cells has the capacity to provide information on cell dynamics. The present work describes a unified framework for 3-D segmentation of surface-stained, living cells. In addition, a comprehensive method for segmentation evaluation is presented, which demonstrates the performance and versatility of the compared segmentation algorithms. The usefulness and sensitivity of automated segmentation became most obvious in Experiment F, Section III, in which the program was able to detect a small but significant increase in cell volume upon treatment with thymidine. These slight changes, ranging from 14% to 23%, were not evident from visual inspection of the images. This striking example demonstrates that the automated watershed segmentation is capable of revealing subtle but important changes in cell parameters as they may occur during the exposure of cells to environmental influences as drugs and toxins.

For many applications the segmentation of surface-stained cells is superior to the segmentation of nuclei and cytoplasmically stained cells, because it is able to detect whole cells in closely packed arrangements like confluent cell cultures or tissue [13], [21], [23]. A robust cell segmentation was obtained by first performing a filtering step. Several unlike approaches for filtering were compared, linear and nonlinear spatial filters as well as PDE-based models. The results showed that typical edge-enhancing filters and linear smoothing filters were less suitable to smooth the ridges compared to coherence-enhancement filters [27], [47] and the nonlinear directional coherence enhancement filter [2]. After the filtering, a ridge enhancement was applied to the filtered image, which resulted in images showing pronounced ridges of which the majority are cell borders. Two methods for ridge enhancement were compared, the Hessian [34] and our related method, ridge enhancement by curvature. They showed comparable results, producing ridges of high contrast. The ridge enhancement in turn enables adaptive thresholding and morphological filling as a reliable and automated method to define marker regions for a marker-controlled watershed segmentation or a level set segmentation. Defining the markers is the most crucial step in the segmentation procedure, since there should be exactly one marker inside each object of interest. In this respect further improvement of the success rate may be obtained by nucleus staining and subsequent use of this information for creating a high-quality marker image as it has been demonstrated for fixed biopsy tissue [23].

The framework for segmentation was extensively tested on cell images from two cell lines with distinct morphologies, using two different types of plasma membrane labeling, and acquired by three types of microscopy. For simplicity, we decided to apply our first choice for preprocessing of the images, the directional coherence enhancement filter and ridge enhancement, for the extensive comparison of the watershed and the level set models in Section III. The segmentation method revealed high success rates when applied to the data sets of fluorescence images displaying cells with distinct margins. In the case of PC12 cells displaying sharp cell boundaries, success rates up to was 96% were obtained compared to manual segmentation. For NRK cells a value up to 97% was obtained. However, segmenting NRK cells is more complicated than segmenting PC12 cells due to the flat morphology. It follows that one of the most important prerequisites to obtain images displaying pronounced cell borders is that the optical plane of the imaging system is preferably perpendicular to the plasma membrane. This is easily achieved with a wide field imaging setup for the spheroidal PC12 cells (Fig. 12), while for the flat NRK cells, confocal microscopy techniques are necessary (Figs. 13–16).

In the present study a comprehensive evaluation scheme based on a region differencing approach was developed and used to assess the performance of the automated cell segmentation. The obtained segmentation evaluation reflects both over- and under-segmentation compared to a ground-truth, where the ground-truth, allowing an uncertainty factor, is acquired from manual segmentation performed by experts. In the past, segmentation evaluation of nuclei or cytoplasmically stained cells were performed using different methods, which makes a between-study comparison difficult. To improve this situation, we aimed at the development of a standardized scheme for evaluation of cell segmentation.

A crucial point for a high-quality segmentation of living cells is the type and quality of the cell border labeling. In the past, antibodies against cell surface proteins or Oregon green phalloidin labeling cortical F-actin were used to label cell borders of fixed cells [13], [21], [23]. Our data show that under optimized experimental conditions both the vital stain WGA-Alexa Fluor and the expressed fluorescent marker PHD-YFP revealed reproducible and high-quality data sets for segmentation of living cells. The advantage of WGA-Alexa Fluor is that it labels all cells and can be applied straightforward to the cell cultures shortly before the microscopic analysis. However, accurate analysis is only possible if the image acquisition takes place shortly after the cell labeling. Prolonged incubation times with WGA-Alexa Fluor lead to endocytosed plasma membrane resulting in numerous intracellular fluorescent spots, which impose a severe problem to the automated segmentation. PHD-YFP on the other hand has to be introduced into cells by a more elaborated transfection method and usually results in only a certain percentage of transfected cells. This problem can be overcome by establishing stably transfected cell lines, or in the case of segmentation of cells in tissue and whole organisms, by establishing transgenic animals. In the latter, cell surface staining by WGA-Alexa Fluor most likely fails due to the restricted diffusion of the dye through the dense extracellular matrix of tissue.

In conclusion, the established approach for automated cell segmentation represents a robust and powerful tool for the statistical analysis of various cell parameters. The experience and the experimental results of this study demonstrate that good solutions can only be obtained if biological procedures and image processing techniques are combined in an optimal way.
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