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A Dividerless PLL With Low Power and Low Reference Spur by Aperture-Phase Detector and Phase-to-Analog Converter

Deyun Cai, Haipeng Fu, Student Member, IEEE, Junyan Ren, Member, IEEE, Wei Li, Member, IEEE, Ning Li, Member, IEEE, Hao Yu, Member, IEEE, and Kiat Seng Yeo, Senior Member, IEEE

Abstract—A 2.1-GHz dividerless PLL with low power, low reference spur and low in-band phase noise is introduced in this paper. A new phase detection mechanism using aperture-phase detector (APD) and phase-to-analog converter (PAC) generates an analog voltage in proportion to the phase error between reference and VCO, and then controls the current amplitude of the following charge pump (CP). The charging and discharging currents in the proposed CP have equal pulse width and equal small amplitude in locked state, which reduces the reference spur and power consumption of the CP effectively. Moreover, compared to the conventional CP with the same bias current in locked state, the proposed CP can contribute a much lower noise to the PLL output. In addition, a method of tunable loop gain with theoretical analysis is introduced to reduce the PLL output jitter. The proposed PLL is fabricated in a standard 0.13-μm CMOS process. It consumes 2.5 mA from a 1.2-V supply voltage and occupies a core area of 0.48 mm × 0.86 mm. The reference spur of the proposed PLL is measured to be −80 dBc/−74 dBc and an in-band phase noise of −103 dBc/Hz at 100 kHz offset is achieved.

Index Terms—Aperture-phase detector, clock generation, dividerless, dual-loop, jitter, low in-band phase noise, low power, low reference spur, phase locked loop (PLL), phase-to-analog converter.

I. INTRODUCTION

The growing demands for PLL designs with low power, low reference spur and low phase noise have been explored recently for varieties of applications such as frequency synthesizers, communication systems and RF transceivers. The classical single-loop PLL [1]–[3] is shown in Fig. 1, which consists of a phase/frequency detector (PFD), a charge pump (CP), a loop filter (LF), a voltage controlled oscillator (VCO), and a frequency divider with a division ratio of $N$. In the classical PLL, the VCO dominates the out-of-band phase noise while CP and divider dominate the in-band phase noise. In the PLL feedback system, the closed-loop transfer function of CP noise is in inverse proportion to the gain from PLL output to the CP output current, which is defined as a feedback gain of CP ($\beta_{CP}$) [4]. A larger $\beta_{CP}$ means the same CP current will contribute less phase error to the PLL output, namely, more CP noise can be suppressed. The in-band CP noise is suppressed by $\langle \beta_{CP}\rangle^2$ when transferred to the PLL output [4]. The block diagram and the characteristic of classic PFD/CP are shown in Fig. 2. PFD output pulse widths are converted to the switch-on time of CP as an average over one reference cycle. The averaging function over a reference cycle introduces the mechanism of divide-by-$N$ in the feedback path. The $\beta_{CP\ CON}$ of the conventional PLL is given by

$$\beta_{CP\ CON} = \frac{\Delta i_{CP\ CON}}{\Delta \phi_{VCO}} \cdot \frac{i_{CP\ CON} \cdot \Delta \phi_{DIV}}{2\pi} = \frac{i_{CP\ CON}}{2\pi N} \cdot \frac{1}{N} \tag{1}$$

where $i_{CP\ CON}$ is the amplitude of CP current. Therefore, CP noise power is multiplied by $N^2$ when transferred to the PLL output. Larger $i_{CP\ CON}$ is beneficial to achieve larger $\beta_{CP\ CON}$, but simultaneously increases thermal noise and power consumption of CP itself. Furthermore, as described in Fig. 3, the PFD converts the phase error between REF and DIV into the charging ($I_{up}$) and discharging ($I_{dn}$) currents according to the switch-on time difference of $(t_{up,n} - t_{dn,n})$. In case that $I_{up}$ and $I_{dn}$ mismatch, one of them has to be switched on for a longer time until the charge is zero at CP output node, and then steady state condition can be achieved [5]. This causes output current ripple and leads to a high reference spur. In order to reduce the reference spur in classical PLL, rail-to-rail amplifiers are usually used to reduce the mismatch of CP charging and discharging currents [6]–[8]. This increases design complexity, noise, area and consumes significantly larger current. In summary, the classical single-loop PLL entails a difficult trade-off among power, noise, spur and design complexity.

By contrast, a dual-loop PLL has advantage to balance different specifications such as noise and power by new phase...
detectors [4], [9], spur and power by dual-path tuning control VCOs [10]–[12]. The dual-loop dividerless PLL in [9] incorporating a phase detector that operates on a windowing technique eliminates the need for frequency divider, and hence the power and noise contributions from divider are eliminated. However, as the phase detection mechanism remains the same with the conventional CP, CP noise contribution is still multiplied by $N^2$. The mismatch in CP still leads to a high reference spur. The dual-loop sub-sampling PLL in [4] reduces the in-band phase noise with low power consumption. Due to the sub-sampling phase detector, no divider is needed in the locked state and the CP noise is not multiplied by $N^2$. However, the disturbances of VCO by the sampler switching activity cause high spur and can possibly make the PLL out of lock. Since the spur is proportional to the VCO gain [13], the dual-loop PLLs in [10], [11] using two CPs and a dual-control VCO are presented to reduce spur and VCO noise due to the reduced VCO gain. The dual-loop PLL in [12] is the extension of the previous works in [10], [11], which employs only one CP with low VCO gain and extended fine-tuning range to reduce spur. The PLLs in [10]–[12] achieve a low spur without rail-to-rail amplifiers. Thus the power consumption of the amplifiers can be avoided. However, due to the switch-on-time controlled CP as conventional PLL, CP and divider noise contributions are still multiplied by $N^2$, which leads to high in-band phase noise of the PLL.

To overcome the aforementioned drawbacks, we describe our proposed PLL topology [14] by aperture-phase detector (APD) and phase-to-analog converter (PAC) to reduce noise, spur and power simultaneously.

Firstly, for the new CP circuit, equal pulse width of charging and discharging currents and equal small amplitude [5] in locked state are designed for achieving low reference spur and low power. Secondly, compared with the classical PLL and the dividerless PLL in [9], the proposed one can reduce the CP noise contribution by increasing the CP feedback gain dramatically. Thirdly, due to the introduction of APD, the dividers in the proposed PLL can be powered off in locked state, eliminating the power and noise contributions from the dividers. Finally, there is no need to design rail-to-rail amplifiers in the CP, which reduces the design complexity and power consumption. Therefore, the proposed PLL can achieve a good trade-off among power, noise, spur and design complexity.

The organization of this paper is as follows. Section II introduces the PLL topology with the loop noise analysis. Section III describes the details of the circuit level design and implementation. Experiment results and discussions are shown in Section IV and conclusions are drawn in Section V.

II. PLL TOPOLOGY AND LOOP NOISE ANALYSIS

General design considerations to the operation of the proposed dual-loop PLL, loop noise analysis, loop parameters design and optimization of PLL phase noise are discussed in this section.

A. Dual-Loop PLL Topology

Fig. 4 shows the block diagram of the proposed dual-loop PLL. The main loop consists of APD, PAC, CP1, third-order LF, VCO, differential-to-single (D2S) and inverter chain. The differential sine-wave outputs of VCO are converted into single-ended steep square-wave (VCO,BUF) for phase detection by the D2S and inverter chain. A frequency locked aid (FLA) loop is added to ensure a correct frequency locking, eliminating the concern of locking in a sub-harmonic mode [4], [9]. The FLA shares the LF and VCO with the main loop. Similar to the classical PLL, FLA uses a divider and PFD/CP, except that a deadzone (DZ) creator is inserted between PFD and CP2 [4].

At the beginning of the frequency acquisition process, FLA senses the phase error between REF and DIV, and the main loop senses the phase error between REF and VCO at the same time. However, FLA overrules the main loop due to its higher gain. When the phase/frequency error between REF and VCO is small enough, the DZ creator closes the CP2 in FLA automatically. Then the main loop dominates the final locking process, which determines the phase noise, reference spur and power consumption of the PLL. After phase locking, CP2 and divider in FLA have no influence on the main loop and do not introduce noise any more, which can be turned off to save power. In the dynamic locking process, the FLA plays a role of coarse tuning and the main loop plays a role of fine tuning. FLA adjusts the VCO frequency close to $N$ times REF frequency, and then the main loop makes the VCO align with REF in the final locking process. Combining with the two loops, we can achieve the locking correctly.

In contrast to the previous dual-loop PLL designs [4], [9], the proposed PLL in this paper can improve the performance from the following perspectives. Firstly, both the sub-sampling CP and the proposed CP are inherently amplitude controlled CPs, which intend to cause small current ripple at the CP output node and lead to low spur [5]. However, the phase detector in the sub-sampling PLL directly samples the sine-wave output voltage of the VCO, which disturbs the VCO operation and causes high reference spur. To avoid such problem, the phase detector introduced in our PLL generates a shaped voltage signal through APD and PAC instead of directly sampling the VCO output. As
Fig. 4. Block diagram of the proposed dual-loop PLL.

a result, the reference spur can be reduced by the proposed PLL. Secondly, the shaped voltage generated by APD and PAC can improve the stability of the PLL. Thirdly, the proposed PLL can reduce the CP noise contribution dramatically compared with the dividerless PLL in [9] and can also reduce the power consumption of CP.

The main loop directly senses the phase error between REF and VCO in a time window by the proposed APD, and then the PAC generates an analog voltage in proportion to the phase error to control the output current amplitude of CP. Fig. 5(a)–(c) shows the transfer curves of APD, PAC and CP circuits, respectively.

The pulse width of the APD output is proportional to \( \Delta \phi_{\text{vco}} \). The gain of APD is given by

\[
K_{\text{APD}} = \frac{\Delta t}{\Delta \phi_{\text{vco}}} = \frac{T_{\text{vco}}}{2\pi} = \frac{1}{\omega_{\text{vco}}} \tag{2}
\]

Then PAC converts the output pulse signals of APD into analog voltage signals and then controls the amplitude of the CP current. The gain of PAC is calculated as

\[
K_{\text{PAC}} = \frac{\Delta v}{\Delta t} = \frac{V_{\text{max}}}{T_{\text{vco}}/2} \tag{3}
\]

where \( V_{\text{max}} \) is the maximum voltage of PAC. The gain of CP is given by

\[
K_{\text{CP}} = \frac{\Delta i_{\text{cp}}}{\Delta v} = g_m \tag{4}
\]

where \( g_m \) is the transconductance of the transistor in the proposed CP, which can be calculated as [15]

\[
g_m = \sqrt{2\mu C_{\text{ox}} (W/L)} I_{\text{CP}} \tag{5}
\]

where \( \mu \) is the mobility of charge carriers, \( C_{\text{ox}} \) is the gate oxide capacitance per unit area, \( W/L \) is the size of the transistor and \( I_{\text{CP}} \) is the CP current amplitude. Thus, \( g_m \) is a variable that changes with the \( I_{\text{CP}} \).

Fig. 6(a) shows the conceptual schematic of APD/PAC/CP. APD directly compares the phases between REF and VCO, then obtains up and dn signals. PAC converts up/dn to analog voltage signal VP/VN and holds VP/VN for the entire reference period (ignoring the finite reset time of the PAC). Finally, CP converts VP/VN to charging current \( i_{\text{cp}} \) and discharging current \( i_{\text{dn}} \). Fig. 6(b) shows the characteristic of the proposed APD/PAC/CP, where the CP current \( \Delta i_{\text{cp}} \) is proportional to \( \Delta \phi_{\text{vco}} \). As such, the ideal locking point is achieved when \( \Delta i_{\text{cp}} \) is equal to zero. As shown in Fig. 6(b), the feedback gain \( \beta_{\text{CP,APD}} \) is always positive in the whole VCO cycle, which is preferable for the stability of PLL. By contrast, the characteristic of sub-sampling PD/CP is shown in Fig. 6(c), where \( A_{\text{VCO}} \) is the amplitude of VCO output and \( g_m \) is the transconductance of the transistor in sub-sampling CP. Note that the characteristic of sub-sampling PD/CP is ideally a sine waveform. As a result, a negative value can occur in \( \beta_{\text{CP,SSPD}} \), which worsens the loop stability and increases settling time. Similar to sub-sampling PLL, the \( \beta_{\text{CP,APD}} \) in this design also varies with the phase error. A manually tunable CP bias current has been adopted according to the
extensive PVT (process-temperature-voltage) analysis to ensure that the PLL can work well in a wide variation range.

B. Loop Noise Analysis

To demonstrate the low in-band phase noise of the main loop, a noise model is presented in Fig. 7. Here we model the proposed main loop as a time continuous system, which is valid as long as the PLL bandwidth is an order of magnitude smaller than reference frequency [4], [16]. In classical PLL and dividerless PLL in [9], the upsampling block introduces \( \frac{N-1}{N} \) zeros between successive pulses of CP current [17]. This block does not correspond to a physical circuit in the classical PLL and dividerless PLL in [9]. Instead it models the fact that the CP is activated only once in every \( N \) PLL clock cycles in order to adjust the \( \phi \), while it remains off during the rest of the time [17]. The combination of the downsampling and upsampling blocks keeps the sampling frequencies consistent around the PLL loop [17]. However, in the proposed PLL, since the PAC holds the output voltage for the entire reference period, the upsampling results in repetition of the first generated voltage instead of filling it with \( \frac{N-1}{N} \) zeros. This change in the signal processing results in a replication by the upsampling with repetition of \( \phi \), and hence the block diagram needs to include a virtual \( \frac{N-1}{N} \) in front of the input phase. Furthermore, since there is no frequency division in D2S and invert chain, the gain of the two blocks in the phase domain is regarded as one.

The noise analysis of the main loop is shown as follows. The PLL open-loop transfer function is calculated as

\[
G(s) = \beta_{\text{CP,APD}} \cdot \frac{K_{\text{VCO}}}{s} \cdot F_{\text{LF}}(s)
\]  

where \( K_{\text{VCO}} \) is the VCO gain and \( F_{\text{LF}}(s) \) is the impedance transfer function of LF. The APD gain is inversely proportional to \( f_{\text{vco}} \), which means that when \( f_{\text{vco}} \) is larger or the division ratio \( N(f_{\text{vco}}, f_{\text{ref}}) \) is larger, the APD gain will drop. Thus, the APD noise when transferred to the output will be larger for a larger \( N \). The noise contribution of the PAC can be calculated by relating the voltage noise at the PAC output. Similar to the noise analysis of CP, we can define a feedback gain \( \beta_{\text{PAC}} \) from PLL output to PAC output voltage. The closed-loop transfer function of PAC noise is shown as

\[
H_{\text{PAC}}(s) = \frac{\phi_{\text{out},n}}{\phi_{\text{PAC},n}} = \frac{1}{\beta_{\text{PAC}} \cdot 1 + G(s)}
\]

The amplitude of PAC output voltage is given by

\[
u_{\text{PAC}} = K_{\text{PAC}}(t_{\text{vco}} - t_{\text{ref}})
\]

where \( t_{\text{vco}} \) denotes the time of the first VCO rising edge in the time window of APD, and \( t_{\text{ref}} \) is the time of the REF rising edge in the time window. Equations relating edge time to signal phase are

\[
t_{\text{vco}} = \frac{\phi_{\text{vco}}}{\omega_{\text{vco}}} t_{\text{ref}} = \frac{\phi_{\text{ref}}}{\omega_{\text{ref}}}
\]

When the loop is in lock, \( \omega_{\text{vco}} = N \omega_{\text{ref}} \). As such, (8) can be rewritten as

\[
u_{\text{PAC}} = K_{\text{PAC}}(t_{\text{vco}} - t_{\text{ref}}) = \frac{i_{\text{cp}}}{K_{\text{CP}}} = K_{\text{APD}} K_{\text{PAC}}(\phi_{\text{vco}} - N \phi_{\text{ref}})
\]
Therefore, the feedback gain of PAC can be calculated as

\[ \beta_{\text{PAC}} = \frac{\Delta v_{\text{PAC}}}{\Delta \phi_{\text{vco}}} = \frac{1}{\omega_{\text{vco}}} K_{\text{PAC}} = \frac{V_{\text{max}}}{\pi}. \]  

(11)

The noise contribution of the CP can be calculated by relating the current noise at the CP output. The closed-loop transfer function of CP noise is shown as

\[ H_{\text{CP,n}}(s) = \frac{\phi_{\text{int,n,CP}}}{i_{\text{p,n}}} = \frac{1}{\beta_{\text{CP,APD}}} \frac{G(s)}{1 + G(s)}. \]  

(12)

The amplitude of CP output current is given by

\[ i_{\text{cp}} = K_{\text{PAC}} K_{\text{CP}} (t_{\text{cc}} - t_{\text{ref}}) = K_{\text{APD}} K_{\text{PAC}} K_{\text{CP}} (\phi_{\text{vco}} - N \phi_{\text{ref}}). \]  

(13)

Therefore, the CP feedback gain can be calculated as

\[ \beta_{\text{CP,APD}} = \frac{\Delta i_{\text{cp}}}{\Delta \phi_{\text{vco}}} = \frac{1}{\omega_{\text{vco}}} K_{\text{PAC}} \cdot g_m = \frac{V_{\text{max}}}{\pi} \cdot g_m. \]  

(14)

From the (11) and (14), it is difficult to estimate if \( \beta_{\text{PAC}} \) and \( \beta_{\text{CP,APD}} \) are related to \( N \) now. Considering the real circuit implementation, there are two different situations as follows, leading to two opposite conclusions. When \( K_{\text{PAC}} \) is proportional to \( f_{\text{vco}} \) or \( V_{\text{max}} \) is a constant and not related to \( f_{\text{vco}} \), \( \beta_{\text{PAC}} \) and \( \beta_{\text{CP,APD}} \) in locked state will be independent of \( N \). Contrarily, \( \beta_{\text{PAC}} \) and \( \beta_{\text{CP,APD}} \) will depend on \( N \) if \( K_{\text{PAC}} \) is a constant and not related to \( f_{\text{vco}} \). We will further discuss this issue in the next section.

In addition, the inverter chain and the D2S circuits will consume power and introduce noise in the proposed PLL. The noise contributions of the D2S and inverter chain can be calculated by relating the phase noise at the output of D2S and inverter chain. Since there is no frequency division in D2S and inverter chain, the feedback gain from PLL output to D2S and inverter chain output phase is one, which is not related to \( N \).

Furthermore, as shown in Fig. 7, noise transfer function of the REF and REF buffer is still multiplied by \( N \) as the classical PLL. As explained later, the noise contributions from REF and REF buffer will dominate the in-band noise of PLL when CP noise contribution is small.

C. Operating Principle of the Proposed CP

The timing diagram of CP is shown in Fig. 8. In each reference period \( T_{\text{ref}} \), the pulse widths of CP charging current \( I_{\text{up}} \) and discharging current \( I_{\text{dn}} \) are set to a fixed value \( T_d \), but the current amplitudes vary with \( \Delta \phi_{\text{vco}} \). When REF_BUF leads VCO_BUF and \( \Delta \phi_{\text{vco}} \) is decreased in the locking process, \( I_{\text{up}} \) is reduced while \( I_{\text{dn}} \) is equal to the minimum current of CP \( (I_{\text{min}}) \). Contrarily, \( I_{\text{dn}} \) is increased with decreasing \( \Delta \phi_{\text{vco}} \), while \( I_{\text{up}} \) is equal to \( I_{\text{max}} \) when REF_BUF lags VCO_BUF. When phase locked, both of \( I_{\text{up}} \) and \( I_{\text{dn}} \) will come to \( I_{\text{min}} \). \( T_d/T_{\text{ref}} \) is designed as 0.26 in our work. Since the effective CP output current is reduced by \( T_d/T_{\text{ref}} \), \( \beta_{\text{CP,APD}} \) is finally decreased by \( T_d/T_{\text{ref}} \).

The characteristics of the proposed CP and the sub-sampling CP currents are shown in Fig. 9(a) and (b) respectively. \( I_{\text{max}} \) and \( I_{\text{min}} \) represent the maximum and minimum currents of each CP respectively. Firstly, \( I_{\text{up}} \) and \( I_{\text{dn}} \) in locked state are the minimum currents of the proposed CP, not the average value of the maximum and minimum currents of the sub-sampling CP. Secondly, in half of the VCO period, \( I_{\text{up}} \) or \( I_{\text{dn}} \) in the proposed CP is always equal to \( I_{\text{min}} \), while \( I_{\text{up}} \) or \( I_{\text{dn}} \) in the sub-sampling CP is always above \( I_{\text{min}} \) in the VCO period. Since the CP current is simply defined by how much \( g_m \) is needed in locked state, it is difficult to compare the \( I_{\text{min}} \) of the two CPs.

D. Loop Parameter Design and Optimization of PLL Noise

As shown in Fig. 4, third-order loop filter is used to suppress the reference spur, which consists of a passive RC filter where a resistor \( R_1 \) is in series with a capacitor \( C_1 \). In addition, capacitor \( C_2 \) is added to reduce the voltage ripple of the VCO control signal \( (V_{\text{ctrl}}) \). Moreover, another pole consisted of \( R_2 \) and \( C_3 \) is used to improve reference spur attenuation. The PLL open-loop bandwidth \( \omega_c \) can be expressed as

\[ \omega_c = \frac{\beta_{\text{CP,APD}} \cdot K_{\text{VCC}} \cdot R_1 \cdot C_1}{C_1 + C_2 + C_3}. \]  

(15)

In general, \( C_1 \gg C_2 \) and \( C_3 \), (15) can be simplified as

\[ \omega_c \simeq \beta_{\text{CP,APD}} \cdot K_{\text{VCC}} \cdot R_1. \]  

(16)

A constant loop bandwidth can be achieved if \( \beta_{\text{CP,APD}} \) and \( K_{\text{VCC}} \) are constant.

To achieve low integrated phase noise (jitter), the PLL bandwidth needs to be delicately designed. The optimal bandwidth \( (\omega_{c,\text{opt}}) \) for the minimum jitter usually occurs at the intersection of the VCO phase noise and the other loop noise [18], [19].
In the proposed PLL design, different $\omega_{c,\text{opt}}$ is selected considering the proportion of CP noise and other loop noise contributions. As shown in Fig. 10, the solid line indicates the PLL output phase noise. When CP noise is dominant, $\omega_{c,\text{opt}}$ is shifted to a higher level with a higher $\beta_{\text{CP,APD}}$, as shown in Fig. 10(a) [4]. In this case, we can choose a higher $\beta_{\text{CP,APD}}$ to achieve a lower PLL jitter. Oppositely, when other loop noise becomes dominant, as shown in Fig. 10(b), $\omega_{c,\text{opt}}$ is the intersection of the VCO phase noise and the other loop noise [4], which is not related to $\beta_{\text{CP,APD}}$. Therefore, to achieve the minimum PLL phase noise, the constant loop bandwidth has to be guaranteed when $\omega_{c,\text{opt}}$ is changed. However, higher $\beta_{\text{CP,APD}}$ will require smaller $R_1$ and larger $C_1$ in LF to ensure the loop stability condition and constant bandwidth [4]. Note that larger capacitor will make the full integration difficult. However, when we set $R_1$ and $K_{\text{VCO}}$, a higher $\beta_{\text{CP,APD}}$ in Fig. 10(b) leads to a wider bandwidth and a worse phase noise. Based on this analysis, there is no need to increase $\beta_{\text{CP,APD}}$ further when the in-band phase noise is dominated by the other loop noise. In this way, the analysis and the conclusion of the PAC feedback gain $\beta_{\text{PAC}}$ is similar to $\beta_{\text{CP,APD}}$.

As a result, in order to avoid such unnecessarily high $\beta_{\text{CP,APD}}$ and optimize the PLL phase noise, a tunable $\beta_{\text{CP,APD}}$ is introduced in this paper. The tunable method will be discussed in the following section with details. The designed loop parameters of LF are shown in Table I.

### TABLE I

**DESIGNED PARAMETERS OF THE LOOP FILTER**

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<td>$R_1, R_2$</td>
<td>3.2 kΩ</td>
<td>$R_2, R_3$</td>
<td>1.9 kΩ</td>
</tr>
<tr>
<td>$C_1$</td>
<td>80 pF</td>
<td>$C_2$</td>
<td>3.2 pF</td>
</tr>
<tr>
<td>$C_3$</td>
<td>3.2 pF</td>
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In this section, we introduce the circuit design and implementation in details. The design considerations of APD, PAC and CP circuits are firstly presented. Then the behavior of the new phase detector in the main loop is illustrated. Finally, the gain control method of APD/PAC/CP is shown and the designs of VCO and other circuits are discussed as well.

#### A. Aperture Phase Detector

APD directly compares the phases between REF_BUF and VCO_BUF in a time window, which eliminates the need for frequency dividers. The schematic of APD is shown in Fig. 11(a) and the timing diagram in locked state is shown in Fig. 11(b). When the timing control signal PUL_window becomes low, APD captures the first rising edge of VCO_BUF and REF_BUF signals. Both the two signals will be reset to ‘0’ when PUL_window goes high, just as if the two signals are truncated in the time window. A classical PFD compares the phases of the truncated signals and then produces up and dn signals. The PUL_window has the same frequency as REF, and the width of time window Wd must be a little wider than the VCO period to avoid edge missing in phase comparison. The middle time point of Wd is the rising edge of REF_BUF, then APD can sense the positive and negative phase errors symmetrically. The timing error at this point is negligible as long as APD can sense both positive and negative phase errors. The generation of the time window will be discussed later.

Note that the truncated signal is different from the real output up/dn of APD. The pulse width of truncated signal in locked state is half of $T_{\text{vco}}$, but the pulse width of up/dn in locked state is determined by the reset time of the classical PFD ($t_{\text{reset}}$). The $t_{\text{reset}}$ is related to the loop gain and a value of 100 ps is designed in this work.

#### B. Phase to Analog Converter

The diagram of PAC is shown in Fig. 12. PAC converts up/dn into analog voltage signal VP/VN. The up/dn signal controls the on-time of the current flowing in $I_{\text{VAC}}$, which finally generates an analog voltage proportional to the pulse width of up/dn. After the conversion, PAC will further hold the output voltage until the reset control signal is active. The output voltage and the gain of PAC can be rewritten as

$$V = \frac{Q_{\text{PAC}}}{C_p} = \frac{I_{\text{PAC}} \Delta t}{C_p}$$

$$K_{\text{PAC}} = \frac{\Delta V}{\Delta t} = \frac{I_{\text{PAC}}}{C_p}$$

where $Q_{\text{PAC}}$ is the charge stored at the output node and $I_{\text{PAC}}$ is the current amplitude flowing in $C_p$. Here $\Delta t$ is the pulse width of up/dn from APD and it is equal to $t_{\text{reset}}$ in locked state. VP/VN in locked state can be calculated as

$$VP = VN = V_{\text{lock}} = \frac{I_{\text{PAC}} t_{\text{reset}}}{C_p}$$

Note that no matter how large the phase error is, the largest pulse width of APD output is $T_{\text{vco}}/2$. Accordingly, the highest output voltage can be designed lower than $V_{\text{DD}}$. In addition, the loop property is mainly determined by the voltage in the locked state,
Fig. 11. (a) Schematic of APD, (b) Timing diagram in locked state.

Fig. 12. Schematic of PAC.

which is always lower than $V_{DD}$. Therefore, the circuit can work well as long as $VP/VN$ is designed below $V_{DD}$ with the largest pulse width. There is a trade-off between the power and noise in PAC. Larger $I_{PAC}$ and smaller $C_p$ will lead to higher $\beta_{PAC}$ and $\beta_{CP,APD}$, which suppresses more PAC and CP noise. However, the power will be increased. In addition, smaller capacitor will be more sensitive to process variation. $I_{PAC}/C_p$ is related to the loop gain of the PLL, which is determined by the requirement of the loop parameter design. Here $V_{tune}$ is used to control the amplitude of the charging current $I_{PAC}$ as well as the amplitude of the output analog voltage, and finally control the current amplitude of the following CP. Though PAC suffers from the PVT variations, this controllable $I_{PAC}$ can guarantee the circuit work well in a wide variation range. $I_{PAC}$ can be estimated as

$$I_{PAC} = \frac{1}{2} \mu_p C_{ox} \left( \frac{W}{L} \right) \left( V_{tune} - V_{DD} - V_{thp} \right)^2$$

where $\mu_p$ is the mobility of charge carriers, $C_{ox}$ is the gate oxide capacitance per unit area, $(W/L)_{M1}$ and $V_{thp}$ are the size and the threshold voltage of M1, respectively. In addition, after the phase detection in a reference period, a control signal Rst_PAC is used to reset the output analog voltage and prepare for the next conversion.

From (18), we can see that $K_{PAC}$ is a constant which is not proportional to $f_{vco}$ in our PAC circuit design and different from sub-sampling PLL where the sampled maximum voltage ($A_{VCO}$) is independent on $f_{vco}$, $V_{n,s}$ of our PAC is actually a variable dependent on $f_{vco}$. This will make $\beta_{PAC}$ depend on $N(f_{vco}/f_{ref})$, which can be understood in the time domain as follows. When a timing error $\Delta t$ between the VCO and REF is detected, the PAC will output a voltage with amplitude $K_{PAC} \cdot \Delta t$. If $N$ is increased while keeping the same VCO phase error ($\Delta \phi_{vco}$) which is equal to $f_{vco} \cdot \Delta t$, $\Delta t$ will be decreased. Due to the constant $K_{PAC}$, the PAC output voltage becomes smaller with larger $N$, leading to a lower $\beta_{PAC}$.

Combining (2) and (18), the feedback gain of PAC in locked state (ignoring the finite reset time of the PAC) with the practical circuit parameters can be rewritten as

$$\beta_{PAC} = K_{APD} \cdot K_{PAC} = \frac{V_{t,ax}}{2\pi} = \frac{I_{PAC} T_{vco}}{C_p} = \frac{T_{ref}}{N}$$

Therefore we see that $\beta_{PAC}$ depends on $N$.

C. Charge Pump

Fig. 13 shows the diagram of CP in the main loop. It has two main advantages. Firstly, CP outputs current amplitude in proportion to $\Delta \phi_{vco}$ and achieves low phase noise. Secondly, CP outputs equal pulse widths and equal amplitudes $I_{up}$ and $I_{dn}$ to achieve low reference spur.

The amplitude of $I_{up}(I_{dn})$ is proportional to the analog voltage signal VP(VN) from PAC, which finally achieves CP current amplitude proportional to $\Delta \phi_{vco}$. A differential pair in CP converts the analog voltage into current and current mirror (M5, M6) is used to inject the charging current into the loop filter. In order to avoid the mismatch of switches in conventional CP, the pulse width of $I_{up}(I_{dn})$ is controlled by a pair of anti-phase signals PUL_CP and PULB_CP which have the same capacitive load. When the timing control signal PUL_CP is high, $I_{up}$ and $I_{dn}$ will be connected to the loop filter. Inversely, when PUL_CP goes low, the current sources are steered away to $C_s$ instead of switched off to alleviate the charge sharing between the loop filter and the current sources [4]. Ideally, a constant $\beta_{CP,APD}$ is produced. In fact, since the amplitude of $I_{up}(I_{dn})$ is the square of the input analog voltage...
due to the nonlinearity of the transistors, $\beta_{CP,APD}$ is not a constant. The gain of CP can be rewritten as

$$K_{CP} = \frac{\Delta I_{CP}}{\Delta V} = g_m - \mu_n \cdot C_{ox} \left( \frac{W}{L} \right) (V_{GS} - V_{th})$$  \hspace{1cm} (22)$$

where $\mu_n$ is the mobility of charge carriers, $V_{GS}$ and $V_{th}$ are the gate-source voltage and the threshold voltage of the MOS transistors (M7, M8 in Fig. 13), respectively. $V_{GS}$ is determined by VP/VN from PAC. We can see that $K_{CP}$ varies with VP/VN.

In locked state, $g_m$ is a constant which is not related to REF/VCO frequency, then $\beta_{CP,APD}$ is mainly determined by $V_{max}$ of PAC. Similar to the analysis of the PAC feedback gain, $\beta_{CP,APD}$ is dependent on $N$ due to the variable $V_{max}$ related to $I_{vcn}$.

Combining (2), (18) and (22), and considering the effective CP output current reduction by $I_{up}$, the feedback gain of CP in locked state can be expressed as

$$I_{up} = I_{dn} = I_{lock}$$

$$= \frac{1}{2} \mu_n \cdot C_{ox} \left( \frac{W}{L} \right) (I_{PAC}T_{ref} - V_{th})^2 \hspace{1cm} (23)$$

In locked state, $g_m$ is a constant which is not related to REF/VCO frequency, then $\beta_{CP,APD}$ is mainly determined by $V_{max}$ of PAC. Similar to the analysis of the PAC feedback gain, $\beta_{CP,APD}$ is dependent on $N$ due to the variable $V_{max}$ related to $I_{vcn}$.

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In locked state, $g_m$ is a constant which is not related to REF/VCO frequency, then $\beta_{CP,APD}$ is mainly determined by $V_{max}$ of PAC. Similar to the analysis of the PAC feedback gain, $\beta_{CP,APD}$ is dependent on $N$ due to the variable $V_{max}$ related to $I_{vcn}$. Therefore, $\beta_{CP,APD}$ depends on $N$ and has the smallest value in locked state due to the minimum current amplitude. However, as explained in Section II, there is no need to design an unnecessarily high feedback gain which will consume large area due to large capacitor in LF for the stable condition [4]. Although $\beta_{CP,APD}$ depends on $N$, the proposed PLL can still reduce the CP noise contribution compared with the classical PLL, which will be discussed later.

The low spur property of the proposed CP can be explained as follows. Firstly, the pulse widths of $I_{up}$ and $I_{dn}$ are set to a fixed value $T_d$, assuming ideal switching, the following equation must be satisfied to meet the steady-state locking condition of zero net CP output charge [5]

$$I_{up} \cdot T_d - I_{dn} \cdot T_d \Rightarrow I_{up} = I_{dn}. \hspace{1cm} (25)$$

Namely, $I_{up}$ and $I_{dn}$ must have equal amplitude in locked state. Therefore the proposed CP eliminates the mismatch problem in the classical PLL and produces a much smaller ripple, as shown in Fig. 14. The ideal locking point is achieved when VP is equal to VN. However, there is still mismatch between the switches due to the non-ideal current source switches. Once there is some mismatch in CP, the loop will shift the locking point from the ideal point and tune VP (VN) to make the $I_{up}$ and $I_{dn}$ equal to each other to satisfy the steady condition. Therefore, the mismatch between the current source transistors still causes static phase error as in a conventional CP, but here it does not generate CP output current ripple and introduce spur [5].

D. Clock Generation and Timing Diagram of APD/PAC/CP

The CLK generation circuit is critical for the proposed main loop, as shown in Fig. 15. Two identical delay cells are used for the time window generation, which makes the middle time point of $W_d$ occur at the rising edge of REF_BUF. The schematic of the delay cell is shown in Fig. 16. To cover the PVT variations, the width of $W_d$ is designed to be tunable by $VC$. To reduce the power consumption of the two delay cells, an additional transistor $M2$ is inserted between $M1$ and $M3$, as shown in Fig. 16. The gate of $M2$ is controlled by input signal IN. The branch labeled as $B_c$ will be switched on when IN is active, while it is switched off when IN is inactive. The branch $H_c$ does not need to be turned on all the time in contrast to the delay cell in [4]. With this method, a current of 100 $\mu$A can be saved. Moreover, the input reference signal REF is processed in the CLK block to generate the final timing control signals of the main loop. Note that PUL_CP and PULB_CP must be active after the PAC charges to a steady analog voltage. As shown in Fig. 15(b), Rst_PAC must come later than PUL_CP and PULB_CP and ensure CP to capture the correct analog voltage. Moreover, an additional latch is used to make the PUL_CP and PULB_CP have perfect symmetry, which can reduce the mismatch of switches.
in CP and then reduce the reference spur. Considering the reset time of PAC, $\beta_{\text{PAC}}$ will be divided by 0.5 finally. REF_BUF is fed to the PFD in FLA and APD as the real reference signal. The detailed connection relationship between CLK timing control signals and APD/PAC/CP is shown in Fig. 17.

The principle of the new phase detection mechanism is shown in Fig. 18. When the VCO_BUF and REF_BUF are phase aligned, the pulse width of up/dn is equal to the reset time of the classic PFD in APD ($t_{\text{reset}}$).

In order to avoid the phase detection dead zone similar to the classical PLL, $I_{\text{PAC}}$, $t_{\text{reset}}$ and $C_p$ are carefully selected to guarantee that $V_{\text{lock}}$ is larger than $V_{\text{thm}}$. When REF_BUF lags VCO_BUF, the pulse width of dn will be larger than $t_{\text{reset}}$ while the pulse width of up remains the same. VN will be higher than $V_{\text{lock}}$ while VP is equal to $V_{\text{lock}}$. This increases the discharging current in CP, then $V_{\text{ctrl}}$ will be decreased and the frequency of VCO will be decreased to make it aligned with REF frequency. In a similar way, when REF_BUF leads VCO_BUF, the charging current will be increased to make the VCO catch up with REF.

Furthermore, the sub-sampling CP current is always on in the whole REF period [4]. As shown in Figs. 13 and 18, the proposed CP current is, however, only active when VN/VP is larger than $V_{\text{thm}}$, which is less than half of the REF period. As such, when compared to the previous sub-sampling CP, the proposed CP can reduce the power consumption.

E. CP Noise Comparison

To demonstrate the CP noise reduction we can achieve using the proposed PLL instead of a classical PLL, we compare the CP noise contributions of the two PLLs. By simply increasing the CP bias current of both PLLs in locked state, the CP noise contribution can be reduced. For a fair comparison, we assume that the two CPs use equal CP current amplitude ($I_{\text{CP,CON}}$) in locked state. The CP feedback gain of the proposed PLL is given by

$$\beta_{\text{CP,APD}} = K_{\text{APD}} \cdot K_{\text{PAC}} \cdot K_{\text{CP}} \cdot \frac{T_d}{T_{\text{reset}}}$$

$= \frac{1}{2} \cdot \frac{1}{2\pi N} \cdot \frac{I_{\text{PAC}}}{C_p} \cdot \frac{\mu_p}{C_{\text{ox}}} \cdot \left( \frac{W}{L} \right)_{\text{B}} \cdot \left( \frac{I_{\text{PAC,ctrl}}}{C_p} - V_{\text{thm}} \right) \cdot T_d \cdot (26)$

The additional factor of 1/2 in (26) compared with (24) is due to the reset time of PAC (neglecting the charging time of PAC). Since the CP current in locked state can be expressed as (23), then (26) can be rewritten as

$$\beta_{\text{CP,APD}} = \frac{I_{\text{CP,CON}}}{2\pi N} \cdot \frac{T_d}{t_{\text{reset}} - \frac{C_p}{I_{\text{APD}}}} \cdot V_{\text{thm}} > \frac{I_{\text{CP,CON}}}{2\pi N} \cdot \frac{T_d}{t_{\text{reset}}} \cdot (27)$$
Note that $I_{PAC}$, $t_{\text{rest}}$, and $C_p$ are carefully selected to guarantee that $t_{\text{rest}}$ is larger than $C_p V_{1LH} / I_{PAC}$. Combining (1) and (27), we can obtain

$$\frac{\beta_{\text{CP,APD}}}{\beta_{\text{CP,CON}}} > \frac{T_d}{t_{\text{rest}}} \tag{28}$$

$T_d / t_{\text{rest}}$ is designed as 40 in our PLL, which indicates the CP feedback gain of the proposed PLL can be 40 times larger than a classical PLL with the same CP current amplitude in locked state. In other words, if we realize the same CP feedback gain, the current amplitude of the proposed CP will be 40 times lower than the classical CP. Thus much lower power will be consumed by the proposed CP.

Moreover, since we assume the two CPs use equal CP current amplitude in locked state, the power spectral density (PSD) of the (thermal) noise generated by the two CPs can be compared as

$$\frac{S_{\text{ICP,APD}}}{S_{\text{ICP,CON}}} = \frac{T_d}{t_{\text{rest}}} \tag{29}$$

where $t_{\text{PFD}}$ is the reset time of the PFD in the classical PLL. Combining (28) and (29), the in-band phase noise due to the CP of the two PLLs can be compared as

$$\frac{E_{\text{in-band,CP,APD}}}{E_{\text{in-band,CP,CON}}} = \frac{\beta_{\text{CP,APD}}^2}{\beta_{\text{CP,CON}}^2} \frac{T_d}{t_{\text{PFD}}} \frac{t_{\text{rest}}}{t_{\text{PFD}}} \tag{30}$$

Since the reset time of the proposed APD is determined by the rest time of a classical PFD, we can assume that $t_{\text{rest}}$ is equal to $t_{\text{PFD}}$. Thus, with the same CP current amplitude in locked state, the proposed CP noise contributed to the PLL output will be 40 times lower than a classical CP, which makes the proposed CP contribute a very low in-band phase noise to the PLL output.

### F. APD/PAC/CP With Gain Control

Based on the issues discussed in Section II, a tunable $\beta_{\text{CP,APD}}$ is proposed to reduce the PLL output jitter. According to (18) and (22), the gain of PAC and CP can be changed by $I_{PAC}$. As shown in (20), $I_{PAC}$ can be changed by $V_{\text{tune}}$, and thus $\beta_{\text{PAC}}$ and $\beta_{\text{CP,APD}}$ can be easily tuned by $V_{\text{tune}}$. Since $\beta_{\text{PAC}}$ and $\beta_{\text{CP,APD}}$ are changed, the other loop parameters will be changed simultaneously. Furthermore, we calculate $\beta_{\text{CP,APD}}$, bandwidth $f_c$, $PM$ and $I_{CP}(I_{\text{tran}})$ in locked state at different values of control voltage $V_{\text{tune}}$. The experiment results are shown in Table II.

<table>
<thead>
<tr>
<th>$V_{\text{tune}}$ (V)</th>
<th>$f_{\text{tune}}$ (kHz)</th>
<th>$f_c$ (MHz)</th>
<th>$PM$ (deg)</th>
<th>$I_{\text{CP}}$ (mA)</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.5</td>
<td>3.6</td>
<td>0.8</td>
<td>46</td>
<td>15</td>
</tr>
<tr>
<td>0.5</td>
<td>6.5</td>
<td>1.4</td>
<td>55</td>
<td>28</td>
</tr>
<tr>
<td>0.45</td>
<td>9.8</td>
<td>2.1</td>
<td>33</td>
<td>45</td>
</tr>
</tbody>
</table>

When we decrease $V_{\text{tune}}$, the analog voltage of PAC and the current amplitude of CP will be both increased. Then $\beta_{\text{CP,APD}}$ and bandwidth of PLL will be increased at the same time. However, since we fix the loop parameter in LF, the $PM$ of the PLL will be changed with the $\beta_{\text{CP,APD}}$ and $f_c$ at the same time. The relationship between settling time and $PM$ is described in [20]. There is an optimal value of $PM$ for the fast settling of PLL, and a high $PM$ does not mean that it is always good for a PLL system. The loop can work well as long as appropriate PM is guaranteed.
Fig. 19. Schematic of VCO.

As shown in Table II, \( I_{\text{up}} / I_{\text{dn}} \) in locked state is much smaller than the CP in the classical PLL. Considering the ratio of on-state time of CP current to reference period, the power of CP can be reduced further. For example, when \( V_{\text{tune}} \) is equal to 0.5 V, the power consumption of CP is less than 28 \( \mu \)A as well as a high \( \beta_{\text{CP, APD}} \) is achieved simultaneously. In conclusion, the proposed CP can reduce the in-band phase noise as well as reference spur with an ultra-low power dissipation, which is further verified by our measurement results.

G. VCO and Other Circuits

As shown in Fig. 19, in order to trade off between the power consumption and phase noise, complementary cross-coupled structure is adopted to form the negative transconductance in the VCO design. Three digitally controlled capacitor arrays (DCCA) are used to achieve a frequency range more than 400 MHz to cover the process variations. To reduce the loop gain variations resulting from changes in the \( K_{\text{VCO}} \), the VCO using an averaging varactor based split-tuned LC-tank [21] is employed in the proposed PLL. The gain of VCO can be described as

\[
K_{\text{VCO}} = \frac{\partial \omega_{\text{osc}}}{\partial V_{\text{ctrl}}} = \frac{1}{\sqrt{L(C_{\text{fixed}} + C_{\text{var}})}} \frac{\partial}{\partial V_{\text{ctrl}}} \left[ \frac{L}{\omega_{\text{osc}}^2} \frac{\partial C_{\text{var}}}{\partial V_{\text{ctrl}}} \right] \tag{31}
\]

where \( L \) and \( C_{\text{fixed}} \) are the inductance and the fixed capacitance of the LC tank, respectively, \( \omega_{\text{osc}} \) is the oscillation frequency and \( \partial C_{\text{var}} / \partial V_{\text{ctrl}} \) is the voltage sensitivity of the varactor which is related to the varactor’s linearity. Different from the fixed DC bias voltage used in the traditional varactor design, the averaging varactor uses distributed voltage values (0 V, 0.6 V, 1.2 V) for three varactors. Therefore, the nonlinearities of the varactors are nearly cancelled. \( K_{\text{VCO}} \) is designed to be 70 MHz/V in our VCO.

To reduce area and design complexity, five stages of TSPC dividers are employed to achieve a 32-division-ratio in the proposed PLL. Since the CP2 in the FLA loop will be closed automatically after phase locking, CP2 will not introduce reference spur. Moreover, rail-to-rail amplifiers in the classical PLL are avoided. Therefore a simple charge pump circuit with feedback [22] is applied in the FLA.

IV. EXPERIMENT RESULTS AND DISCUSSIONS

To validate the proposed design concept, a chip-prototype was implemented in TSMC 0.13-\( \mu \)m 1.2-V CMOS process, as shown in Fig. 20. This chip occupies a core area of 0.48 mm \( \times \) 0.86 mm excluding PADs and the proposed components of APD/PAC/CP consume very small area. The frequency of reference signal is 66 MHz and the measured PLL output frequency is 2112 MHz. Fig. 21 shows the PLL output phase noise from Agilent Spectrum Analyzer E4440A when we set \( V_{\text{tune}} \) to 0.55 V. The measured in-band phase noise is \(-103\) dBc/Hz at 100 kHz offset and out-of-band phase noise is \(-137\) dBc/Hz at 10 MHz offset. The in-band phase noise is greatly limited by the reference signal quality. It is already verified by testing the phase noise of the 66 MHz reference signal generated from Agilent E4438C, as shown in Fig. 22. Considering the frequency multiplication, \( 2\pi \log N \) is added to predict the ideal phase noise of PLL output. If we only consider the reference signal noise contribution to the PLL output, the ideal phase noise is only \(-108\) dBc/Hz at 100 kHz offset. The phase noise of our reference signal is 25 dB higher than the reference signal derived from the low noise crystal oscillator in [4]. It indicates that the reference signal noise contributes significantly to the in-band phase noise of the proposed PLL.

When we decrease the gain control signal \( V_{\text{tune}} \) to 0.5 V, \( \beta_{\text{CP, APD}} \) is increased and the PLL bandwidth is extended at the same time, as shown in Fig. 23. However, the in-band phase noise remains the same as in Fig. 21. Note that the phase noise of our PLL is dominated by the other loop noise, and CP is not
the main in-band noise source any more. This explains why the in-band phase noise cannot be improved when we increase the $\beta_{\text{CP,APD}}$. In this case, the small $\beta_{\text{CP,APD}}$ and the narrow bandwidth according to the analysis in Section II are beneficial to reduce the phase noise at 1 MHz offset and the jitter of PLL output. The measured phase noise results thereby validate our previous theoretical analysis in Sections II and III.

When the PLL is locked, the power supplies of the dividers and CP2 in FLA are turned off and the reference spur is also measured with Agilent Spectrum Analyzer E4440A to be $-70 \text{ dBc}$ at 66 MHz offset as shown in Fig. 24. The VCO dissipates 1.9 mA, and the rest circuits 0.6 mA. The FLA consumes a current of 1.7 mA and is powered down after phase locking. For our PLL, the power consumption blocks are only VCO, buffers and some control circuits. The power contributions from CP and dividers are nearly eliminated. Thus the proposed PLL can achieve an ultra-low power consumption of 3 mW.

Furthermore, to clearly illustrate the locking process of the proposed PLL, the measured locking curve of the proposed PLL is shown in Fig. 25. The locking process is totally different from the classical PLL. In phase 1, the VCO frequency is higher than the REF signal, and the two loops operate at the same time to align the REF and the VCO frequency. In phase 2, the discharging current in CP2 is switched on and $V_{\text{ctrl}}$ is decreased at the same moment. This reduces the phase error between REF and VCO gradually. At the end of phase 2, the phase error finally falls into the DZ of FLA and the CP2 in FLA is closed automatically. Afterwards, the main loop dominates the final locking process, as shown in phase 3. As mentioned previously, the FLA operates as coarse tuning and main loop operates as fine tuning in the dynamic locking process. With the use of the dual-loop architecture, the correct frequency locking can be achieved as demonstrated.

Table III summarizes the proposed PLL performance with a comparison of a few published integer-PLLs. To fairly compare the in-band phase noise with other work, a normalized in-band phase noise is calculated as [24]

$$\xi_{\text{norm}} = \xi_{\text{in-band}} - 20 \log N - 10 \log f_{\text{ref}}.$$  \hspace{1cm} (32)

This work achieves the lowest power dissipation and reference spur as well as a moderate in-band phase noise.
A 2.1-GHz PLL with low power low reference spur and low in-band phase noise has been presented. By the new phase detection mechanism based on APD/PAC/CP, the amplitudes of CP charging and discharging currents have equal small amplitude with equal pulse width after phase locking. Thus leads to a much lower reference spur. Furthermore, compared with the classical PLL, the proposed PLL can increase the CP feedback gain dramatically with the same CP bias current as classical PLL, the proposed PLL can increase the CP feedback gain much low reference spur. Furthermore, compared with the classical PLL, the proposed PLL can increase the CP feedback gain dramatically with the same CP bias current as classical PLL in locked state. Thus the proposed CP contributes a very low noise to the PLL output. Due to the APD, the dividers in the proposed PLL can be turned off in locked state, eliminating the power and noise contributions from the dividers. In addition, a tunable loop gain (with theoretical analysis) is introduced to reduce the PLL integrated phase noise. As such, one can achieve low power consumption, low reference spur. As demonstrated by a chip-prototype in TSMC 0.13 CMOS process, the proposed PLL has a power consumption of 3 mW, a reference spur of $-80 \text{ dBc} / -74 \text{ dBc}$ at 66 MHz offset and an in-band phase noise of $-103 \text{ dBc/Hz}$ at 100 kHz offset.

V. CONCLUSION

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REFERENCES


Deyun Cai received the B.S. degree in microelectronic engineering from Xi’an Jiaotong University, China, in 2009. She is working toward the M.S. degree in microelectronic engineering at Fudan University, Shanghai, China.

Her current research interest is mainly in millimeter-wave integrated circuit design, with a focus on 60 GHz voltage-controlled oscillator circuit design based on meta-material, active and passive device modeling and testing.

Haipeng Fu received the B.S. degree in communication engineering from Harbin Institute of Technology, China, in 2007. Since 2007, he has been with the Department of Electronic Engineering, Fudan University, Shanghai, China, where he is currently working toward the Ph.D. degree.

His research focuses on RF and millimeter-wave integrated circuit design.

Junyan Ren received the B.S. degree in physics in 1983 and the M.S. degree in electronic engineering in 1986 from Fudan University, China.

Since 1986, he has been with the State-Key Lab of ASIC and System Lab and Micro/Nano-Electronics Innovation Platform, Fudan University. Currently he is a Full Professor in Microelectronics, and vice director of State-Key Lab of ASIC and system. He is the author and/or co-author of over 100 technical papers of conferences and journals. Also, he has filed over 20 China patents. His researches interest includes RF/analog/mixed-signal integrated circuit with communication applications.

Wei Li received the B.Sc. and M.Sc. degrees from Harbin Engineering University China, in 1986 and 1989, respectively, and the Ph.D. degree from Ghent University, Belgium, in 2001, in electrical engineering.

From 1989 to 1996, she was a Lecturer at Harbin Engineering University where she worked on research and development of RF and Microwave Circuit/System Designs and so on. From 1997 through 2001, she joined the INTEC-design lab at Ghent University of Belgium as a Research Engineer, responsible for RF and Microwave Circuit and System Designs in Instrumentation and Measurement, and Passive Optical Access Network, etc. In 2002, she joined in Research and Innovation Center at Alcatel Shanghai-Bell Co., Ltd., Shanghai, China, serving as a Project Coordinator/Researcher for the standardization development of HSDPA. Since February 2004, she has been an Associate Professor with Microelectronics School, Fudan University. She has authored/co-authored more than 40 research papers in the field of telecommunication in International/National Journals and Conferences, and has filed 3 Europe patents and over 10 China patents. Her current research interests include CMOS radio frequency and analog/mixed-signal integrated circuits for ultra-wideband applications and the reconfigurable radio frequency system.

Ning Li received the B.S. degree in electronic engineering from Fudan University, China, in 1984. Since then, he worked respectively at the Lab of Device of Semiconductor and the State Key Lab of ASIC & Systems at Fudan University. He is currently an Associate Professor in the Department of Microelectronics, Fudan University. His research interests are in the area of analog integrated circuits and CMOS RF integrated circuits.

Hao Yu received the B.S. degree from Fudan University, Shanghai, China, in 1999, and the M.S. and Ph.D. degrees from the Electrical Engineering Department, University of California, Los Angeles, in 2007, in the field of the integrated circuit and embedded computing.

He was a Senior Research Staff Member at Berkeley Design Automation (BDA) until 2009, one of top-100 start-ups selected by Red-herrings at Silicon Valley. Since 2009, he has been an Assistant Professor with Nanyang Technological University, Singapore. He has 42 refereed international publications and 5 book/chapters. His primary research interests include: 3-D cyber-physical computing system; and analog/RF design exploration at extreme scale.

Dr. Yu has received a best paper award in ACM *Transactions on Design Automation of Electronic Systems* (TODAES), two best paper award nominations in Design Automation Conference (DAC) and International Conference of Computer-Aided-Design (ICCAD), and one inventor award from Semiconductor Research Cooperation (SRC). He is on the Editorial Board of several journals and serves as the technical program committee member and session chair of several conferences.

Kiat Seng Yeo (SM’09) received the B.Eng. (hons.) in 1993, and the Ph.D. degree in 1996 both from Nanyang Technological University, both in electrical engineering.

He joined the School of Electrical and Electronic Engineering, Nanyang Technological University in 1996. Head of the Division of Circuits & Systems and a Board Member of the Singapore Semiconductor Industry Association (SSIA), he is a widely known authority on low-power IC design and a recognized expert in CMOS technology and radio frequency IC design. As a result of his innovative pioneering work in the field of IC design, he has successfully attracted over S$30 million of external research funding from various funding agencies and the industry in the last 5 years. He is currently a Professor in the School of Electrical and Electronic Engineering and Founding Director of VIRTUS, a new research centre of excellence jointly set up by Nanyang Technological University and Singapore Economic Development Board. He has authored over 300 refereed papers in top-tier journals and conferences in his area of research. He is the author of 6 books, 3 book chapters and holds 25 patents, including two patents for the world’s smallest integrated transformer and several patents for 60-GHz applications. He provides consultation to multinational corporations and was General Chair, Co-General Chair and Technical Chair of several international conferences. He gave keynotes and invited presentations at various scientific meetings, workshops and seminars.

Dr. Yeo serves on the Editorial Board of *IEEE TRANSACTIONS ON MICROWAVE THEORY AND TECHNIQUES*. He was awarded the Public Administration Medal (Bronze) on National Day 2009 by the President of the Republic of Singapore. He was also awarded the distinguished Nanyang Alumni Award in 2009 for his outstanding contributions to the university and Singapore’s society.