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<td>Author(s)</td>
<td>Voight, Barry; Widiwijayanti, Christina; Mattioli, Glen; Elsworth, Derek; Hidayat, Dannie; Strutt, M.</td>
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Magma-sponge hypothesis and stratovolcanoes: Case for a compressible reservoir and quasi-steady deep influx at Soufrière Hills Volcano, Montserrat

Barry Voight,¹ Christina Widiwijayanti,¹ Glen Mattioli,² Derek Elsworth,¹ Dannie Hidayat,¹ and M. Strutt³

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[1] We use well-documented time histories of episodic GPS surface deformation and efflux of compressible magma to resolve apparent magma budget anomalies at Soufrière Hills volcano (SHV) on Montserrat, WI. We focus on data from 2003 to 2007, for an inflation succeeded by an episode of eruption-plus-deflation. We examine Mogi-type and vertical prolate ellipsoidal chamber geometries to accommodate both mineralogical constraints indicating a relatively shallow pre-eruption storage, and geodetic constraints inferring a deeper mean-pressure source. An exsolved phase involving several gas species greatly increases andesite magma compressibility to depths >10 km (i.e., for water content >4 wt%, crystallinity ~40%), and this property supports the concept that much of the magma transferred into or out of the crustal reservoir could be accommodated by compression or decompression of stored reservoir magma (i.e., the “magma-sponge”). Our results suggest quasi-steady deep, mainly mafic magma influx of the order of 2 m³s⁻¹, and we conclude that magma released in eruptive episodes is approximately balanced by cumulative deep influx during the eruptive episode and the preceding inflation. Our magma-sponge model predicts that between 2003 and 2007 there was no evident depletion of magma reservoir volume at SHV, which comprises tens of km³ with radial dimensions of order ~1–2 km, in turn implying a long-lived eruption. Citation: Voight, B., C. Widiwijayanti, G. Mattioli, D. Elsworth, D. Hidayat, and M. Strutt (2010), Magma-sponge hypothesis and stratovolcanoes: Case for a compressible reservoir and quasi-steady deep influx at Soufrière Hills Volcano, Montserrat, Geophys. Res. Lett., 37, L00E05, doi:10.1029/2009GL041732.

2. Constraints at SHV

[3] The SHV has been investigated from 1995-present but the architecture of its magma storage zone remains enigmatic because some critical evidence is conflicting. The reservoir top has been reported at ~5 km (~115–130 MPa) based on phase equilibrium experiments and limited melt inclusion data on volatiles [Barclay et al., 1998], hornblende phenocryst chemistry [Rutherford and Devine, 2003], and the deepest locations of volcano-tectonic earthquakes occurring near the conduit [Aspinall et al., 1998]. Early GPS surface deformation data were interpreted to suggest a reservoir depth of ~6 km coupled to a deforming dike [Mattioli et al., 1998], but post-1997 geodetic data supported a deeper source >9 km, assuming a spherical reservoir geometry [Mattioli and Herd, 2003; G. S. Mattioli et al., GPS imaging of the SHV magma system from 1995 to 2008, submitted to Geophysical Research Letters, 2009]. The cumulative volume of the eruption, about 1 km³ DRE [Wadge et al., 2010], and its chemical and petrological consistency over 14 years suggests that the andesite magma source is voluminous, several to tens of km³. The response of borehole strainmeters to the major 2003 dome collapse further suggested a volatile-saturated magma body of several km³ with a top at 5–7 km depth [Voight et al., 2006]. The mixed andesitic lavas require a deep supply of mafic magma [Murphy et al., 2000]. Seismic imaging (B. Voight et al., The SEA-CALIPSO volcano imaging experiment on Montserrat: Aims, plans, campaigns at sea and on land, and lessons learned, submitted to Geophysical Research Letters, 2009) has sought magma storage regions >5 km (E. Shalev et al., Three-dimensional seismic velocity tomography of Mont-
tserrat from the SEA-CALIPSO offshore/onshore experiment, submitted to Geophysical Research Letters, 2009) but with poor resolution. A 2D seismic velocity section on a SE–NW line through SHV reveals a ∼10 km‐wide body with fast average velocity from the surface to >8 km depth [Paulatto et al., 2010]. These results may be explained by crystallized intrusions and host rock precipitation of silica and hydrothermal minerals, with currently‐active magma storage region(s) contained inside this body but masked at the seismic resolution.

Thus the strongest constraints on reservoir architecture may be from geodetic imaging. Here we examine the merits of an internally stratified, single crustal reservoir with top below 5 km bsl and centroid near 10 km, whose geometry is possibly vertically‐elongated, and whose base is supplied by a deep factory for intermediate to mafic hydrous melts at least partly fractionated near and above the crust‐mantle boundary [Voight et al., 2008]. The model presented here is an alternative to others that have been proposed. Notably, Mattioli et al. [1998] modeled 1995–97 surface deformation from GPS geodesy as a halfspace with two sources of deformation, a Mogi‐type source at ∼6 km, and a shallower NW‐trending dike. Subsequent solutions, conditioned by post‐1999 data which are both spatially and temporally denser, favored a deeper spherical source (G. S. Mattioli et al., Long term surface deformation of Soufrière Hills Volcano, Montserrat from GPS geodesy: Inferences from simple elastic inverse models, manuscript in preparation, 2009). This led Elsworth et al. [2008] to propose a model with two stacked magma reservoirs, at depths of 6 km and 12 km, connected from surface to deep crust and mantle by vertical conduits; GPS velocities were co‐inverted with surface efflux to calculate magma transfer rates through intermediate and deep crust. These results differ substantially from the model presented here, as discussed below.

3. Data and Modeling

[5] Surface deformation associated with the ongoing eruption of SHV was measured initially using campaign GPS beginning in 1995, with the earliest observations acquired 6 weeks prior to quasi‐continuous andesite extrusion in November [Mattioli et al., 1998]. Since 1996 a network of continuous GPS (cGPS) sites has operated, with the current network (post‐2003) comprised of 10 sites located at radial distances between 1.6 and 9.6 km from the center of activity [Mattioli et al., also submitted manuscript, 2009].

[6] It is convenient to consider episodes of ground inflation and deflation in pairs, with each inflation followed by a succeeding eruption and concurrent deflation. The initial inflation is inferred to have occurred between 1992–1995, but surface deformation observations at SHV only began in August 1995 [Mattioli et al., 1998]. The initial poorly observed epoch was followed in November by the first of three distinct episodes of surface subsidence recorded by GPS at SHV, which correspond to a deflating crustal source and active surface efflux, separated by surface uplifts that correlate with inflating sources and observed pauses in surface activity [Elsworth et al., 2008; Mattioli et al., submitted manuscript, 2009]. Caribbean‐fixed velocities reveal radial displacements toward the volcanic source during deflations, and away from the source during inflations (Figure 1). Here we focus on a representative pair of inflations and deflations, from 13 July 2003–01 Nov 2005, and 02 Nov 2005–31 Jan.
2007, respectively, which encompass the strengthened post-Feb 2003 cGPS network [Mattioli et al., 2004, also submitted manuscript, 2009]. Horizontal and vertical ground displacements (and error bars) with radial distance from the vent for the two cases are shown in Figure 2.

[7] First we consider the 2005–2007 deflation (Figure 2b), in order to directly compare ground deformation to erupted volume. Our cGPS data have been adjusted to correct for surface load effects related to emplacement of dome lava during this episode, 205 Mm$^3$ assuming a density of 2100 kg/m$^3$ [Poulos and Davis, 1994]. The plot compares the adjusted cGPS data to results from elastic analytical models. Elastic response is inferred from observed constant rates of surface deformation during inflation and deflation, and rapid changes in deformation sense that are synchronous with the efflux record (see auxiliary material).

A point source, embedded in an elastic half-space and using uncorrected data, excluding HERM which is significantly affected by dome loading, yields an inverted centroid depth as 10.3 km and a reservoir volume change $DV_r$ of $-44.2$ Mm$^3$ [Delaney and McTigue, 1994] (see auxiliary material). Manual fits to the same displacement data were of similar or superior fidelity [Mattioli et al., 1998, also submitted manuscript, 2009] (see auxiliary material) representing a spherical source at nominal depth 10.0 km and $DV_r = -30.0$ Mm$^3$.

[8] Data for the preceding inflation epoch, 13 July 2003–01 Nov 2005 (Figures 1a and 2b) are compared in Figure 2 (no load corrections required in this case since the dome was already removed) to results from analytical models. A point source [Mogi, 1958], embedded in an elastic half-space under the vent and excluding the proximal HERM site, yields an inverted centroid depth as 10.4 km and a reservoir volume change $DV_r$ of 16.8 Mm$^3$. Again, forward models yield a spherical source at nominal depth 10.0 km and $DV_r = 16.0$ Mm$^3$.

[9] We also explored alternative geometries of vertical prolate-ellipsoids centered from 6 to 14 km and variable aspect ratios. Figure 2b shows the forward models with $Z = 10.0$, $c = 4.0$, $a = 2.0$, 2.4 km, identical to that used in Figure 2a, and $DV_r = 23–25$ Mm$^3$. The vertical elongation model appears supported by the 2003–05 GPS data, which display a central dimple of vertical displacement better fit by this model close to the conduit (Figure 2a).

[10] Now we address magma volumes and magma compressibility. The compressibility $C$ of saturated magma plus exsolved gas, which is the inverse of effective bulk modulus $\beta$, greatly exceeds host rock. Following the relations of Huppert and Woods [2002], and assuming exsolution occurs at chemical and thermodynamic equilibrium (valid for slow processes), the exsolved volatile content, $n$, derives from Henry’s Law. Assuming water is the dominant volatile species, Henry’s Law constant $s = 4.1 \times 10^{-6}$ Pa$^{-1/2}$ for H$_2$O vapor, $p$ is pressure, and $x$ is crystal content (further details are in the auxiliary material). Assuming $N = 5$ wt% we calculate for a magma chamber depth of 10 km ($\pm$4 km) an average $C = 1/\beta = 7.58 \times 10^{-10}$ Pa$^{-1}$, and average $\beta = 1.32 \times 10^7$ Pa. The assumption of $N = 5$ wt% is justified by data from Barclay et al. [1998], who reported...
as much as 5.05 wt % H₂O from melt inclusions in 1996 SHV lavas and pumice, and by recent data, which have revealed N > 6 wt % in pumice glass samples [Edmonds et al., 2008]. The evidence also suggests an excess vapor phase at depth that includes appreciable CO₂ and SO₂. The range in CO₂–H₂O in melt inclusions in pumice is consistent with an exsolved CO₂–rich vapor phase to pressures >400 MPa [Edmonds et al., 2008]. The significance of these observations is that exsolved volatile phases in addition to H₂O are available to enhance compressibility of magma at depth. [11] Next we correct for the injected (or discharged) magma volume DVisdm and the deflected reservoir wall volume change DVisdr [Johnson, 1992; Johnson et al., 2000], as DVisdm/DVisdr = (1 + 4μ/3β), where μ is shear modulus of the host rock, and β is the effective bulk modulus of resident magma in the reservoir. We assume μ = 5.0 × 10⁶ Pa [Elsworth et al., 2008], yielding a DVisdm/DVisdr = 6.0. [12] Now we apply this relation to the 2005–2007 eruption-deflation episode. The spherical forward model gave DVisdr = −30 Mm³ for volume change of the source cavity, suggesting a corresponding volume of magma withdrawn from the reservoir of −30 × 6.0 = −180 Mm³. The measured volume of erupted lava during this deflation was 316 Mm³ DRE (MVO data). The difference is 136 Mm³, which can be accounted for by injection into the reservoir from a deep source over the course of the episode, with corresponding discharge of an equivalent volume. The average deep influx for this episode is thus 136 Mm³/4.557 × 10⁻⁷ s = 2.98 m³/s. An ellipsoidal model cannot be evaluated strictly with this equation, but as a very rough estimate the implication is a discharged volume of −40 × 6.0 = −240 Mm³, a difference of 76 Mm³ with erupted lava, and a deep influx of ~1.6 m³/s. [13] For the preceding 2003–2005 inflation, the sphere inversion model gave DVisdr = 16.8 Mm³ for volume change of the source cavity, suggesting a corresponding volume of magma intruded into the reservoir of 16.8 × 6.0 = 100.8 Mm³. The average deep influx for this epoch is thus 100.8 Mm³/7.271 × 10⁻⁷ s = 2.00 m³/s. As a rough estimate the ellipsoid model suggests a deep influx of 2.6 m³/s. The steadiness of this calculated magma input, the small magnitudes of input relative to the chamber volume (maybe 0.1% replenishment over 2 years), and the apparent linearity of the volume changes in time (see auxiliary material) suggest that chamber total pressures do not significantly change, and that compressibility as influenced by total pressure and composition stays approximately constant. 4. Discussion [14] The pressure in the reservoir is assumed to increase due to influx of deep magma [cf. Blake, 1981] and through fractional crystallization and volatile oversaturation [Blake, 1984; Tait et al., 1989; Blundy et al., 2006]. In our view the eruption phase is triggered when overpressure reaches a critical value with respect to wall rock tensile strength (a value dependent on reservoir geometry and ambient wallrock stress state), and a dike toward the surface is generated (or reopened), although its geometry may be modified near the surface [Costa et al., 2007]. The pulsatoly behavior of the SHV eruption, reflected in the GPS pattern, indicates a repetition of the process with waxing and waning of reservoir overpressure. With volatile saturated magma containing exsolved bubbles of vapor, the mixture is compressible and reservoir overpressure is only relieved when a significant part (perhaps 1 to 10%) of the reservoir mass is erupted [Bower and Woods, 1998], ignoring any additional deep influx. With relief of overpressure, the conduit seals and the eruption phase is paused. Edifice inflation begins again with a pause in surface efflux, and when overpressure has rebuilt to a critical threshold due to continued deep influx and crystallization, a dike reopens, and an eruptive episode restarts. At present at SHV, three complete 2–3 year cycles of inflation and succeeding eruption/deflation have occurred. A fourth inflation began in April 2007. Thus the current magma reservoir and eruption comprises materials injected since 1992 plus older, partly-molten andesitic materials capable of being remobilized by new hot, volatile rich magma. The upper part of the reservoir contains crystal-rich, highly viscous, gas-saturated, rhyolitic melt (similar to erupted lava), overlying a lower part of crystal-poorer less-viscous but hydrous intermediate to mafic magmas [cf. Annen et al., 2006; Zellmer et al., 2003]. Our models suggest magma is stored in a reservoir centered around 10 km depth, but whose top may be several km shallower in accordance with petrological criteria [Barclay et al., 1998]. [15] Primary aspects of our model are that (1) an exsolved gas phase primarily involving H₂O, CO₂ and SO₂ greatly increases magma compressibility, suggesting that most of the magma volume transferred into or out of the reservoir is accommodated by compression or decompression of stored reservoir magma rather than by quasi-elastic deflection of reservoir walls, and (2) deep influx is both continuous and nearly steady. With respect to (1), our calculations suggest that about 48% of the volume of magma removed from the reservoir in 2005–07 was accommodated by decompression of resident reservoir magma, with 42% recharged by deep influx in 2005–07, and only 10% by inward deflection of the reservoir walls. For the inflation episode of 2003–05, about 83% of the volume of magma injected into the reservoir was accommodated by compression of resident magma, with the remaining 17% taken up by outward deflection of reservoir walls. Johnson [1992] and Johnson et al. [2000] reported comparable numbers for Kilauea volcano for the 1983–1986 Pu‘u ‘O‘o basalt eruption, with only 20–25% by volume accommodated by chamber enlargement, and the rest by compression or decompression of stored magma. [16] With respect to point (2), in both inflation and deflation episodes our results suggest deep influx of the order of 2 m³/s⁻¹, consistent with a steady-state process. The long-term average eruption rate from July 1995 to July 2009 is 1.8 m³/s⁻¹ DRE (MVO data). [17] Finally, estimates of resident reservoir volume appear feasible. A simple approach is to assume bubble compression accounts for accommodation of injected or released magma from the chamber. Assuming bubble porosity of the order ~1 vol% [e.g., Voight et al., 2006], our estimate of 180 Mm³ for decompression-released magma in 2005–07 yields a spherical chamber radius of 1.6 km, or for a cylindrical reservoir from 6–14 km, a radius of 0.85 km. Considerations of magma crystallinity increase these values; a crystal fraction of 0.4 yields sphere radius of 2.2 km, and cylinder radius 1.3 km. The reservoir volume thus is of order of tens of cubic kilometers. Our model appears consistent with both mineralogical constraints indicating shallow storage of some erupted lava, GPS indications of a deeper mean-pressure source when the full reservoir expands or
contracts, and magma budget anomalies. The presence of an exsolved gas phase involving multiple species greatly increases magma compressibility to depths >10 km and suggests that most of the magma volume transferred into or out of the reservoir can be accommodated by compression or decompression of stored reservoir magma with radial dimensions of ~1–2 km.

5. Conclusions

We use well-documented time histories of pulsatory GPS-derived surface deformation and magma efflux to geodeically image magma storage and transfer within the deep crustal system of the Soufrière Hills volcano from 2003 to 2007, with an inflation succeeded by an episode of eruption-plus-deflation. The spherical and prolute ellipsoidal models presented here contrast with the vertically stacked dual–Mogi-type geometry favored by Elsworth et al. (2008). The ellipsoid model, a geometrical idealization for a vertically–elongated shape that can be more complex, better incorporates mineralogical and phase equilibrium constraints indicating relatively shallow storage of erupted lava and GPS-derived surface deformation for the single epoch of eruption and repose (Mattioli et al., submitted manuscript, 2009) that implies a deeper mean–pressure source when the full reservoir deforms. The presence of an exsolved gas phase involving several species greatly increases magma compressibility to depths >10 km, and supports the concept that most of the magma volume transferred into or out of the mid-crustal reservoir can be accommodated by compression or decompression of in situ reservoir magma, which we term the magma-sponge. For both inflation and deflation epochs our results suggest quasi–steady deep, largely mafic magma influx of the order of 2 m s⁻¹. We conclude that the magma released in eruptive episodes is approximately balanced by the accumulated deep influx of the eruptive episode and the preceding inflation. For this model there is no evident depletion of magma reservoir volume through 2007, which comprises tens of km² with radial dimensions of order ~1–2 km.

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References