

High performance thermoelectrics and challenges for practical devices

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Thermoelectric materials can be potentially employed in solid-state devices that harvest waste heat and convert it to electrical power, thereby improving the efficiency of fuel utilisation. The spectacular increases in the efficiencies of these materials achieved over the past decade have raised expectations regarding the use of thermoelectric generators (TEG) in various energy saving and energy management applications, especially at mid-high temperature (400-900 °C). However, several important issues that prevent successful TEG commercialisation remain unresolved in good part because of lack of a research roadmap.

The efficiency of a thermoelectric (TE) material is defined by the dimensionless figure of merit $ZT = S^2\sigma T/\kappa$, where S is the Seebeck coefficient, σ is the electrical conductivity, T is the operational temperature, and κ is the thermal conductivity composed of the electronic contribution (κ_{el}) and lattice contribution (κ_{lat}). However, the power conversion efficiency of a TE device (η) depends not on the ZT maximum at a given temperature, but on the average ZT (ZT_{ave}) over a wide temperature range as well as the temperature difference between the hot (T_h) and the cold source (T_c) as follows:

$$\eta = \frac{T_h - T_c}{T_h} \frac{\sqrt{1 + ZT} - 1}{\sqrt{1 + ZT} + T_c/T_h}$$

Because these material properties (S , σ and κ) are interconnected through both the carrier concentration and electronic structure, the optimisation of any particular property is generally

performed at the expense of another property, which makes the achievement of high ZT values very challenging¹. Effective routes to increasing ZT include electronic structure modifications such as electronic band structure engineering and the generation of extrinsic defects through alloying and nanostructuring to lower the lattice thermal conductivity.

A small but important commercial area where the first-generation TE devices and modules have already been successfully employed was the long-term space exploration conducted by the United States National Aeronautics and Space Administration (NASA) and the Soviet Union. Similar to the original Voyager 1 and Voyager 2 missions the recent Mars 2011 (rover Curiosity, November 2011) and 2020 missions (rover Perseverance, July 2020) are equipped with a radioisotope TE power system, and future Mars missions will also rely on the same system of electrical power generation. Using heat from the radioactive decay of plutonium oxide, this system produces dependable electricity that charges the rover's two primary batteries, and its TE modules are composed of the first-generation PbTe/tellurium–antimony–germanium–silver (TAGS) materials manufactured by Teledyne. The long-term reliability possible by TE generators (TEGs) was proven by these and other NASA missions where none has ever failed because of failure in the TE power generation system. After the long dormant period in research activity caused by the frustration over unsuccessful attempts to further enhance performance, TE materials have attracted significant attention from researchers during the past two decades. As a result, tremendous progress has been made in increasing the figure of merit. The field has bloomed with an outburst of new concepts and ideas that were subsequently implemented to break the four-decade old ZT records established in the 1950s and 1960s. The result was a new generation of materials developed since the early 2000s that significantly exceeded the expectations (the timeline of these advances is shown in **Box 1**). We note that there is considerable progress on development of organic, hybrid organic-inorganic, and inorganic thermoelectric materials and devices toward room temperature energy harvesting^{2, 3, 4}, which will not be discussed within the scope of this perspective because their ZT values are not on a comparable level yet to those of the inorganic counterparts. The new figures of merit achieved by the new materials

exceeded the old values by more than a factor of two and widely considered to be adequate for their implementation in modern TE devices with efficiencies greater than those of the state-of-the-art devices by more than 100%. However, the development of corresponding TE devices and modules that can transform heat to electricity using high-temperature sources operated between 400 and 900 °C has proceeded very slowly.⁵ The question is ‘why’?

Key developments in TE material improvement over the past 15 years

The “first-generation” materials employed in TE devices decades ago had power conversion efficiencies (PCE) of 3–6% in the temperature range of 300–1000 °C. The new materials could easily achieve PCE between 12 and 15%, which would be a remarkable breakthrough considering the conversion of low-quality energy (heat) to high-quality energy (electricity). It is reasonable to expect that such large PCEs would be commercially viable for a variety of applications. Practical TEGs can be divided into stationary and mobile ones. In the stationary generators, the hot side temperatures tend to be stable, and some parameters that may affect the device performance (such the overall weight and sensitivity to vibration) are typically relaxed. However, in mobile applications (such as those harvesting exhaust waste heat in vehicles), additional challenges include temperature fluctuations of the hot source and mechanical vibrations negatively affecting the device integrity and stability.

Various economic factors, such as the long-term uncertainty in the price of fossil fuels, are also stifling the development of TE devices on a commercial scale. For example, to recover waste heat in automobiles, the accrued energy savings can be used as electrical power to extend the vehicle mileage.⁶ These savings must be substantial and significantly exceed the TEG cost. Over the past decade, crude oil price fluctuations resembled a rollercoaster, and their long-term average values exhibited a decreasing trend. Although it is difficult to accurately predict the price of crude oil, its value should sustainably well above current prices to stimulate utilisation of TE generators in automobiles. Because taxation strongly affects the fuel price, certain countries with high gasoline taxes may reach this level sooner than others.

Stationary applications of TEGs can involve large units installed in the industrial facilities⁷ that are utilised for various manufacturing processes emitting large amounts of waste heat. To date, the number of commercially available TEGs is very small and affects only very few niche applications. These generators still use the first-generation materials, specifically bismuth telluride alloys and lead telluride.

The vehicles that can be considered viable candidates for the implementation of TEGs include semi-trucks, which run more a hundred thousand miles per year at a fuel economy of approximately six miles per gallon. Therefore, even at the 5% minimum energy savings achieved by TEG utilisation, approximately \$6,000/y can be saved, which translates into \$90,000 over the vehicle lifetime of ten to fifteen years. For personal vehicles, the savings would be considerably smaller.

What is holding back the development of high efficiency TEGs containing the new high-performance materials? The key technical obstacles are related to the thermal stability of the electrical contacts attached to the hot generator side; the mechanical stability and the long-term chemical stability of TE materials, which must be maintained for at least ten years; under the hot side.

It is interesting to compare the current development stage of TE technology, and little progress made in creating commercially viable energy converters, to the robust advances in the photovoltaics field. In the latter, the last two or three decades have also been transformational in the development of photovoltaic semiconductors with increased efficiency. This process has resulted in a flourishing and rapidly growing solar photovoltaic technology with falling costs and an industry with a market size of billions of dollars. What is particularly striking is the speed at which the recent emergence of perovskite halides as materials for solar cells has led to a budding industry currently on the cusp of commercialisation. The field of thermoelectrics has analogous advances in new materials

but there is a striking lag to the development of devices as mentioned above and very few researchers have the capability to fabricate TE power-generating devices.

Owing to the advances and breakthroughs in TE materials, this *perspective* discusses their potential to be implemented in devices and modules with a focus on TE power generation. After classifying the materials in terms of operating temperature, those most likely to be used in future devices are briefly discussed. We also discuss the key challenges and possible future strategies that can promote the further development of TE power generation technology, however, more extensive and comprehensive reviews can be found elsewhere.^{5, 6, 8, 9 10} This perspective does not discuss TE cooling devices as they have existed for decades, and no corresponding enhancements in material performance have been achieved.

The powerful general design concepts devised more than a decade ago that have remarkably enhanced the performance of bulk TE materials are:¹¹ endotaxial nanostructuring involving the nucleation, growth, and spinodal decomposition processes that reduce the thermal conductivity of a material; electronic band alignment, electronic band convergence, resonance states, and electronic structure modification that enhance the power factor ($S^2\sigma$); and panoscopic all-scale architecturing that combines all beneficial effects into a single material system. In particular, proper band alignment is very important for achieving high power factors for two-phase nanostructured composites^{12, 13}. In this case, a designed composition contains two separate phases with energy-aligned conduction or valence bands to facilitate carrier transport while actively scattering heat-carrying phonons. Electronic band convergence has been critical for tuning the electronic structure to achieve the maximum power factor. It involves the modification of separate electronic bands of the same carrier type aimed to converge their energies and substantially increase their contributions to carrier transport^{13, 14}. Because each band makes its own contribution to the Seebeck coefficient on a weighted basis, strong enhancement can be achieved while maintaining high electrical conductivity. Some of the performance optimization process in 1st generation ternary TE

materials, e.g. $(\text{Bi}_{0.2}\text{Sb}_{0.8})_2\text{Te}_3$, is related to the band convergence, but was not referred to specifically as such.¹⁵ The Pb-based chalcogenides (PbTe, PbSe, and PbS), filled skutterudites ($\text{REM}_4\text{Sb}_{12}$: RE = rare earth, M=Fe, Co, or Ni) and half-Heusler (HH) alloys are the key systems in which the above concepts led to superior performance characteristics. In terms of their ZT_{max} and ZT_{ave} values achieved during operation in the mid-temperature range, lead tellurides are the most promising materials, followed by complex filled skutterudites. However, in terms of mechanical strength (a key feature for the actual electronic devices), skutterudites and HH alloys are the most promising materials followed by tellurides. In addition to these concepts, there were discoveries of compounds with unprecedented ZT performance such as SnSe, MgAgSb, Mg_3Sb_2 , $\text{Yb}_{14}\text{MnSb}_{11}$ and $\text{La}_{3-x}\text{Te}_4$.

This article is organised as follows. First, it discusses the recent advances in the development of high-performance TE materials, especially those with high stability, low manufacturing costs, and high scalability. Second, it describes the demand for novel TE device fabrication technologies based on these materials and the current state. Third, it considers the key challenges and possible strategies for transitioning to high efficiency devices and modules that will open the path to broader use and commercialization. Fourth, it concludes that the main reasons for the absence of available TE devices and modules based on the materials are knowledge gaps in how to develop stable high-temperature electrical and thermal interfaces.

The most important breakthroughs in new TE materials occurred in the mid-temperature range from 300 °C to approximately 650 °C, which matches the majority of heat sources suitable for energy harvesting and thus TE devices will produce the strongest impact. Above 650 °C, their implementation is considerably more challenging because the stability requirements become even more severe not only for the TE materials, but also for many other components of the devices and modules, including heat exchangers. Therefore, the prospects for harvesting the energy of high-temperature heat sources via solid-state TE technology are more remote than for mid-temperature sources. Leading materials systems for applications above 650 °C include the HH alloys $\text{Nb}_{1-x}\text{Ti}_x\text{FeSb}$ and $\text{Nb}_{1-x}\text{Hf}_x\text{FeSb}$ with a

ZT of ~ 1.5 at 1200 K^{16, 17} and a promising ZT_{ave} of ~ 1 (500–1200 K)¹⁶, $\text{La}_{3-x}\text{Te}_4$ with a ZT of ~ 1.2 at 1200 K¹⁸ and $\text{Yb}_{14}\text{MnSb}_{11}$ with a ZT of 1.3 at 1223 K through suitable doping.¹⁹

TE modules from high performance materials and related challenges

General requirements for practical modules

To fabricate reliable TE power generation modules, it is important to realise very stable low-resistance electrical contacts (especially on the hot generator side) between the connecting electrodes and TE materials. A TE module is to be exposed to high temperatures, which can result in a chemical reaction and/or atomic diffusion at the electrode–material interface, leading to its instability and degradation. This extreme environment set in motion several complex phenomena that promote the development of detrimental secondary phases that reduce module conversion efficiency. Therefore, efficient and very stable diffusion barriers between the connecting electrodes and TE materials are required to prevent the chemical reactions and/or atomic diffusion. This is a nontrivial challenge because such barriers must also have low electrical contact resistance (in the magnitude of a few $\mu\Omega\text{cm}^2$) and be tailored to the specific TE materials. It requires a clearer fundamental understanding of these parasitic processes and more basic research on this subject. The coefficients of thermal expansion of TE materials, electrodes, barrier materials should match well to reduce thermomechanical stresses which degrade stability. One reason for the sparse basic research conducted in this area has been the broad perception that this essentially is an easily tractable device engineering problem that can be solved empirically. TE materials with good mechanical properties are critical for device modules with long service lifetimes. Vickers Hardness and Fracture Toughness are often used to gauge the mechanical performance of the TE materials. Some published works on TE devices, TE materials, module efficiency tests, have reported values of Vickers Hardness > 1 GPa and Fracture Toughness > 1 MPa $\text{m}^{1/2}$ which can serve as rough guide for the required mechanical properties for practical device applications, however, these may vary for different applications (e.g. stationary, mobile etc).

PbTe based modules

The so-called legacy (first-generation) PbTe-based modules developed in the 1960s and 1970s exhibited a PCE of 5.1% at $T_h = 783$ K and $T_c = 366$ K^{20,21}. The efficiencies of the second-generation modules containing nanostructured PbTe-based materials (**Fig. 1a**) exceeded those by more than 100%. A low contact resistivity of below 10 mΩ cm was important for the minimisation of thermal losses. For example, modules constructed from p-type PbTe–MgTe (second generation, $ZT \sim 1.9$) and n-type PbTe (first generation) materials demonstrated PCE $\sim 8.5\%$ at $T_h = 873$ K and $T_c = 283$ K^{22, 23}. Based on a simulated temperature distribution a subsequent segmented module was designed utilising legacy $\text{Bi}_{2-x}\text{Sb}_x\text{Te}_{3-y}\text{Se}_y$ alloys on the cold side of the TE legs to increase the PCE at lower temperatures up to 12% (**Fig. 1b**). The key to this successful demonstration was the fabrication process, which employed the pressure-assisted sintering of TE materials with diffusion barriers such as Fe and 80% Co-20% Fe-based alloys²³. The theoretically predicted efficiency for this cascaded module was 15.6%, which included 23% losses experienced by an early experimental module due to the high resistance of electrode contacts. These losses pointed to the necessity of significant design improvements and were ultimately minimised to approximately 5–10% of the theoretical efficiency. Thermal cycling stability is another critical aspect of commercial applications. Generally, PbTe-based TE modules demonstrate good thermal stability at $T < 793$ K. In the PbTe–MgTe-based module, a slight decrease in PCE was observed during operation at $T_{\text{tot}} = 873$ K for 24 h, while no apparent changes were detected at $T_{\text{hot}} \leq 773$.²³ The corresponding module comprising the nanostructured $\text{Pb}_{0.953}\text{Na}_{0.040}\text{Ge}_{0.007}\text{Te}$ p-type leg (**Fig. 1a**) with T_h and T_c maintained at 873 K and 283 K, respectively, produced 2 W with promising stability and $\sim 12\%$ PCE (**Fig. 1c-f**). In addition, the n-type $(\text{PbSn}_{0.05}\text{Te})_{0.92}(\text{PbS})_{0.08}$ TE material ($ZT \sim 1.5$) was used to build a uni-coupled module²⁴ by coupling with p-type $\text{Ge}_{0.87}\text{Pb}_{0.13}\text{Te}$ ($ZT \sim 2.2$). A high PCE of 12% was achieved at $T_{\text{hot}} = 773$ K, and $T_{\text{cold}} = 323$ K with $P_{\text{max}} = 0.145$ W, close to the theoretically predicted PCE of 13.6% and $P_{\text{max}} = 0.16$ W.

Te is a rare metal with an abundance of ~0.001 ppm in the earth crust, and is mainly obtained as the by-product of the electrolytic refining of Cu.²⁵ The annual production of Te is difficult to assess estimated to be ~1000 tons, which potentially can become a scale up bottleneck for TE devices using PbTe. Thus, the use of PbSe or PbS instead of PbTe in TE devices has been considered by researchers.^{26, 27, 28, 29} The implementation of Pb(S, Se) materials would not only lower the costs, but because of their higher melting points they could increase the operational temperature for higher efficiency and results in higher Vickers hardness than PbTe. A recent report described a demonstration in a thermoelectric device with ZT_{\max} in the range 1.5-1.9 at around 700-900K.³⁰ Using a heavily alloyed composition $\text{Pb}_{0.99-y}\text{Sb}_{0.012}\text{Sn}_y\text{Se}_{1-2x}\text{Te}_x\text{S}_x$ segmented with n-type Se-doped Bi_2Te_3 as the n-type leg and coupled with a typical p Na-doped PbTe segmented with $\text{Bi}_{2-x}\text{Sb}_x\text{e}_3$ as the p-type leg. An eight-couple module produced 3.1 W of power corresponding to the maximum conversion efficiency of 12.3% with $\Delta T = 507$ K and current $I = 3.7$ A. The simulated highest conversion efficiency of the segmented module was 13.9% at a temperature difference $\Delta T = 513$ K. The slightly lower efficiency compared to the theoretical one was attributed suboptimal electrical contact resistance. Here, too the use of Te may be problematic for broad based uses of Bi-Sb-Te compounds as the most used segmented modules for low temperature. Thus, alternative Te-free compounds are highly desirable. Recently, high efficiencies of 6.5~7.3% have been achieved at low temperatures (<593 K) for devices with Mg-Sb based compounds (e.g. Mg_3Sb_3 ³¹ or $\text{Mg}_3(\text{Sb, Bi})_2$ ³²), which makes promising for scalable applications.

The high mechanical strength is rare in the top performing TE materials but is necessary for viable module fabrication. PbTe single crystals exhibit a low Vickers hardness of approximately 0.3 GPa, which can be increased to 0.8 GPa through Na doping³³. Hot-pressed polycrystalline PbTe pellets containing 5–10mol% PbS possess a higher Vickers hardness values up to 1.2 GPa, which is still lower than those of skutterudite and HH alloys (3–4 GPa).³⁴ Further enhancements of the material mechanical strength are desirable to increase the resistance to mechanical fracture during operation. In this regard, replacing Te

with S or Se in PbTe as in $\text{Pb}_{0.93}\text{Sb}_{0.05}\text{S}_{0.5}\text{Se}_{0.5}$ which exhibits a Vickers hardness above 2.0 GPa is another advantage²³.

A study on PbTe evaporation revealed that for the device operated at $T_{\text{hot}} = 793$ K and $T_{\text{cold}} = 333$ K, some reduction in the cross-sectional area was observed due material sublimation occurred at distances of 0.5 and 1.1 mm from the hot generator side after 456 h³⁵. This suggests that high thermal stability of TE devices can be achieved if a proper threshold is maintained for the high-temperature side. Recent studies on this topic are promising, such as those on Ga-doped PbTe-GeTe with $ZT_{\text{average}} = 1.27$ between 400 and 773 K³⁶.

Skutterudite-based modules

Skutterudite-based TE materials have been favourites for TEGs because of attractive mechanical properties (corresponding to a Vickers hardness of 4 GPa and flexural strength up to 180 MPa for Yb-filled CoSb_3)³⁷ and sufficiently high ZT values.³⁸ A 4×4 leg device was built using $\text{Yb}_y\text{Co}_4\text{Sb}_{12}$ ($ZT \sim 1.5$) as the n-type component and $\text{Ce}_y\text{Fe}_3\text{CoSb}_{12}$ as the p-type component achieved an energy conversion (η) of 8.4% with $\Delta T = 577$ K and $T_{\text{hot}} = 873$ K³⁹. An 8×8 leg device (**Fig. 2a**) using CoSb_3 as both the n-type (doped with Yb, Ca, Al, and Ga; $ZT \sim 1.2$) and p-type (doped with Pr, Ti, Ga, Ba, and Fe; $ZT \sim 0.85$) components has been fabricated as well⁴⁰. The PCE and maximum power output (P_{max}) were $\sim 9.1\%$ and ~ 42 W at a current of ~ 15 A and ΔT of 600 K (**Fig. 2b**). In segmented TE modules composed of Bi_2Te_3 /skutterudite⁴¹, PCE reached $\sim 12\%$ with ΔT of 540 K.

The above-mentioned tests were performed in controlled gas environments (such as Ar or N_2). The results of a durability test conducted on skutterudite legs during thermal cycling in an open atmosphere revealed that their failure mainly resulted from oxidation and interlayer diffusion processes⁴². If crack generation occurs typically on the hot side of the TE legs, it increases the internal resistance and decreases the open circuit voltage (V_{oc}), **Fig. 2c**.

Mitigation efforts include interfacial barrier layer and packaging protective against oxidation. A recent study on the screening of barrier layers involving density functional theory modelling revealed that Nb electrode could be used to effectively inhibit the interfacial reaction⁴³. A

subsequent experimental study on such a skutterudite/Nb junction showed stable hot side interfacial resistance for up to 100 d at 848 K with PCE of 10.2% and P_{\max} of 4.1 W at ΔT of 574 K, **Fig. 2d**. In addition to the above, Sb sublimation losses at $T > 873$ K causing composition changes represent a potential risk that degrades the performance of CoSb_3 -based TE devices⁴⁴. To minimise it the skutterudite-base materials can be chemically engineered to shift the ZT peak to lower temperatures. This concept was tested on two-leg devices⁴⁵ containing n-type $\text{Yb}_{0.25}\text{Fe}_{0.25}\text{Co}_{3.75}\text{Sb}_{12}$ ($ZT \sim 1.3$ at 740 K) and p-type $\text{La}_{0.7}\text{Ti}_{0.1}\text{Ga}_{0.1}\text{Fe}_{2.7}\text{Co}_{1.3}\text{Sb}_{12}$ ($ZT \sim 0.97$ at 760 K), which demonstrated an efficiency of 7.2% at a ΔT of only 366 K ($T_{\text{hot}} = 679$ K).

Half-Heusler modules

The half-Heusler HH compounds with the XYZ formula (X and Y: transition or rare earth metals, Z: p-block elements) exhibit robust mechanical strength, versatile composition, high thermal stability, and reasonably high ZT values. For these reasons, some of these materials can potentially be used in practical applications. However, their synthesis is a complex procedure due to the very high temperature and activation energy. The recent development of p-type HH materials with high ZT values considerably increased the efficiencies of the corresponding modules^{46, 47}. A 4×4 leg TE device⁴⁷ with $\text{FeNb}_{0.88}\text{Hf}_{0.12}\text{Sb}$ ($ZT \sim 1.5$ at 1200 K) as the p-type leg and ZrNiSn ($ZT \sim 1.0$ at 950 K) as the n-type leg exhibits a PCE of 6.2% at $\Delta T = 655$ K with $T_{\text{hot}} = 1000$ K, **Fig. 2e**. Here, Hf doping of the p-type legs is used to decrease the lattice thermal conductivity, however, Hf is expensive, and its use may lead to unfavourable material costs. To avoid Hf, Bi-doped ZrCoSn ⁴⁸ and Ti-doped TaFeSb ⁴⁹ have been proposed for p-type HH materials with ZT values of 1.4–1.5 at 973 K. The single-leg modules based on these HH alloys demonstrate PCEs of 9.0–11.4% in the T_{hot} of 823–973 K and $T_{\text{cold}} = 300$ K, **Fig. 2f**.

The optimisation of geometrical parameters is useful for minimising heat and electrical losses and predicting increases in η and P_{\max} . This was done using finite element analysis for a 4×4 leg device consisting of n-type $\text{Hf}_{0.5}\text{Zr}_{0.5}\text{NiSn}_{0.98}\text{Sb}_{0.02}$ ($ZT \sim 1.03$) and p-type

(Nb_{0.8}Ta_{0.2})_{0.8}Ti_{0.2}FeSb ($ZT \sim 1.12$).^{50, 51} At close ZT values of the p-type and n-type legs in this example⁴⁷, a PCE of 8.3% and P_{\max} of 8.5 W were reported for this single-stage TE device⁵¹. Segmented modules were prepared with n-type Zr_{0.5}Hf_{0.5}NiSn_{0.985}Sb_{0.015} and p-type Zr_{0.5}Hf_{0.5}CoSb_{0.8}Sn_{0.2} HH compounds on the hot side and Bi₂Te₃ on the cold side⁵⁰. The obtained 4×4 leg device exhibited a record high PCE of 12.4% with a maximum area power density of 1.5 W/cm². Adding nanoparticles as inclusions to HH alloys to form nanocomposites is a promising method for reducing their thermal conductivity. A uni-coupled thermoelectric device fabricated from (Hf_{0.6}Zr_{0.4})NiSn_{0.99}Sb_{0.01}/W nanocomposite (n-type) and Hf_{0.5}Zr_{0.5}CoSb_{0.8}Sn_{0.2} (p-type) possessed a PCE of 10.7% and area power density of 13.9 W/cm² with $\Delta T = 674$ K⁵². This device exhibited no apparent performance degradation after 10 thermal cycles conducted between 373 and 1027 K. For successful commercialisation of HH alloy-based TE devices, the manufacturing costs must be low by avoiding expensive elemental components and developing a synthetic approach with a lower energy input. Although thermal cycling of HH alloy-based devices was performed in the past^{52, 53}, these cycles were either too few (only 10 thermal cycles were conducted for a (Hf_{0.6}Zr_{0.4})NiSn_{0.99}Sb_{0.01}/W-based TE device⁵²) or performed at a too low temperature (up to 873 K for a Zr_{0.5}Hf_{0.5}CoSb_{0.8}Sn_{0.2}-based device⁵³). Therefore, longer tests lasting thousands of hours at $T_{\text{hot}} > 1000$ K and post-mortem studies with a focus on the interfacial region close to the hot side are required to further understanding device reliability.

Mg₂Sn_{1-x}Si_x-based modules

Mg₂Sn_{1-x}Si_x-based TE devices have been widely explored due to several attractive features, including the presence of nontoxic elements. Encouraging results have been reported for the Mg₂Si TE devices with Ni electrodes prepared using a plasma-activated sintering technique, which exhibited no performance deterioration after aging for 1000 h.⁵⁴ Unfortunately, the effectiveness of the p-type counterpart of Mg₂(Si,Sn) is very low ($ZT \sim 0.7$ at 750 K)⁵⁵. The volatile nature of magnesium at moderately high temperatures results in phase instability, compositional changes, and degradation of the TE properties. Despite enormous efforts, these drawbacks have significantly limited commercial applications.^{54, 56, 57, 58, 59, 60, 61} A single

leg (3.6 mm × 3.6 mm × 4.35 mm) of polycrystalline n-type Mg₃Sb₂-based material, in which In₅₂Sn₄₈ and Ag₅₆Cu₂₂Zn₁₇Sn₅ were used as brazes for the cold and hot sides, respectively, demonstrated a PCE of 10.6% at a temperature gradient of 400 K (T_{hot} = 773 K). This is among the highest efficiencies obtained for this temperature difference⁶². However, the large-scale application of Mg₃Sb₂-based generators is currently impeded by challenges related to the material and device fabrication procedures.

Nascent SnSe modules

The recent discovery of SnSe single crystals with record-breaking ZT values above 2.6 in the temperature range of 600–700 °C and their availability in both p-type and n-type forms have raised expectations for SnSe-based TE devices in the near future.^{63, 64, 65, 66} This is particularly true in the light of new developments suggesting that polycrystalline compactions can achieve efficiencies close to those of single crystals. Currently, applications of SnSe in devices is limited by their poor mechanical properties of single crystals.⁶⁷ But the mechanical properties of polycrystalline SnSe are better (Vickers hardness: 669 MPa, flexural strength: 21 MPa, fracture toughness: 0.62 MPa m^{1/2}). To date, very few SnSe-based TEGs have been reported. A p-type polycrystalline SnSe-based power generator was built by a pseudo-three-dimensional (3D) printing method with a small peak output power of 20 μW with T_{hot} = 772 K (**Fig. 3a**)⁶⁸. A recent study showed coupling n-type Sn_{1-x}Pb_xSe legs (ZT=2.5) with p-type Bi₂Te_{2.7}Se_{0.3} delivered a conversion efficiency of 4.4% with ΔT=200 K⁶⁹. This efficiency is much lower than the expected value because of suboptimal electrical contact between the electrode and the legs. Therefore, finding effective metallisation layers is critical for SnSe-based devices. Initial results have highlighted how challenging it can be. For example, a single Ag metallisation layer was unable to inhibit the diffusion of Sn atoms into the Ag layer, resulting in a high contact resistivity of 7.03 mΩ·cm². Meanwhile, the application of a single Ni metallisation layer generated surface cracks because of the different thermal expansion coefficients of the various Ni-based compounds, such as Ni₁₇Sn₃, Ni₃Sn, and Ni_{5.63}SnSe₂⁷⁰. An Ag/Co/Ti metallisation multilayer achieved a specific contact resistance of 1.53 mΩ·cm²,

lower than that a single Ag layer, but still much higher than the contact resistances of commercial bismuth antimony telluride devices⁷¹.

Cu₂Q (Q= S, Se, Te) modules

Cu₂Q p-type materials are highly promising TE materials with $ZT = 1.5$ at 1000 K for Cu₂Se and $ZT = 1.7$ at 1000 K for Cu₂S^{72, 73}. These materials show good electronic transport properties and intrinsically low lattice thermal conductivities of the phonon–liquid electron–crystal frameworks. Unfortunately, the same liquid-like mobility also decreases stability due to electromigration of Cu ions in the samples destroying the TEG modules. This was deemed to be insurmountable and led to the termination of decade-long research studies mainly by NASA's Jet Propulsion Laboratory⁷⁴. Recent strategies, however, employing electrically conductive but ion-blocking secondary phases or interfaces show that the long-range Cu ion electromigration can be hindered potentially allowing stable devices to be studied^{75, 76, 77}.

Potential Yb₁₄MnSb₁₁ modules

The Yb₁₄MnSb₁₁ compound is a promising material for power generation in the temperature range of 975–1275 K with a peak ZT of 1.0 at 1223 K⁷⁸. The ZT value can be further increased to 1.3 at 1223 K through suitable doping.¹⁹ Yb₁₄MnSb₁₁ shows good compatibility with other state-of-the-art p-type TE materials, which can be used to prepare segmented modules in various temperature ranges. A high PCE of 18.6% was predicted for a segmented p-type leg composed of Yb₁₄MnSb₁₁/CeFe₄Sb₁₂/TAGS/(Bi, Sb)₂Te₃ with $\Delta T = 975$ K ($T_{\text{hot}} = 1275$ K and $T_{\text{cold}} = 300$ K)⁷⁸. Yb₁₄MnSb₁₁ exhibits good mechanical properties (Vickers hardness: > 3 GPa)⁷⁹ and high thermal stability (no vapor losses up to 1395 K with La doping)⁸⁰, and can be produced by a scalable ball-milling process under Ar atmosphere⁷⁹. However, no experimental testing of functional modules or single-leg devices fabricated from Yb₁₄MnSb₁₁ has been reported. The material would be almost exclusively used in space applications because of the cost-prohibitive nature of its composition.

Based on above discussion, a summary table I of the materials properties and device efficiency are shown below. For mid-high temperature operation, the thermal expansion matching is essential for module reliability. Because of the heavy atoms present the top-performing thermoelectrics, they tend to have a soft lattice nature and thus high thermal expansion coefficients. On the contrary the best metal electrodes have much lower ones by a factor of 2 to 4. How can such contacts achieve very low resistivity that must be maintained and survive the large temperature fluctuations? It is known that doping or adding secondary phases can tune the respective thermal expansion coefficients and this could be a way to mitigate these issues to a certain extent. It has been demonstrated, by matching the thermal expansion of n- and p- types Half-Heusler, the interfacial shear stresses can be reduced by 40% and significantly improve the reliability.⁸¹ For segmented modules with Bi_2Te_3 , both thermal expansion and dimension of the segment components should be consistent between n- and p-type legs. Therefore, continued innovations in design are needed to reconcile the thermally disparate materials.

Future research directions

Despite the tremendous progress in the field of TE materials for power generation, commercialisation and practical implementation of TEGs proceed very slowly. Currently, the fabrication of commercial Bi_2Te_3 π -type module is fully automated in each step and is capable for mass production. However, module fabrication using the newly developed high-ZT materials is not a trivial task and is required for practical TE power generation. There is a long way yet to go, before addressing the jugular issues, and a viable heat to electricity conversion industry for widespread TEG use. Beyond sporadic activities, no systematic basic research is being conducted to solve the problems blocking the full development of modules based on the new TE materials. Basic ongoing research focusing needs to be expanded beyond only increasing ZT to tackle all the other issues discussed above. Therefore, future research directions will need to be aimed at addressing simultaneously these key challenges all of which have to do with mechanical strength and interfaces. The mechanical and fracture strength of most high-performance thermoelectric materials is poor

with a few exceptions such as the HH alloys and perhaps the skutterudites (**Fig. 3b**). *Is it possible to raise the toughness and fracture strength of the new high ZT materials or to mitigate the risk of cracking during operation via innovative device design?* In general, most high-performing thermoelectric materials tend to have high thermal expansion coefficients whereas the best metal electrodes are low (**Fig. 3c**). The differences in thermal expansion coefficients across the interfaces of the materials in any given module will inevitably cause cracking at the interface and electrical discontinuities and will have to be reconciled. The development of metal electrodes matching the thermal expansion coefficients of TE materials will be required to create stable low resistance electrical contacts for high temperature operation. This can be realized either by alloying metals with various thermal expansion coefficient or by clever architectures design such as multiple layers. From Table I, the thermal expansion coefficient of TE materials (except Cu₂Se) usually ranges at 10-20 10⁻⁶ K⁻¹, while metals such as Cu, Ag, Ni, Co and Ti have a thermal expansion coefficient between 1 10⁻⁶ K⁻¹ to 20 10⁻⁶ K⁻¹,^{82, 83} which makes the strategy possible. Electrodes with low resistance contacts must be achieved both at the high temperature and low temperature and of the thermoelectric leg. This is more difficult to achieve on the high temperature end of the device. The understanding of effective diffusion barrier layers to the electrode joints on the hot side is crucial. Obviously, there are other factors that go into overall mechanical strength such as yield strength and fracture toughness. These are properties for which we do not know much about for most of the high-performance thermoelectric materials as even small compositional modifications typically done to optimize ZT also change these. *What is the cutting-edge fundamental material science that needs to be done to try to increase the mechanical strength or at least learn to live with low strength by ingenious designing devices that are tolerant to this weakness?* The interface stability as a function of temperature, temperature fluctuations, and time will need to be understood at a fundamental level and controlled. Specifically, reactions between electrodes and TE materials and creation of new detrimental phases are the most worrisome. A moderate diffusion rate at the interface is essential for the formation of a strong interface, but a rather rapid or extensive one could lead to the unwanted degradation of TE materials. For development of stable metallization at

high temperature, high throughput methods should be a useful strategy to identify viable electrode systems.⁴³ The potential for chemical sublimation of TE materials during operation can be a problem and must be mitigated or suppressed by developing low-cost protective media including, various epilayers, as well as argon or helium gas (more conventional gases such as nitrogen or carbon dioxide can be also applied for this purpose). Solid insulation coatings containing silica, certain types of ceramics, phosphate glasses, and lead oxide enamels may decrease the sublimation rates of TE materials as well; however, the latter would require proper engineering to prevent failure due to rupture. In view of the above-mentioned key challenges for TE devising, a transverse TE device⁸⁴ is worth highlighting. In such devices, the electrical contacts are made only on the cold sides, which avoid the concerns on the instability of the interface and contact of the hot sides as in conventional devices. A high device ZT of ~ 0.7 has been achieved for Re_4Si_7 single crystal in a transverse TE device.⁸⁴ Such devices may not be applicable to all TE materials because it has special requirements for anisotropic transport properties along different crystal axis for p- and n-type carriers requiring single crystals. The subfield of transverse thermoelectrics is undeveloped as a result. For TE materials with symmetric crystal structures or polycrystalline nature, constructing multi-layer heterostructures may be necessary, where, however, only very low ZT values ($\sim 10^{-2}$) have been demonstrated. Although there are additional issues to overcome including optimal thermal interfaces to efficiently guide the heat from the source through the devices and resist detachment, the aforementioned challenges are make-or-break propositions. These are not necessarily just engineering issues. There has to be considerable basic research focus to raise our fundamental understanding as tackling these challenges will define the lifetime of the TE modules which will have to be in the order of a decade or two. A scientific and technological research roadmap is needed to highlight necessary steps to transition from real advances in ZT research into a viable TEG technology. The stability, reliability and efficiency of thermoelectric devices and modules need to be measured reliably and this is not trivial. The development of TE modules and TEGs is in a similar state as the materials research was 20-30 years ago only the challenges are more severe. Therefore, such work currently is only being done in very few Laboratories

with home-build systems. The availability of easy to use commercial device and module measurement systems for use by non-specialists will produce reliable data that can be compared across different labs is necessary. It may also be useful to establish third-party agencies for standard evaluation of the TE device performance, similar to what currently is done in photovoltaic device research, for reliable comparison between different materials and devices reported by different groups. In addition, several new engineering approaches have been developed to fabricate planar and vertical TE devices including laser direct sintering⁸⁵, tape casting⁸⁶, and vacuum filtration⁸⁷, where these methods still use Bi-Te commercial powder in device fabrication. Similar processing techniques could be adapted for the new TE materials. We are optimistic that future research focusing on bridging the chasm between the materials discovery and development on the one hand and the device/module engineering communities on the other will achieve meaningful advances in broad based module development.

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Author contributions

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Competing interests

The authors declare no competing interests.

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Table I. Summary of properties and device conversion efficiency of discussed materials

Material	Peak ZT	Linear Thermal Expansion ($\times 10^{-6} \text{ K}^{-1}$)	Vickers Hardness	Fracture Toughness	PCE (%)	Melting/Decomposition Point	Operation Temperature range
PbTe-based	1.4 (n) ²⁴ 2.2 (p) ²⁴	$\alpha_{373-773 \text{ K}} = 19$ to 20 (n & p) ^{*j} ^{88, 89}	0.3 GPa ^{33, 90}	0.59 MPa m ^{1/2} ^{33, 90}	14.0 (n) ²⁴ (T _{cold} = 323 K, T _{hot} = 773 K)	1190-1210K	500-900K
PbSe-based	1.8 (n) ³⁰ 1.7(p) ⁹¹	$\alpha_{300\text{K}} = 19.4$ (n & p) ^{*j} ⁹²	0.18 GPa ⁹³	0.67 MPa m ^{1/2} ⁹⁰	12.3 (n) ³⁰ (T _{cold} = 293 K, T _{hot} = 800 K)	1340-1350K	600-1000K
Skutterudite-based	1.7 (n) ⁹⁴ 1.45 (p) ⁹⁵	$\alpha_{473-873 \text{ K}} = 10$ to 12.2 ^{*ii} , ⁹⁶ , ^{97, 98} 14.5 ^{*iii} ⁹⁶	4.2 GPa ⁹⁹	1.49 MPa m ^{1/2} ¹⁰⁰	9.1 (n) ⁴⁰ (T _{cold} = 323 K, T _{hot} = 923 K)	1137-1147K ¹⁰¹	500-900K
Half-Heusler-based	1.0 (n) ¹⁰² 1.5 (p) ¹⁰²	$\alpha_{200-800 \text{ K}} = 8.6$ to 12.1 ^{*iv} , ¹⁰³ , ¹⁰⁴ 10.6 to 12.9 ^{*v} ^{103, 104}	8.5-14.4 GPa ¹⁰³	2.1 MPa m ^{1/2} ¹⁰³	6.2 (p) ¹⁰² (T _{cold} = 336 K, T _{hot} = 991 K)	--	>900K
Mg ₃ Sb ₂ -based	1.7 (n) ¹⁰⁵ 1.3 (p) ¹⁰⁶	$\alpha_{300-773 \text{ K}} = 22.3$ (n & p) ^{*j} ¹⁰⁷	1.1 GPa ¹⁰⁸	1.4 MPa m ^{1/2} ¹⁰⁸	10.6 (n) ⁶² (T _{cold} = 373 K, T _{hot} = 773 K)	1508-1528K ¹⁰⁹	500-900K
SnSe-based	2.8 (n) ⁶⁵ 2.6 (p) ⁶³	$\alpha_{200-800 \text{ K}} = 13$ to 14.9 (n & p) ^{*j} ^{110, 111}	0.67 GPa ⁶⁷	0.62 MPa m ^{1/2} ⁶⁷	--	1120-1140K	>900K

Cu ₂ Se-based	2.7 (p) ⁷⁷	$\alpha_{773-1000\text{ K}} = 107$ ⁷²	0.43 GPa ¹¹²	2 MPa m ^{1/2} ¹¹²	9.1 (p) ¹¹³ (T _{cold} = 300 K, T _{hot} = 973 K)	1376-1396K	>900K
Yb ₁₄ MnSb ₁₁	1.3 (p) ⁷⁹	--	>3 GPa ⁷⁹	--	--	>1200K ¹¹⁴	>900K

*Notes: *) Chemical composition and thermal expansion coefficient data are very similar for both n- and p-type variations. *ii)

For n-type filled CoSb₃-based skutterudites. *iii) For p-type filled FeSb₃-based skutterudites. *iv) For n-type (Ti,Zr,Hf)NiSn-

based Half-Heusler alloys. *v) For p-type Ti(Fe,Co)Sb-based Half-Heusler alloys.

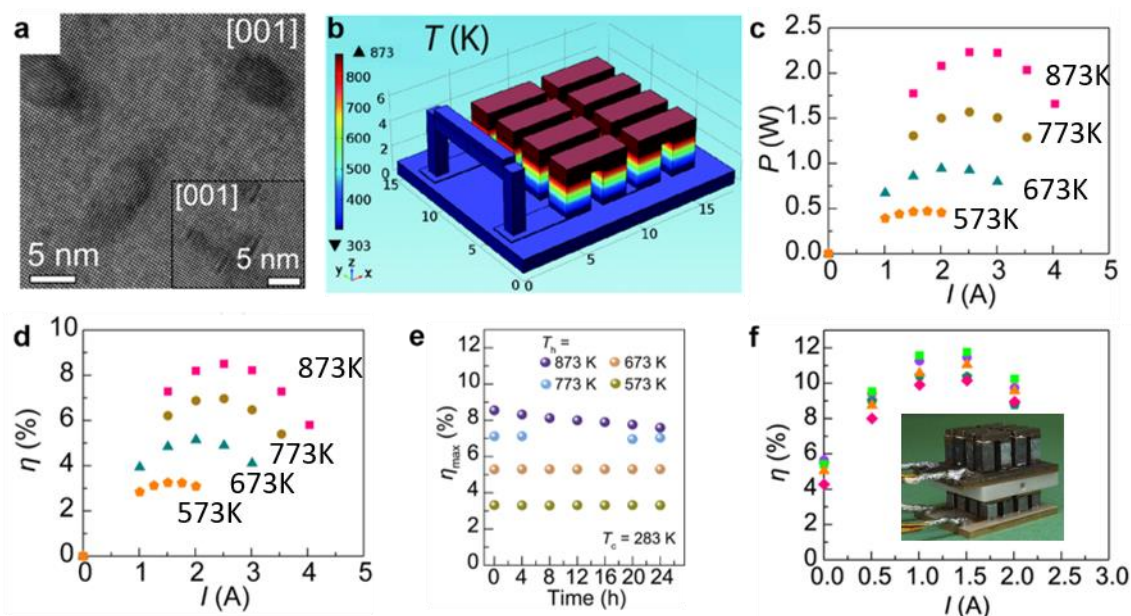


Fig. 1 | The power and conversion efficiency of PbTe based modules. **a**, High-resolution TEM image of $\text{Pb}_{0.953}\text{Na}_{0.040}\text{Ge}_{0.007}\text{Te}$ showing nanoprecipitates and disk-like nanostructures (inset) in the [001] zone axis; **b**, Typical results of numerical simulations for the nanostructured PbTe-based module (PbTe-2% MgTe doped with 4% Na (p-type) and PbTe doped with 0.2% Pbl_2 (n-type)) for hot side at 873 K and cold side at 303 K and load conductivity of $4.5 \times 10^2 \text{ S cm}^{-1}$. Dimensions of the module are in mm; **c**, Electrical power output (P) and **d**, Conversion efficiency (η) of the nanostructured PbTe-based module as function of electrical current (I). The hot-side temperature (T_h) was changed from 873 K to 573 K, while the cold-side temperature (T_c) was maintained at 283 K; **e**, η_{max} as a function of time (hours) for 24-hr testing with $T_h = 873, 773, 673,$ and 573 K and $T_c = 283 \text{ K}$ of Nanostructured PbTe-Based Module; **f**, PCE (η) as function of current (I) of the nanostructured $\text{Pb}_{0.953}\text{Na}_{0.040}\text{Ge}_{0.007}\text{Te}$ module cascaded with a Bi_2Te_3 module (inset). T_h and T_c were at 873 K and 283 K, respectively. The measurements were performed at various currents (2.0–4.0 Amp).^{22, 23} Copyright 2015, The Royal Society of Chemistry & Copyright 2020, Cell Press.

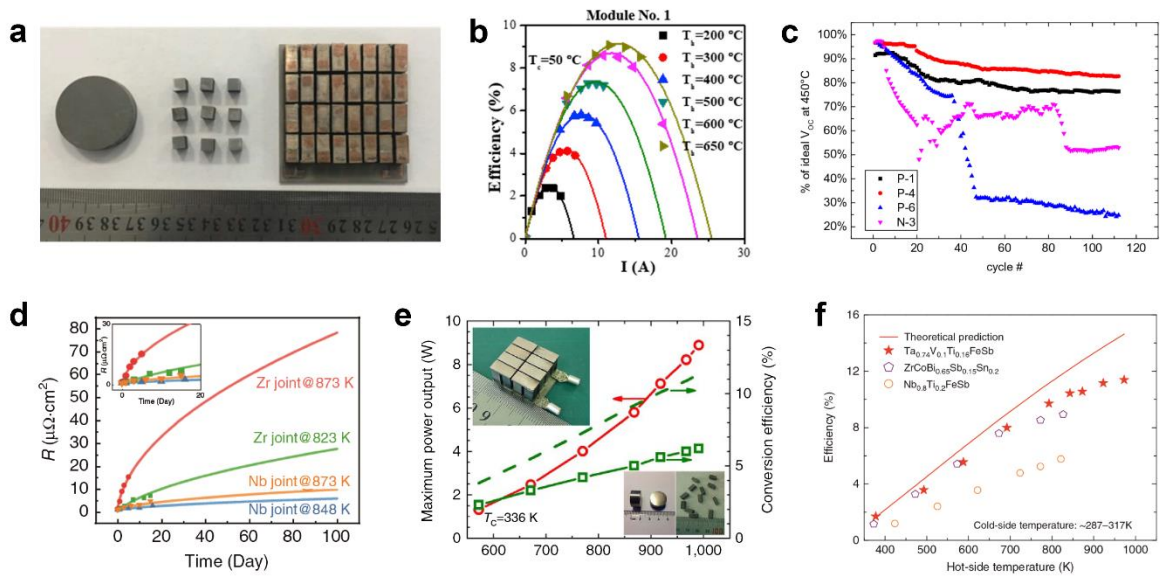


Fig2. | The conversion efficiency and stability of skutterudite based modules. **a**, An 8×8 leg device made from n-type CoSb_3 (filled with Yb, Ca, Al, Ga, $ZT \sim 1.2$) and p-type CoSb_3 (filled with Pr, Ti, Ga, Ba, Fe, $ZT \sim 0.85$). **b**, energy conversion efficiency with different hot side temperatures, T_{hot} . The cold side temperature is kept at 50 °C (323K).⁴⁰ **c**, Change of open circuit voltages V_{oc} of four p-skutterudite legs upon thermal cycling. The hot sides are cycled between 150 °C (423 K) and 500 °C (773 K) and the cold sides are cycled between 25 °C (298 K) and 50 °C (323 K).⁴² **d**, Interfacial resistivity R for skutterudite/Nb and skutterudite/Zr joints after aging at 823 K and 873 K for different days. Dots are experimental data and lines are numerical curve fitting.⁴³ **e**, Maximum power output (P_{max}) and PCE (η) as a function of hot side temperature (T_{H}) for a TE device made from $\text{FeNb}_{0.88}\text{Hf}_{0.12}\text{Sb}$ and ZrNiSn . The dash line represents the theoretical conversion efficiency assuming no electrical and thermal contact resistances.⁴⁷ **f**, Measured hot-side temperature-dependent heat-to-electricity PCE of $\text{Ta}_{0.74}\text{V}_{0.1}\text{Ti}_{0.16}\text{FeSb}$ and $\text{ZrCoBi}_{0.65}\text{Sb}_{0.15}\text{Sn}_{0.2}$.⁴⁹ (add copy right)

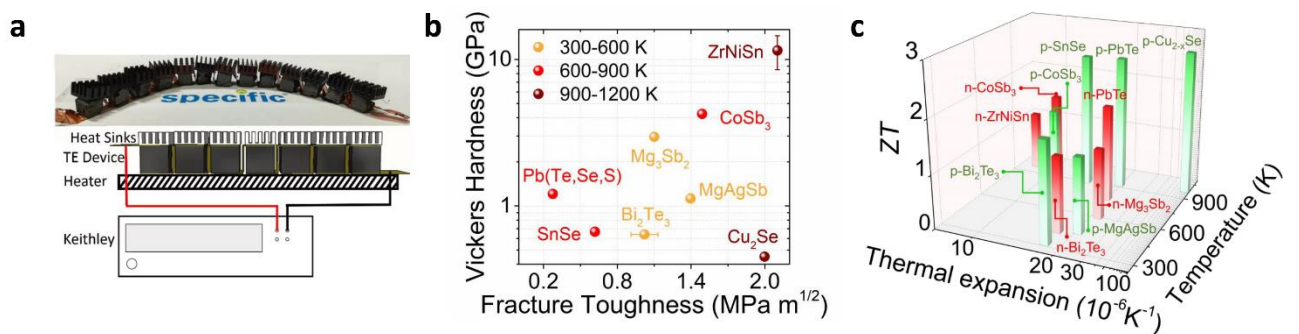


Fig3. | A SnSe based modules and summaries of mechanical and thermal properties of TE materials. **a**, 3D printed SnSe thermoelectric power generator.⁶⁸ **b**, Histogram of peak ZT , Vickers Hardness and Fracture Toughness of bulk polycrystalline ZrNiSn ,^{47, 103, 115} CoSb_3 ,^{94, 95, 99, 100} Bi_2Te_3 ,^{116, 117, 118, 119} SnSe ,^{66, 67} Cu_2Se ,^{77, 112} PbTe ,^{33, 90, 120, 121} Mg_3Sb_2 ,^{106, 108} and MgAgSb .^{100, 122} As shown in the legend, the data bars of each material are colour-coded according to the temperature range of their peak ZT 's. The Vickers Hardness values are plotted using a log scale. The error bar of the Vickers of the ZrNiSn -based Half-Heusler alloys were determined for samples with different doping compositions. **c**, Plot of

thermal expansion coefficient data and peak ZT of bulk polycrystalline CoSb_3 ,^{94, 95, 96, 97, 98} ZrNiSn ,^{103,}
¹¹⁵ Bi_2Te_3 ,^{118, 119, 123, 124} SnSe ,^{66, 110, 111} Cu_2Se ,^{72, 77} PbTe ,^{88, 89, 120, 121} Mg_3Sb_2 ,^{106, 107} and MgAgSb .^{122, 125,}

¹²⁶ As shown in the legend, the data points of each material are colour-coded according to the temperature range of their peak ZTs. The thermal expansion coefficient is plotted using a log scale.

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Box 1

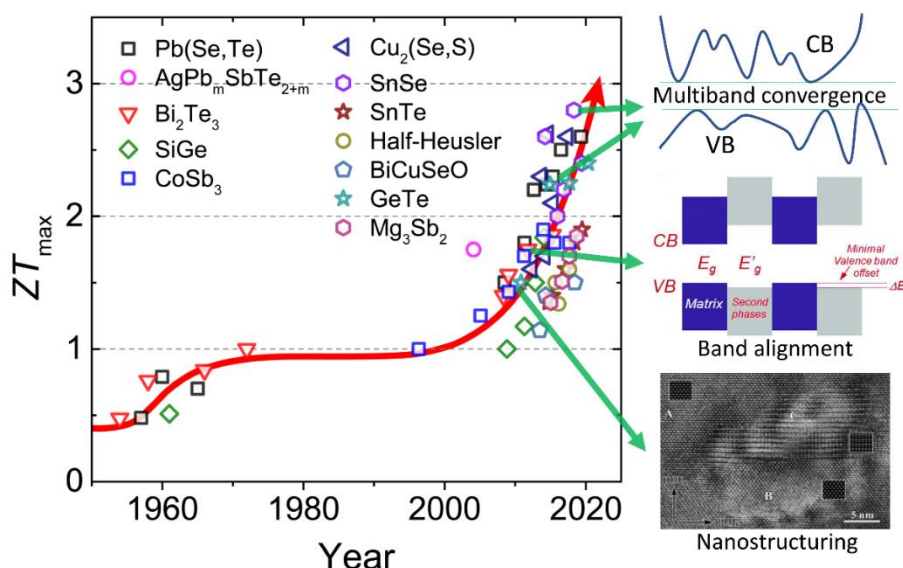


Figure | Decadal timeline and progress in raising the efficiency of thermoelectric materials through successive innovations since around 2000. The red line is drawn as a guide to the eye. On the right side some of the key Innovations in materials design concepts that let these advances are shown schematically.

In-situ inclusion of nanostructures are of great importance in improving TE performance. Nano precipitates of a second phase are caused to grow in the TE material which acts as the host matrix. These dispersed nano-sized objects act as efficient phonon scattering centers, strongly impeding heat flow. During the nucleation and growth, the interface created between the host matrix and the precipitates should be as coherent as possible which is referred to as endotaxy. Electronic band alignment between the two phases is necessary to easily transmit charge carriers especially in an endotaxial interface. This arrangement can effectively scatter phonons and at the same time allow charge carrier to pass through with ease. This strategy requires the creation of special heterogeneous materials. when the heterogeneity scale extends beyond the nano-sized regime (e.g. 5-50 nm) and into what we call the meso scale (50-1000 nm) then additional heat-carrying phonon can be scattered whose mean free paths are comparable to those of the scale. In that case we have an all-scale architecture that can scatter a broad spectrum of phonons. The all-scale architecture is the most effective composite structure for many thermoelectric systems.

Multiband convergence is when the electronic conduction (CB) or valence band (VB) extrema in a given electronic structure of a thermoelectric material occur multiple times and fall within a small energy range. For example when an electronic structure has only one extremum it generally is considered to be inferior from the thermoelectric performance point of view than a corresponding structure that has multiple. The presence of many such band extrema can enable the achievement of very high power factors. When electron or hole pockets are created through doping in each individual band extremum of the CB or VB, each pocket contributes to the power factor in roughly an additive manner (see ref 11 for a more extensive discussion).