

1 **Estimating p - y curves for clays by CPTU method: a framework and empirical**
2 **study**

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31 **Abstract:** Despite its wide use as a tool in foundation design, the CPTU test was rarely
32 recommended to work for design and analysis of laterally loaded piles. Obtaining lateral response
33 of pile foundations is a complicated engineering problem, especially in nonhomogeneous soils.
34 This paper presents a review of the relationship between the piezocone test and the bearing
35 response of laterally loaded piles, and introduces a framework for estimating p - y curves for clays
36 direct using CPTU parameters. In order to validate this method, full-scale lateral load tests of
37 bored piles with corresponding CPTU tests in Jiangsu soil deposits were conducted and data were
38 used for comparison with the predicted results. In addition, case histories were further considered
39 in detail to study the application of the proposed method for different field conditions. It is
40 demonstrated that the results predicted by the proposed CPTU-based p - y curve agree relatively
41 well with the measured results. The proposed method can provide a fast and effective design tool
42 that can be applied to clayey soils with full consideration of soil profiles along the pile embedded
43 depth.

44 **Key words:** Piles; p - y curve; piezocone penetration test (CPTU); clays; load tests; case reports.

45 **Introduction**

46 Pile foundations are often required to be designed against significant lateral loads in addition
47 to vertical loads. These lateral loads can be imposed by wind, earthquake, wave, earth pressure,
48 etc. For the estimation of lateral load capacity of a single pile and the purpose of doing an efficient
49 and safe pile foundation design, the pile-soil interaction characteristics should be evaluated
50 accurately. However, the bearing capacity of laterally loaded piles is mainly controlled by the

51 forms of the lateral soil resistance. The non-linear and elastic-plastic response of surrounding soils
52 as well as the non-homogeneity of soil properties makes the analysis of laterally loaded piles
53 difficult and restricts development of the design methods.

54 In the determination of the bearing capacity of laterally loaded piles, well-known analytical
55 theories and numerical methods have certain shortcomings. Furthermore, full-scale pile load tests
56 are very expensive and time-consuming. Laboratory model tests disturb the soil and centrifuge
57 tests have large energy consumption. All of these are challenging for engineers to effectively
58 select an appropriate method. Therefore, to overcome the shortages of the traditional methods, a
59 practical and fast method should be proposed to evaluate the lateral behavior of pile foundations.

60 Among various foundation design methods, the piezocone penetration test (CPTU) is
61 adopted in soil investigation due to its cost-effectiveness and popularity (Robertson, 2009). For
62 the design of laterally loaded piles, however, less attention and attempt were paid to the CPTU test
63 mainly due to the different loading direction of the vertical cone penetration from the lateral pile
64 loading process (Kim et al. 2014). Because of the simplicity of the beam-on-elastic foundation
65 (BEF) approach (Ashour et al. 2004), the lateral pile-soil interaction behavior is commonly
66 characterized by a series of uncoupled nonlinear springs which are applied along the pile
67 embedded depth. These are known as p - y curves (Randolph et al. 2005; Taghavi and
68 Muraleetharan 2016). Up to date, several formulations have been suggested to predict p - y curves
69 in different soil conditions (Matlock 1970; Reese et al. 1975; Murchison and O'Neill 1984;
70 Franke and Rollins 2013). Moreover, various commercial programs based on p - y analysis have
71 been established to aid **engineers** in lateral load analysis (e.g. *LPILE* (Ensoft 1999), Com624P
72 (Reese and Wang 1993), FloridaPier (FDOT, 1996), ALP program (Oasys 2013). All the programs

73 require inputs of soil parameters at different depths and the adequacy of input profiles is crucially
74 important for the successful implementation of the p - y analysis.

75 This paper aims at describing the feasibility of estimating p - y curves by the CPTU method
76 for analysis of laterally loaded piles in clays. A CPTU-based p - y analysis method is established to
77 calculate the lateral load capacity and evaluate the lateral bearing characteristics of single piles, by
78 building the relationship between Matlock p - y curve parameters and CPTU profiles. In order to
79 **examine** the accuracy of the proposed method, field full-scale lateral pile test results in Jiangsu
80 soil deposits were conducted and used for comparison with the predicted results.

81 **Correlation between cone resistance and lateral pile load capacity**

82 In-situ cone penetration tests (CPTs) having less average cost than traditional soil boring or
83 corresponding laboratory and field tests are widely used in soil investigation, vertical bearing pile
84 design and other geotechnical engineering issues (Puppala et al. 1995; Lunne et al. 1997; Mayne
85 2007; Liu et al. 2011; Cai et al. 2012; Shahin 2013). In recent years, a group of scientists began to
86 focus on the application of CPT technique to the analysis of pile foundations under lateral loads.
87 Some beneficial explorations have been undertaken and several studies are available for
88 describing the potential correlation between cone resistance and pile lateral load capacity (Schnaid
89 and Housby 1991; Anderson et al. 2003; Abu-Farsakh et al. 2003; Lee et al. 2010; Suryasentana
90 and Lehane 2014; Bouafia 2014; Ebrahimian et al. 2015). It has been recognized that the cone
91 resistance can be expressed as a function of the horizontal soil effective stress rather than the
92 vertical soil effective stress, which is similar to the bearing mechanism of laterally loaded piles
93 (Schnaid and Housby 1991; Lee et al. 2010). Moreover, a comprehensive comparison of four test

94 methods (SPT, CPT, DMT, and PMT) conducted by Anderson et al. (2003) also indicated that
95 CPT has a prominent prediction accuracy in evaluating the bearing capacity of laterally loaded
96 piles. A numerical derivation of a CPT-based p - y curve for piles was proposed previously by
97 Suryasentana and Lehane (2014) for sands employing hardening soil (HS) models. However, there
98 is still no theoretical explanation for that the cone resistance is mainly controlled by horizontal
99 soil effective stress.

100 As an advanced technology, the CPTU test generally provides three separate measurement
101 readings including the cone tip resistance q_c , sleeve frictional resistance f_s and penetration
102 pore-water pressures u_2 , and also gives nearly continuous information about the field subsurface
103 stratification. Fig.1 shows physical and schematic diagrams of the international standard CPTU
104 piezocone with a projected area of 1000 mm², an apex angle of 60°, and a sleeve surface area of
105 15000 mm² (Tong et al. 2011).

106 In the process of a CPTU test, along with continuous penetration of the probe (rate of 2 cm/s),
107 plastic damage in soils will be produced near the cone tip. The cone tip resistance consists of two
108 parts, the normal stress σ_n perpendicular to the cone tip side, and the shear stress τ along the cone
109 tip wall (see Fig.1). The shear stress τ defined by Konrad and Roy (1987) is given as follows:

110 (1)
$$\tau = (\sigma_n - u_m)M \tan \phi'$$

111 where ϕ' is the internal soil friction angle, M is the contact surface friction coefficient, and u_m is
112 the pore water pressure in the position of the plastic damage area, which is represented by:

113 (2)
$$u_m = \alpha u_2$$

114 where u_2 is the penetration pore-water pressure at the shoulder position (see Fig.1), and α is the

115 conversion factor, range in $1 \sim 1.1$ (Roy et al. 1982). To obtain the corrected cone resistance for
 116 pore pressure effects, a correction must be applied to account for the design of the cone. The
 117 actual cone resistance q_t is obtained as follows (Campanella et al 1981; Liu et al. 2004):

$$118 \quad (3) \quad q_t = q_c + u_2(1 - a)$$

119 where a is the bearing net area ratio, $a=0.8$.

120 The following expression for a cone with half apex angle θ and diameter d is then obtained
 121 considering the force equilibrium in the failure zone:

$$122 \quad (4) \quad q_t \cdot d = 2(\sigma_n \cdot \frac{d}{2 \sin \theta} \cdot \sin \theta) + 2(\tau \cdot \frac{d}{2 \sin \theta} \cdot \cos \theta)$$

123 From Eq. (1) and Eq. (2), the balance equation above can be simplified as follows:

$$124 \quad (5) \quad q_t = \sigma_n + (\sigma_n - \alpha u_2) M \tan \phi' \cot \theta$$

125 As indicated by Eq. (5) and Fig. 1, the actual total stress q_t is directly related to the normal
 126 stress σ_n . Here, the definition of horizontal soil effective stress σ_h and vertical soil effective stress
 127 σ_v is given, and σ_n can be decomposed by σ_h and σ_v as follows:

$$128 \quad (6) \quad \sigma_n = \sigma_h \cos \theta + \sigma_v \sin \theta$$

129 For standard CPTU cone, the apex angle is immobilized 60° and its half is $\theta=30^\circ$ (see Fig.1).
 130 The contribution ratio of the σ_h and σ_v for the normal stress σ_n can be calculated by the ratio of
 131 $\cos \theta$ and $\sin \theta$, so that the result is obviously $\sigma_h : \sigma_v = 1.73:1$ from a simple but persuasive analysis.
 132 That is to say, the CPTU cone resistance q_t is mainly controlled by the horizontal soil effective
 133 stress σ_h rather than the vertical soil effective stress σ_v , which is consistent with the previous
 134 conclusion (Schnaid and Housby 1991; Lee et al. 2010). For laterally loaded piles, it is well

135 known that the horizontal soil effective stress σ_h affects the level of the pile bearing performance,
136 indicating that estimation of lateral pile capacity using CPTU results is feasible.

137 **Framework for constructing CPTU-based p - y curves**

138 *Matlock (1970) p - y curve*

139 It is generally accepted that the p - y curve has a non-linear shape and is characterized by
140 certain soil parameters. For laterally loaded piles in clays, the p - y curve proposed by Matlock
141 (1970) is widely used and adopted in various specifications (API 2000; DNV 2004; JTS 2012).
142 Fig.2 shows the curve feature of the Matlock p - y model applying in soft clay. Soft clay is widely
143 distributed in China's coastal areas, especially in Jiangsu province (Liu et al. 2008). The function
144 of the Matlock p - y curve in Fig.2 is given in the following normalized form:

$$145 \quad (7) \quad \frac{p(z)}{p_u} = 0.5 \cdot \left[\frac{y(z)}{y_{50}} \right]^{1/3}$$

146 where $p(z)$ is the lateral load per unit length, p_u is the ultimate lateral soil resistance, $y(z)$ is the pile
147 lateral displacement and y_{50} is the critical lateral displacement. As shown in Fig.2, the $p(z)$ value is
148 set as a constant p_u beyond the lateral displacement of $8y_{50}$. Because of fewer parameters and
149 simple form, this p - y relation is widely adopted to the simulation of clays.

150 For the analysis of the ultimate lateral resistance of surrounding soils, p_u complies with the
151 following equation:

$$152 \quad (8) \quad p_u = N_c s_u D$$

153 where s_u is the undrained shear strength, D is the pile diameter and N_c is a bearing capacity factor.
154 According to Matlock (1970), N_c varies from 3 to 9 depending on the depth range given as

155 follows:

$$N_c = 3 + \frac{\gamma' z}{s_u} + \frac{0.5z}{D} \quad (z < z_r)$$
$$N_c = 9 \quad (z \geq z_r)$$

156 (9)

157 where γ' is the effective unit weight of soils, z is the depth from the ground surface and z_r is the
158 limit depth below ground surface which can be estimated using the following relationship
159 (Matlock, 1970):

$$z_r = \frac{6D}{\gamma' \frac{D}{s_u} + 0.5}$$

160 (10)

161 **CPTU parameters for the derivation of Matlock p - y curve**

162 Since current design software such as *LPILE* for estimating the lateral load capacity of piles
163 commonly requires p - y curves, which originated from the Matlock p - y model for clays. This
164 section presents the methodology to obtain the Matlock p - y curves from CPTU parameters. The
165 corresponding comprehensive relationship between piezocone parameters and p - y curve
166 parameters p_u, y_{50} is established, and the CPTU-based p - y analysis method for clays is proposed.

167 ***Ultimate lateral soil resistance p_u***

168 Undrained shear strength s_u for clays as shown in Eq. (8), is one of the important
169 characterization factors for determination of p_u values. An effective way to obtain the p_u is to use
170 CPTU data to obtain the s_u firstly. The cone factor method is a common approach to estimate s_u
171 using the CPTU cone resistance given as the following relationship:

$$s_u = \frac{q_t - \sigma_{v0}}{N_{kt}}$$

172 (11)

173 where N_{kt} is the cone factor, and σ_{v0} is the in situ total vertical stress. This method is simple to
174 apply and accounts for the influence of stress level on soil strengths. As the parameter σ_{v0} cannot
175 be obtained from the piezocone test, the rapidity and efficiency of CPTU technology are reduced.
176 In order to overcome this defect, the effective cone factor method was proposed (Lee et al. 2010),
177 and s_u can be defined by:

$$178 \quad (12) \quad s_u = \frac{q_t - u_2}{N_e} = \frac{q_e}{N_e}$$

179 where q_e is the effective cone resistance, and N_e is the effective cone factor. Noted that no
180 additional testing procedure is required as all parameters in Eq. (12) can be obtained from CPTU
181 results. Substituting Eq. (12) into Eq. (8), the following equation can be obtained after
182 rearranging:

$$183 \quad (13) \quad p_u = \frac{N_c}{N_e} D q_e$$

184 ***Critical lateral displacement y_{50}***

185 For critical lateral displacement y_{50} , according to API (1993), y_{50} is defined as follows:

$$186 \quad (14) \quad y_{50} = 2.5 \varepsilon_{50} D$$

187 where D is the pile diameter and ε_{50} is the limit strain corresponding to 50% of failure stress in
188 unconfined compression tests.

189 However, the parameter ε_{50} is particularly sensitive to the disturbance of soils in a laboratory.
190 The ε_{50} value of remolded soils is different from the one of undisturbed soils. Instead, in-situ tests,
191 such as DMT, PMT, and CPT/CPTU, can achieve minimum disturbance and provide more

192 accurate original soil parameters. Table 1 shows four equations for estimating ε_{50} (%) by
193 Ebrahimian et al. (2015) using CPT data. The Model 3 equation from Table 1 is presented as
194 follows:

$$195 \quad (15) \quad \varepsilon_{50} = 0.86q_c - 0.5$$

196 Obviously, M3 has the highest accuracy with $R^2=0.92$ among the four models. Another
197 advantage is that Eq.(15) can predict ε_{50} more directly requiring only one parameter q_c . Therefore,
198 in this study Eq.(15) is adopted to determine the y_{50} of the Matlock p - y curve through Eq. (14). In
199 order to achieve dimensionless of ε_{50} values, the Eq.(15) is rewritten as the following form.

$$200 \quad (16) \quad \varepsilon_{50} = 0.086 \frac{q_c}{p_a} - 0.5$$

201 In which p_a is the reference pressure, taken to equal atmospheric pressure (0.1MPa). The
202 units for q_c and p_a are in MPa. The Matlock p - y curve can be given from CPTU data combined
203 Eqs.(13) and (16). Specifically, the CPTU-based Matlock p - y curve is defined as:

$$204 \quad (17) \quad p(z) = 0.5 \left(\frac{N_c}{N_e} q_e D \right) \left[\frac{100y(z)}{(0.215q_c / p_a - 1.25)D} \right]^{1/3}$$

205 Thus, it is appropriate to establish a framework for estimating p - y curves by CPTU data for
206 clays. The proposed CPTU-based p - y curve (Eq. (17)) can directly be imported into commercial
207 programs (e.g. *LPILE*), and the aim of fast calculation of lateral load capacity for pile design is
208 achieved. As the horizontal bearing capacity of a pile is mainly controlled by the upper **soil layers**,
209 a CPTU penetration depth of more than $20D$ (D designates pile diameter) in this study is
210 prescribed to satisfy the computational requirement. The different steps of illustrating the
211 application of the CPTU- based p - y analysis method are shown in Fig. 3. This method is quick and

212 efficient.

213 **Verification of the method**

214 **Field test**

215 In this section, field full-scale lateral pile tests with corresponding CPTU tests are conducted
216 and used to validate the proposed CPTU-based p - y model. Selected CPTU test sites are all
217 sensitive Quaternary deposits in Jiangsu Province of eastern China. These Quaternary deposits are
218 located in cities of Jingjiang and Kunshan (Fig. 4), and layered clays are mainly distributed. The
219 test piles in two sites belong to cast-in-place bored piles with slurry wall protection. The basic
220 parameters of the test piles are shown in Table 2. The CPTU test position is close to the center
221 position of the test pile along the opposite side of the loading direction. The distance between the
222 test pile and its adjacent CPTU hole is within 3m. A loading/unloading method is used for
223 conducting lateral pile load tests. The pile-head lateral load is applied in steps of 10% of the
224 ultimate lateral bearing capacity of the test piles. Prior to lateral load tests, a series of strain
225 gauges are first attached to the steel cage and then lowered into drill holes at Jingjiang site. In
226 detail, 30 pairs of strain gauges are distributed on the upper pile at a vertical interval of 1 m, and
227 10 pairs are distributed along the lower half of the pile at a vertical interval of 2 m. Fig. 5 shows a
228 schematic of the lateral pile load test set-up and the field data collection during the test process.

229 The piezocone penetration device used in this test is produced by Vertek-Hogentogler & Co.
230 of USA. The equipment is a versatile piezocone system equipped with advanced digital cone
231 penetrometers fitted with 60 ° tapered and 10 cm² tip area cones, which can provide the
232 measurement of cone tip resistance q_t , sleeve friction f_s , and penetration pore-water pressure u_2 .

233 All the CPTU tests are conducted in accordance with international standards (ISSMFE 1989;
234 ASTM D5778 2012) after the construction of piles. The groundwater table (GWT) at the test
235 locations is documented immediately after the CPTU tests. The layer numbers and representative
236 profiles of the CPTU soundings in two test sites are presented in Fig. 6. Required parameters (e.g.,
237 q_t , u_2 , q_e) of the CPTU-based p - y curve (Eq. (17)) can be obtained directly from the piezocone
238 penetration profiles. In Fig. 6, the u_0 line represents the hydrostatic pressure line.

239 **Presentation and discussion of results**

240 The bending moments of testing piles at every loading step are calculated by **strain gauges**,
241 from which the soil reaction per unit length can be obtained (Kim et al. 2004). In this study, the
242 measured bending moment is fitted as a seventh order polynomial function of z by the
243 least-squares fitting method. By double differentiation and integration of the bending moments,
244 the p - y curves at different depths are obtained (Zhu et al. 2012). The representative p - y curves of
245 silty clay (layer No. ①) and soft clay (layer No. ②) derived from Eq. (17) at Jingjiang site in
246 comparison with those of lateral pile load tests are depicted in Fig. 7. The soil resistance values of
247 soft clay play out using half of the coordinate value ($p/2$) in the figure. It can be concluded that the
248 predicted p - y curves from the proposed method agree well with that obtained from full-scale
249 lateral load tests of instrumented piles. In addition, the lateral soil resistance values for silty clay
250 show a reasonable increase from $1D$ to $4D$ (D means pile diameter) and are larger than that of soft
251 clay.

252 The accuracy of the predicted allowable pile capacity (H_a) is checked by using Eq. (17)
253 directly in *LPILE* program and then comparing the predicted results with that measured from

254 lateral load pile tests. For the determination of H_a , the load-deflection criterion given by JGJ
255 94-2008, *Chinese technical code for testing pile foundations* is adopted. A representative
256 $H-\Delta Y/\Delta H$ curve for Jingjiang load test is shown in Fig. 8, where ΔY represents the horizontal
257 displacement gradient of the pile head, and the value corresponding to the end of the first line is
258 the allowable lateral pile capacity. Fig. 9 presents the H_a values obtained from the proposed
259 method and the lateral load tests at Jingjiang and Kunshan sites. It can be concluded that the
260 predicted and measured results are generally consistent considering the data scatter. The upper and
261 lower bound lines in Fig. 9 show the boundaries of a zone, characterized by certain ratios of
262 predicted values to measured values of H_a . The proposed CPTU-based p - y method in this study
263 has a great advantage in predicting the horizontal bearing capacity of pile foundations with a
264 (0.85-1.14) ratio boundary. The proposed method can give virtually the same H_a values as those
265 from full-scale lateral pile load tests.

266 **Application: Case history evaluation of lateral load pile responses**

267 In order to further highlight and broaden the applicability of the proposed CPTU-based p - y
268 method, the case study of lateral responses of bored piles using this method is performed. The two
269 case histories are as follows.

270 1. Test piles in Yangtze River clay deposit at Jingjiang, Taizhou, China.

271 2. Test piles in Taihu Lake clay deposit at Wujiang, Suzhou, China.

272 The distribution and geologic formation of these two sites are shown in Fig. 4. Two bored
273 piles called T1 and T2 in each site are installed and tested. A series of CPTU tests are performed
274 nearby the position of test piles after the construction of piles and stress stability of surrounding

275 soils. In order to evaluate the proposed method, the p - y curves are derived at depth intervals of
276 $D/2$ for every site from the CPTU profiles. Thereafter, the scale effect of laterally loaded piles (for
277 Case 1) and the lateral pile response to the thickness variations of a very soft clay interlayer (for
278 Case 2) are analyzed particularly.

279 **Case 1: Test piles at Jingjiang**

280 This case history involves large diameter and super-long bored piles with a diameter and
281 length equal to 1.0m and 68m, respectively. The flexural rigidity of the pile body is EI
282 $=0.16 \times 10^7 \text{kN} \cdot \text{m}^2$. The soil profiles at the test site show a composite soil layer condition with silty
283 clay, soft clay, and some sand layers. CPTU tests adjacent to the test pile are conducted with a
284 penetration depth reaching 33 m ($33D$). The typical profiles of q_t , u_2 and q_c with depth are
285 presented in Fig. 6(a). Through inputting the p - y curves from Eq.(17) into *LPILE* program, a
286 numerical model of the large diameter and super-long pile is established. The model's sketch and
287 soil distribution are shown in Fig. 10, where the upper 33m clay layers adopt the CPTU-based p - y
288 curves, while the underneath sand layers adopt build-in Reese's p - y curves of *LPILE* program.

289 Fig.11 shows the comparison of the measured and predicted lateral loaded-deflection (H - Y)
290 curves and the bending moment (M) curves under $H_a=172$ kN of test piles (T1 and T2). The
291 determination of H_a still adopts the method given by JGJ 94-2008, *Chinese technical code for*
292 *testing pile foundations*. As shown in Fig. 11, the predicted results using CPTU-based p - y method
293 are in close agreement with the field measured results. The maximum bending moment of the pile
294 in this study occurs at $(3 \sim 5) D$ depth below ground level. Owing to the accuracy of the
295 CPTU-based p - y model in the *LPILE* program, the horizontal bearing response of the pile against

296 different pile diameters are further analyzed. Fig. 12 presents the calculated results of the piles
297 with different diameters of $0.6D$, $0.8D$, $1.0D$, $1.2D$, $1.5D$, $2.0D$. It can be seen that the pile
298 diameter has a significant impact on the bearing capacity of laterally loaded piles. The allowable
299 bearing capacity increases with the increase of pile diameter. Taking the lateral load
300 corresponding to 6 mm displacement as the design value of lateral pile capacities (JGJ 94-2008,
301 *Chinese technical code for testing pile foundations*), the design value of $2.0D$ pile is 320kN, three
302 times as much as that of $0.6 D$ pile. Additionally, the scale effect can change the stress distribution
303 of deep pile bodies. With the increase of pile diameter, the bending moment grows, but the depth
304 of maximum and zero bending moment positions reduce. These result in the increase of the
305 horizontal bearing capacity of pile foundations.

306 **Case 2: Test piles at Wujiang**

307 This case history involves the lateral pile response to the thickness variations of a very soft
308 clay interlayer in Taihu Lake site. The diameter, length and flexural rigidity of the bored pile are
309 0.7m, 55m, and $EI = 4.03 \times 10^5 \text{kN} \cdot \text{m}^2$, respectively. The previous survey determines that a soft clay
310 interlayer with a thickness between (0.50 ~ 6.00) m is widely distributed **overlying** a clay layer.
311 In-situ CPTU results based on Liu's China-soil classification chart (Liu et al. 2013), presented in
312 Fig. 13, also show the existence of the very soft clay in the test field. A representative profile of
313 piezocone penetration is shown in Fig. 14. For analysis of piles in Wujiang site, the predictive
314 capability of the proposed p - y method is demonstrated beforehand by comparing predicted
315 load-deflection curves and bending moment curves to the measured. As indicated by Fig. 15, the
316 feasibility of the proposed p - y method is proven. Hence, the further analysis of lateral pile
317 responses to the thickness variations of the soft clay interlayer can be conducted decisively.

318 Fig. 16 shows the comparison of the bending moment and the displacement for various soft
319 clay interlayer thicknesses (h) under a given horizontal force $H_a=150\text{kN}$. Five thicknesses in this
320 study are set: $h=0.5\text{m}$, 2.0m , 3.0m , 4.5m , 6.0m . For the bending moment distribution, although
321 there is no change in the curve shape, the locations of maximum and zero bending moment
322 positions move down, and the maximum bending moment values increase with the increase of
323 interlayer thickness. The location and magnitude of the maximum bending moment, in this case,
324 moves down by 85% and increases by 100%, respectively. The pile head displacement for $h=6.0\text{m}$
325 is nearly four times larger than that for $h=0.5\text{m}$ in this case. It can be concluded that the soft clay
326 interlayer has a significant effect on the lateral bearing capacity of the piles. In addition, the
327 increase rates of the maximum bending moment (M_{\max}) and the pile head displacement (Y) are
328 both reduced with the increase of interlayer thickness, and the $M_{\max}-h$ and $Y-h$ curves flatten out
329 after $h=4.5\text{m}$ shown in Fig. 16. Those mean that the very soft clay interlayer within the scope of
330 4.5 m thickness is a key object for the lateral pile bearing capacity. If it exceeds 4.5m, the
331 interlayer effect can be ignored, which can simplify the soil investigation for the pile design in the
332 Taihu Lake area.

333 **Conclusions**

334 Obtaining the lateral response of pile foundations is a complicated engineering problem.
335 Efforts have been made in this study to estimate $p-y$ curves for clays by CPTU method. Case
336 examples of lateral pile projects in Jiangsu soil deposits are executed to validate the proposed
337 method. Based on the results, the following conclusions can be drawn:

338 (1) A CPTU-based $p-y$ analysis method for estimating the lateral response of pile foundations is

339 proposed based on the relationship between CPTU profiles and Matlock p - y curve parameters.

340 The proposed p - y model is convenient for the design of pile foundations, completely relying
341 upon in-situ soil parameters.

342 (2) The predicted p - y curves direct from CPTU results agree well with that obtained from the
343 full-scale lateral pile tests in this study. The allowable lateral capacity of the test bored piles
344 obtained from the proposed method is consistent with that from field tests in Jiangsu soil
345 deposits.

346 (3) Two cases are examined to broaden the applicability of the proposed CPTU-based p - y method
347 for predicting the lateral pile responses in different clay sites. The scale effect of large
348 diameter piles and the lateral pile response to thickness variations of the soft clay interlayer
349 are examined.

350 (4) The CPTU-based p - y model is an efficient and rapid method for determining the bearing
351 characteristics of laterally loaded piles in clays and can be used as an alternative to
352 conventional methods. Further research with different soils and pile types (e.g. driven piles)
353 should be carried out to improve the applicability of the model.

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List of Tables

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478 **Table 2** Characteristics of investigated piles

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482 **Table 1** Models to determine ε_{50} (Ebrahimian et al. 2015)

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Model	Equation	Parameter	$R^2(\%)$
M1	$\varepsilon_{50} = 16.3s_u - 0.7$	s_u	74.9
M2	$\varepsilon_{50} = 5s_u OCR - s_u - 0.01OCR - 0.5$	s_u, OCR	81.4
M3	$\varepsilon_{50} = 0.86q_c - 0.5$	q_c	91.7
M4	$\varepsilon_{50} = 0.85q_{net} + 0.1$	q_{net}	85.8

484 Note: Net cone tip resistance $q_{net} = q_{c+} u_2 (1-\alpha) - \sigma_{vo}$; R^2 is the correlation coefficient, and the higher the value is,
485 the greater the precision.

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Table 2 Characteristics of investigated piles

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Test site	Pile type	Length /m	Diameter /mm	Allowable horizontal bearing capacity /kN
Jingjiang	Bored pile	68	1000	172
Kunshan	Bored pile	47	700	135

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519 bending movements; (b) lateral pile deflections; (c) maximum bending moments; (d) pile head
520 displacements

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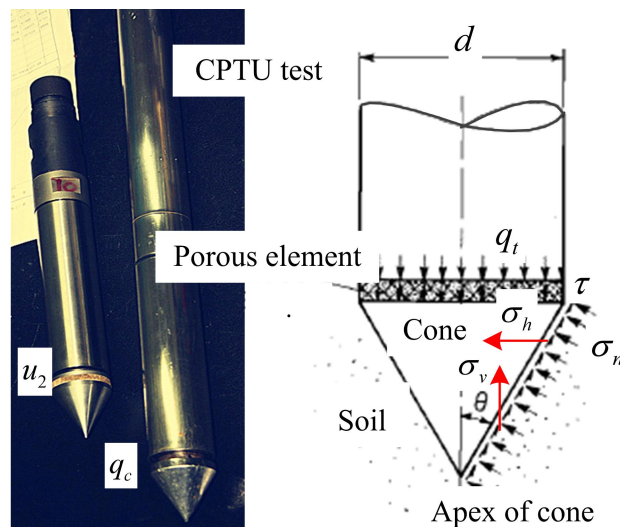
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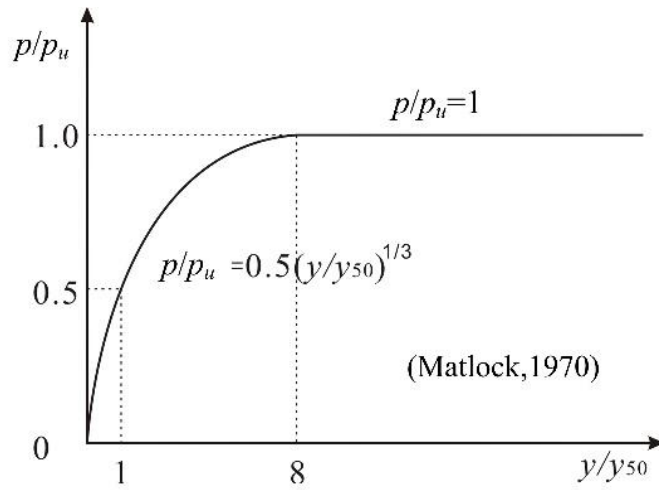
Fig. 1 Physical and schematic diagrams of a piezocone penetrometer

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Fig. 2 Schematic shape of Matlock (1970) p - y curve

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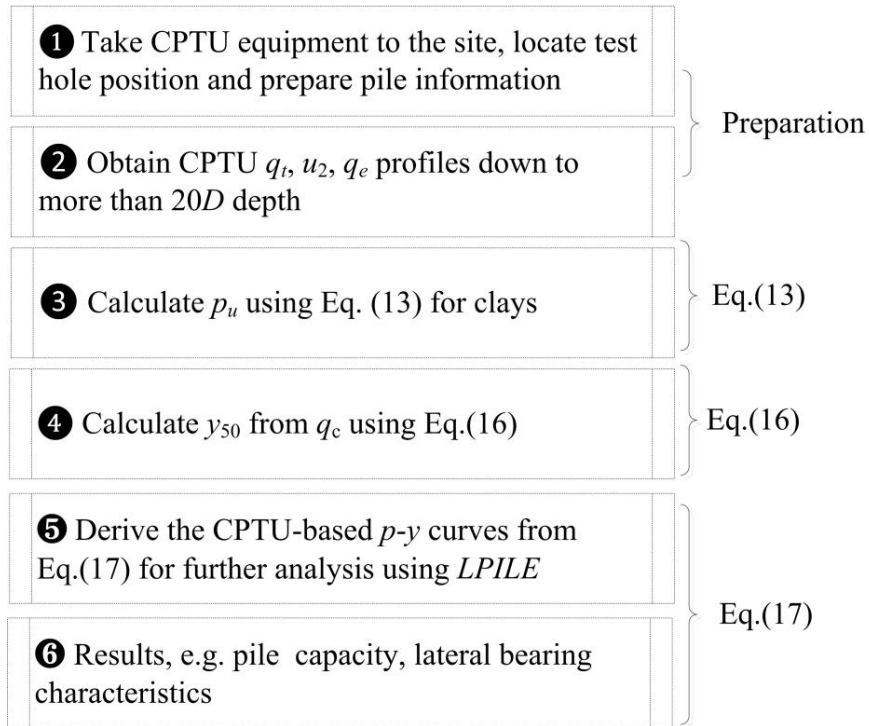
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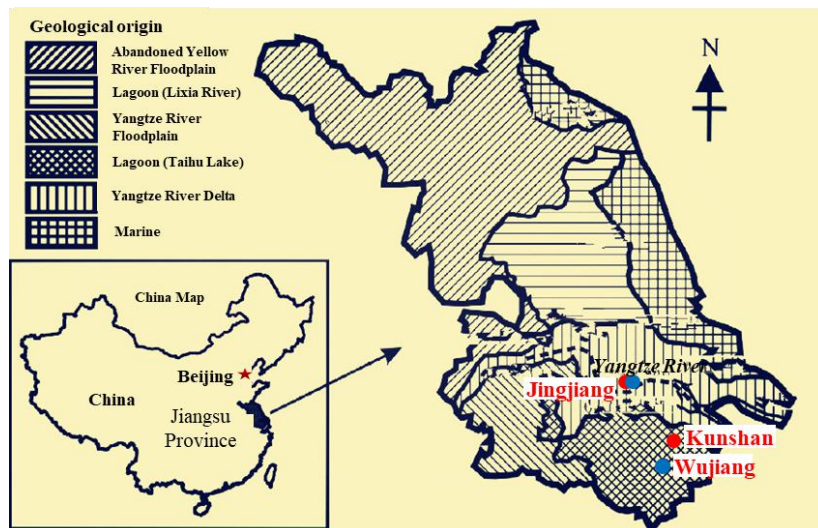
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Fig. 3 Step-by-step application of the CPTU-based $p-y$ analysis method

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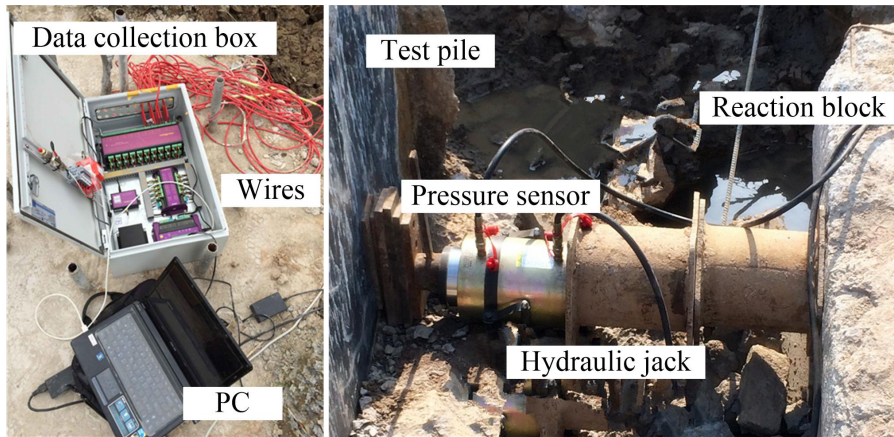
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Fig. 4 Distribution and geologic formation of the testing sites

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Fig. 5 Photos of lateral pile load test set-up and field data collection

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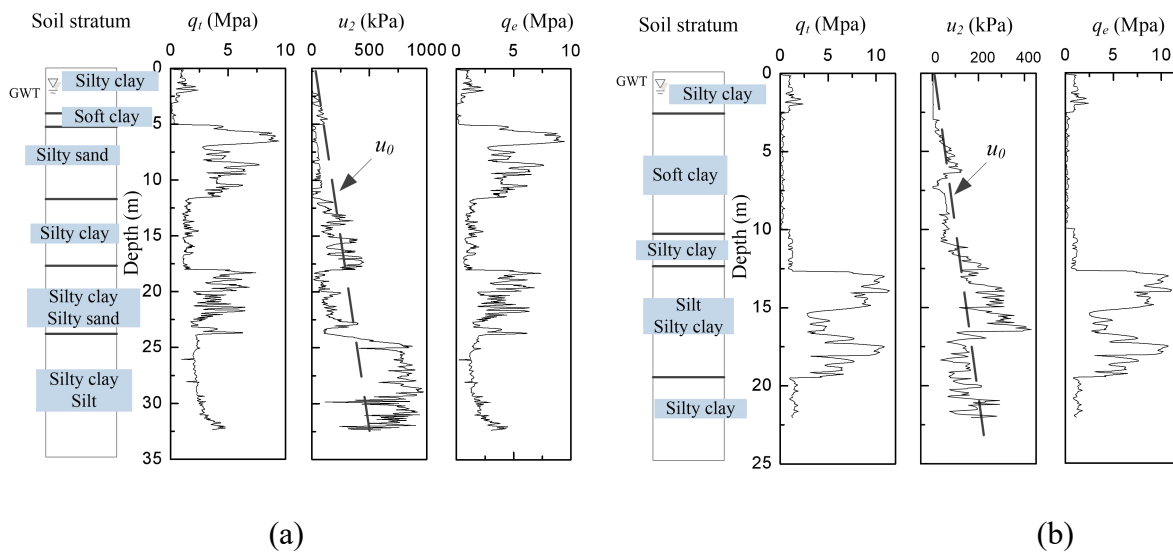
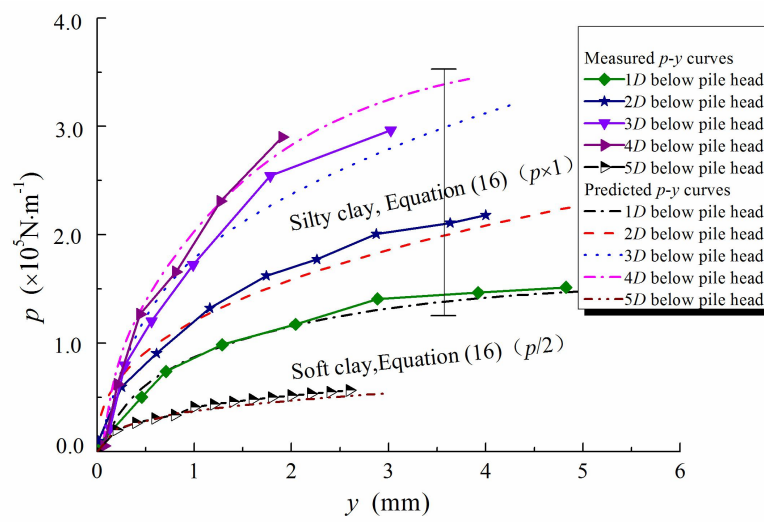


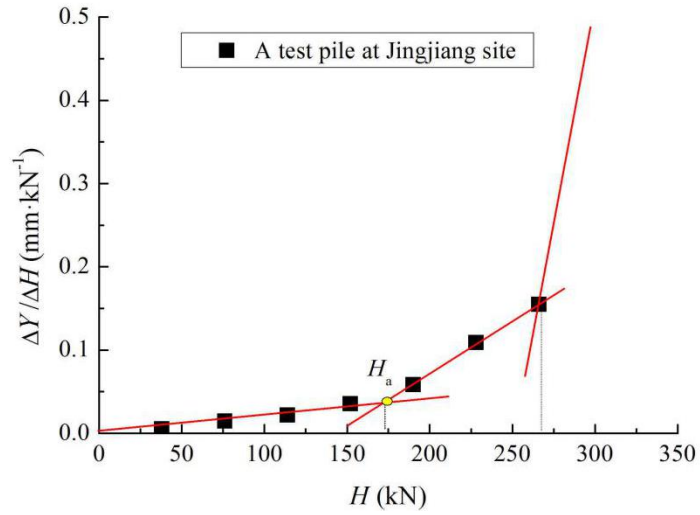
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Fig. 7 Comparison of predicted (from CPTU data) and measured (from moments in pile section) p - y curves at Jingjiang site



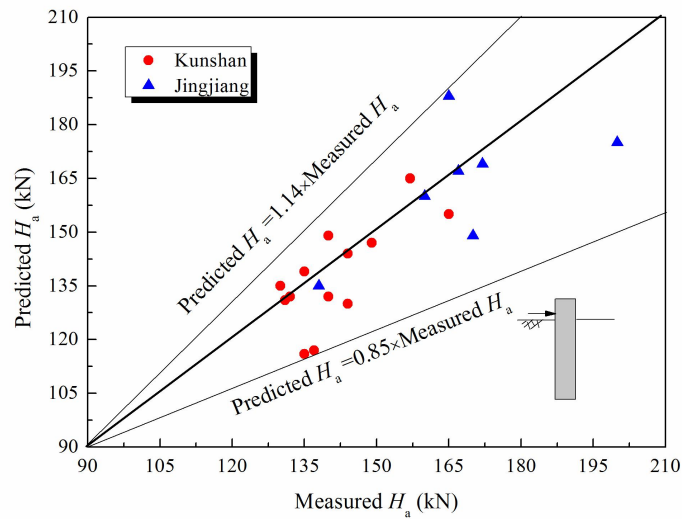
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Fig. 8 Determination of H_a value from the H - $\Delta Y/\Delta H$ curve

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Fig. 9 Comparison of predicted and measured H_a values for test piles at Kunshan and Jingjiang sites

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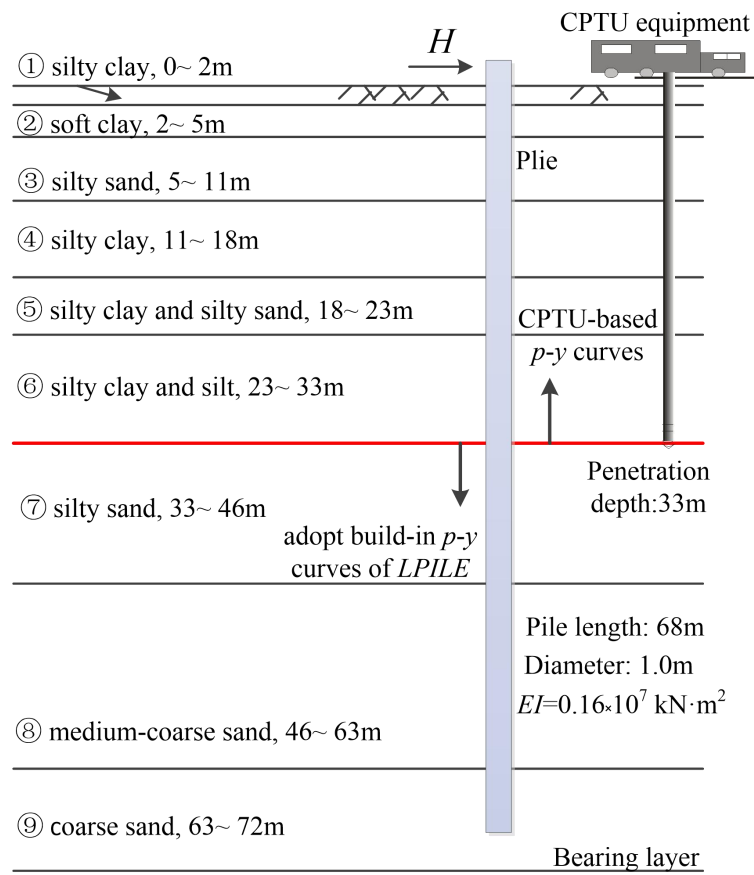
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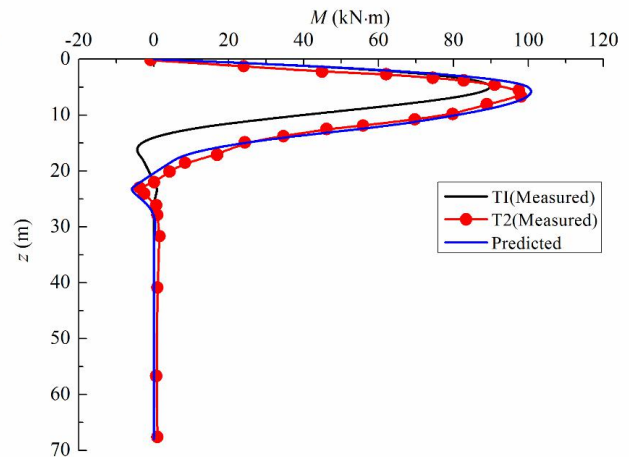
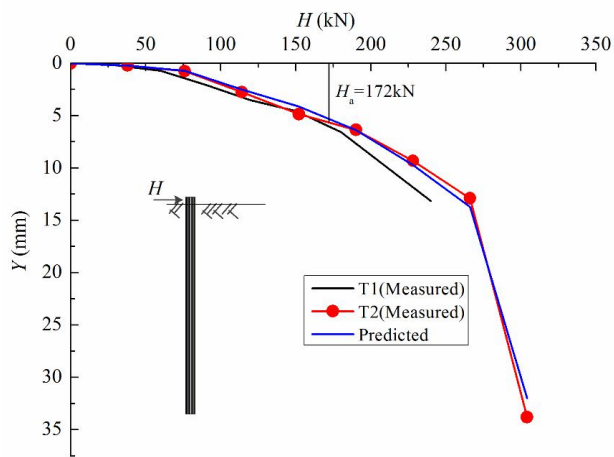
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Fig. 10 Schematic of the *LPILE* numerical model based on the proposed p - y curves

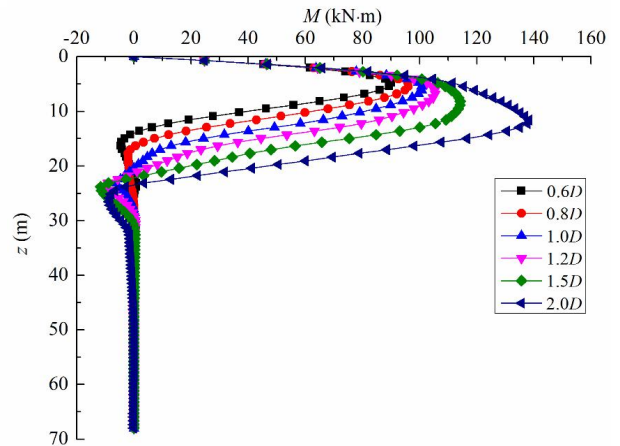
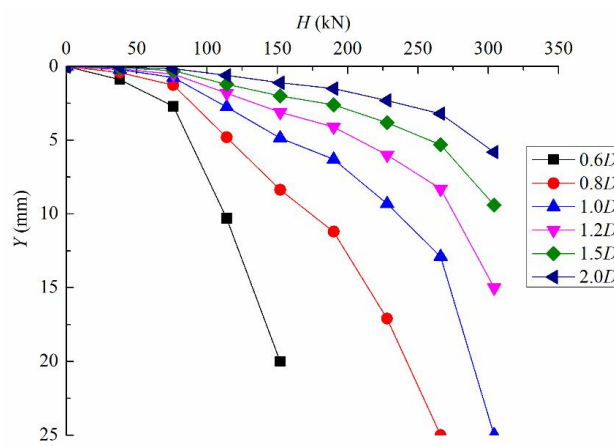
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623 **Fig. 11** Comparison of measured and predicted (a) pile head deflections and (b) bending moments
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631 **Fig. 12** Responses for various diameter piles: (a) lateral loaded-deflection curves; (b) bending
632 moment curves under $H_a=172\text{kN}$

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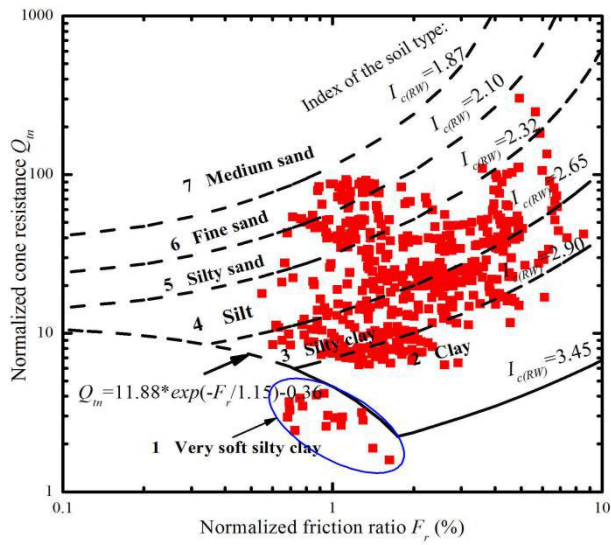
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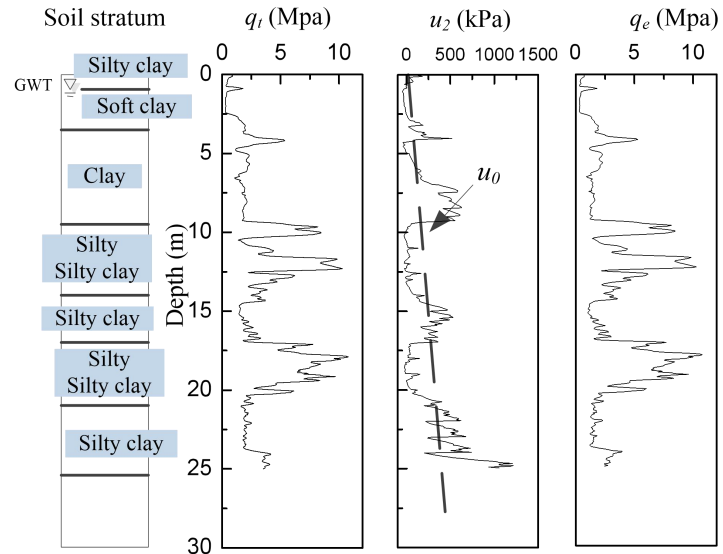
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643 **Fig. 13** Soil behavior type classification chart from CPTU data based on Liu's method at Wujiang
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650 **Fig. 14** Representative profiles of piezocone penetration test at Wujiang site

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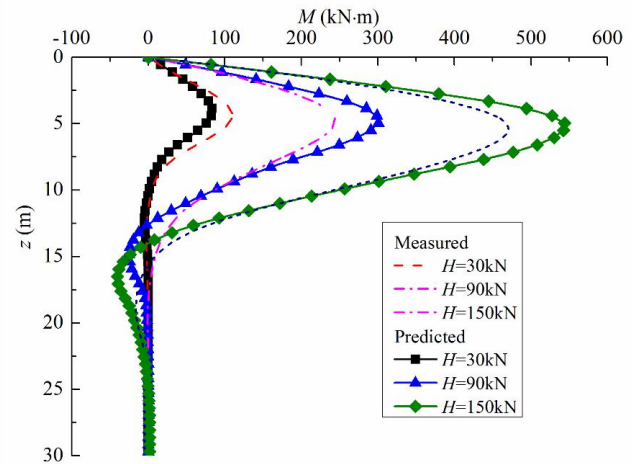
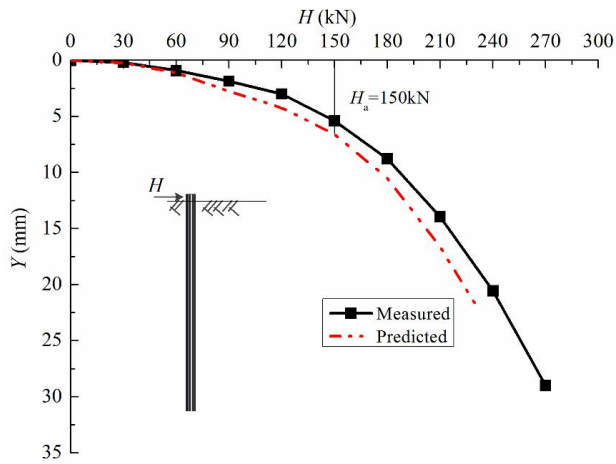
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Fig. 15 Comparison of numerical predictions with field measurements: (a) lateral loaded-deflection curves; (b) bending moment curves.

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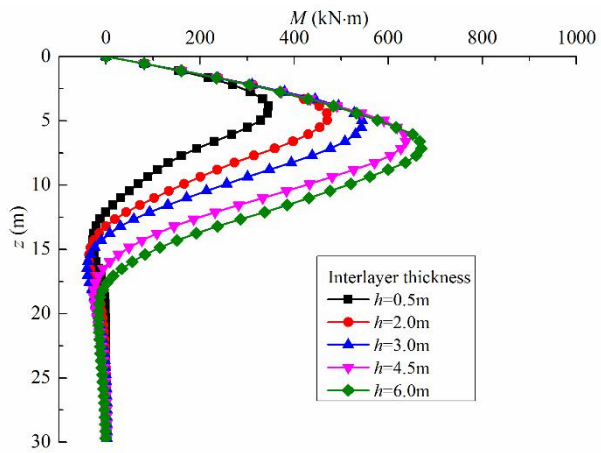
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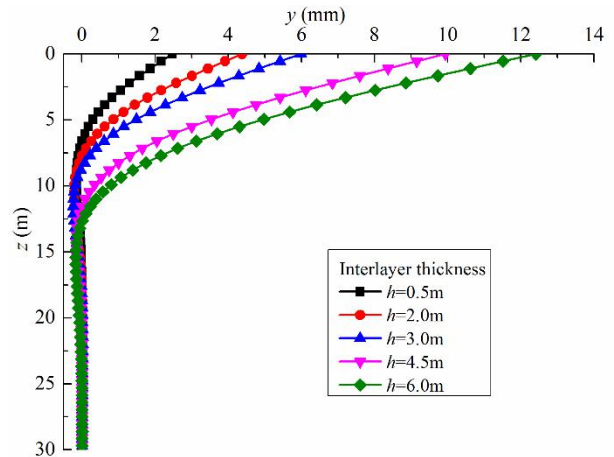
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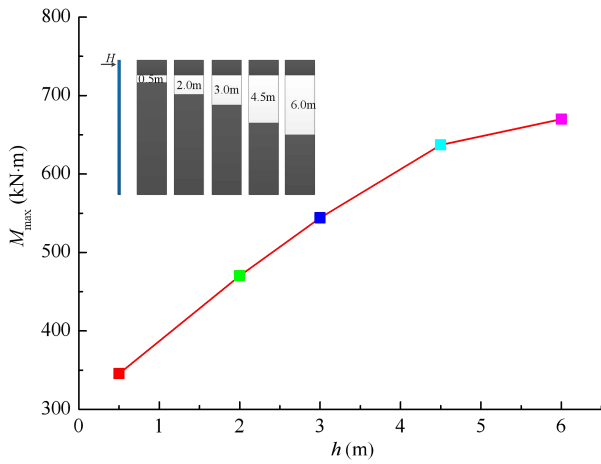
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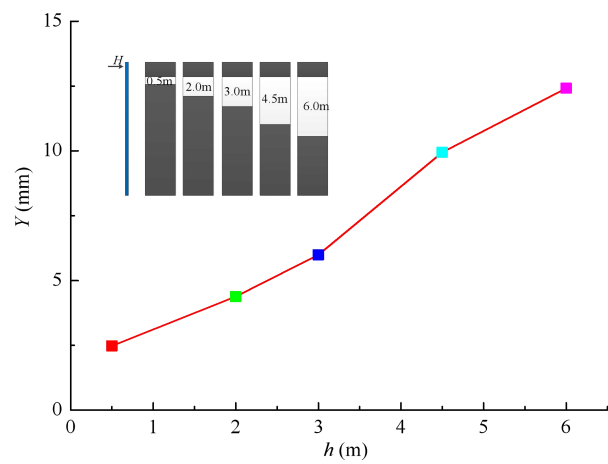
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693 **Fig. 16** Responses of piles subjected to $H_a=150\text{kN}$ for various soft clay interlayer thicknesses: (a)
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