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The Cost of Imperfect Knowledge: How Epistemic Uncertainties Influence Flood Hazard Assessments

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Key Points:

- Flood hazard assessments involve sophisticated probability and physics-based models that require the specification of many parameters
- We propose a Bayesian methodology to include uncertainty in models parameters into flood hazard estimates and mapping
- The inclusion of uncertainty in parameters can significantly affect hazard estimates and its omission can lead to non-conservative planning

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Abstract Classical approaches to flood hazard are obtained by the concatenation of a recurrence model for the events (i.e., an extreme river discharge) and an inundation model that propagates the discharge into a flood extent. The classical approach, however, uses “best-fit” models that do not include uncertainty from incomplete knowledge or limited data availability. The inclusion of these, so called epistemic uncertainties, can significantly impact flood hazard estimates and the corresponding decision-making process. We propose a simulation approach to robustly account for uncertainty in model’s parameters, while developing a useful probabilistic output of flood hazard for further risk assessments via the Bayesian predictive posterior distribution of water depths. A Peaks-Over-Threshold Bayesian analysis is performed for future events simulation, and a pseudo-likelihood probabilistic approach for the calibration of the inundation model is used to compute uncertain water depths. The annual probability averaged over all possible models’ parameters is used to develop hazard maps that account for epistemic uncertainties. Results are compared to traditional hazard maps, showing that not including epistemic uncertainties can underestimate the hazard and lead to non-conservative designs, and that this trend increases with return period. Results also show that the influence of the uncertainty in the future occurrence of discharge events is predominant over the inundation simulator uncertainties for the case study.

Plain Language Summary Estimating the annual probability of some flood-depth level is a key input for risk analysis and engineering design. This is typically calculated via sophisticated probability and physics-based models that require many parameters. However, the classical approach uses a fixed set of “best parameters” for this and do not include the degree of uncertainty, even when such uncertainties may be very high. This work proposes a method to estimate the annual probability of flood-depth including the uncertainty in the parameters used to compute it. More importantly, it shows that not including this uncertainty might severely underestimate the hazard and consequently lead to unsafe designs.

1. Introduction

Flooding appears as the most frequent and one of the costliest natural hazards worldwide, with millions of people affected every year and billions of dollars in insured and uninsured losses. In the last 20 years, floods have caused more than 640 billion US\$ in economic losses (22% of the total among all natural hazards) and affected more than 1.6 billion people, representing the 22% and 41% among all natural hazards respectively (UNDRR, 2019). These values have seen a steady increase over the last decades, mainly due to the increment of exposed people and assets in flood-prone areas (Ahmadalipour & Moradkhani, 2019; Alfieri et al., 2016; Jongman et al., 2012), but also as an effect of human intervention on the environment such as deforestation or land development (Houknpè et al., 2019; Szwagrzyk et al., 2018), and anthropogenic climate change that results in an increased frequency of flood drivers such as intense rainfall (Davenport et al., 2021) and sea-level rise (Taherkhani et al., 2020). Unless efforts are improved toward reducing risk and mitigating the impact of flooding, this trend is expected to continue in the future as recognized in the Sendai Framework for Disaster Risk Reduction developed by the United Nations in 2015 (UNDRR, 2015).

As a key component of a comprehensive risk analysis, a hazard model is required to characterize the future occurrence of potentially damaging events (Grünthal et al., 2006; Smith, 2013). This “potential” for damage is numerically quantified through an intensity measure (IM) that should have a good correlation with the damages (direct or indirect, tangible or intangible) under analysis (Grünthal et al., 2006; Kameshwar & Padgett, 2014; Wang et al., 2021). In the specific case of flooding, water depth has been, and still is, the most used IM to characterize

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its damaging potential (Galasso et al., 2021; Nofal & Van De Lindt, 2022; Scawthorn et al., 2006). In recent years, however, other intensity metrics such as flood duration and flow velocity (or any combination of those), has been used to estimate flood-related damage (Ahmadalipour & Moradkhani, 2019; Mohanty et al., 2020; Nofal & Van De Lindt, 2022; Pregnolato et al., 2015).

In practice, flood hazard is typically defined as the probability of exceedance of an IM level at any point of interest during a given period of time (Galasso et al., 2021; Nofal & Van De Lindt, 2022). This is usually presented in the form of “hazard curves” that relate IM levels with an annual exceedance probability (AEP) or a mean time of recurrence, also known as return period (RP). To get a grasp of the spatial distribution of hazard, the outcome is best conveyed through flood maps for different RPs (Kalyanapu et al., 2012; Nofal & Van De Lindt, 2022; Romanowicz & Kiczko, 2016).

Since observations of IMs (e.g., inland water depths during flood events) usually scarce for most locations, a purely statistical description of their probability distribution is not possible (Dasgupta et al., 2020; Jafarzadegan et al., 2023; Papaioannou et al., 2017). The alternative is to compute IMs as a function of forcing variables for which historical data are available, such as precipitation (Sun et al., 2018), river discharge (Pavelsky et al., 2014) or sea-level rise (Marcos et al., 2019). As a result, IMs occurrence can be computed from the concatenation of two distinct models: a “recurrence model” that describes the probability of occurrence of extreme forcing events; and a “source-to-site propagation model” (or just propagation model for brevity) that represents how the triggering event is translated into a spatial (and temporal) distribution of IM levels (i.e., spatially distributed flood extent and depth). The former is inherently probabilistic and typically modeled via standard stochastic time process such as the Poisson process or independent annual maxima process (Bousquet & Bernardara, 2021; Fawcett & Green, 2018). The propagation model, on the other hand, is typically modeled through deterministic physics-based models such as a hydrologic and/or a hydraulic inundation model (Jafarzadegan et al., 2023).

The “classical method,” as it will be referred in this work, involves computing the event’s magnitude, such as peak discharge in riverine flooding, for different RPs and use it as input of the inundation model to develop flood maps for the different recurrences. This is done using appropriately calibrated recurrence curves and inundation simulators based on available data and expert’s knowledge (Nofal & Van De Lindt, 2022). This is the standard approach for most practical applications in the industry, due to its conceptual simplicity and ease of implementation. It does, however, assume that the models used are perfectly “true.” The only probabilistic nature of the approach comes from the inherent uncertainty in the future occurrence of extreme events; also termed “aleatory uncertainty” (J. Hall & Solomatine, 2008).

A broad range of researchers during the last decades have brought attention to the importance of including other, more subjective, sources of uncertainty into risk analysis in general, and flood hazard modeling in particular (Beven, 2014; Di Baldassarre et al., 2010; J. Hall & Solomatine, 2008; Merz & Thielen, 2005). Subjective uncertainties, also termed here “epistemic,” can arise from the data we use to constrain our models, our lack of knowledge regarding the true physical processes involved, or our limited analytic and computational capabilities for providing results (J. Hall & Solomatine, 2008). Their inclusion may lead to impactful modifications in the decision making process, at the cost of a significant increment in analytical and computational complexity (Di Baldassarre et al., 2010; Merz & Thielen, 2005).

Many researchers have dealt with the inclusion of epistemic uncertainties in flood hazard models, specifically riverine floods, in the last decades. Some works have focused mainly on dealing with uncertain representations on the recurrence of the input discharge events. That is, defining a distribution for the uncertain discharge for a given return period. This includes accounting for statistical fitting errors due to limited-length data and distribution family (Apel et al., 2008; G. T. Aronica et al., 2012; Neal et al., 2013; Romanowicz & Kiczko, 2016; Stephens & Bledsoe, 2020; Winter et al., 2018), additional forcing variables such as flood volume (Candela & Aronica, 2017) or sea-level rise (Muñoz et al., 2022), or more general hydrograph shape uncertainties through hydrological modeling (Ahmadisharaf et al., 2018; Falter et al., 2015; Grimaldi et al., 2013; Meresa et al., 2021; Zahmatkesh et al., 2021). Others have focused on including uncertainty in the inundation model through its most sensitive parameters such as roughness coefficients (G. T. Aronica et al., 2012; Bharath & Elshorbagy, 2018; Di Baldassarre et al., 2010; Kalyanapu et al., 2012; Kiczko et al., 2013; Romanowicz & Kiczko, 2016), Digital Elevation Maps (DEM) (Apel et al., 2008), or cross-section geometrical properties (Stephens & Bledsoe, 2020). Furthermore, many of these have included both the epistemic uncertainties in the discharges recurrence as well as in the inundation model (Apel et al., 2008; G. T. Aronica et al., 2012; Bharath & Elshorbagy, 2018;

Di Baldassarre et al., 2010; Kalyanapu et al., 2012; Kiczko et al., 2013; Romanowicz & Kiczko, 2016; Stephens & Bledsoe, 2020; Zahmatkesh et al., 2021).

The typical outcome from most of these approaches is in the form of “probability of flood” maps for different return periods. That is, for a specific return period, different forcing events and/or inundation model parameters are randomly sampled and used to obtain an ensemble of flood maps from which the probability of flooding is computed empirically (Bharath & Elshorbagy, 2018; Di Baldassarre et al., 2010; Domeneghetti et al., 2013; Kiczko et al., 2013; Neal et al., 2013; Stephens & Bledsoe, 2020; Zahmatkesh et al., 2021). However, a flood risk analysis requires estimating potential damages from the hazard outcomes, and this type of input is not very helpful since most flood damage models use as input the water depth above ground level (and eventually flow velocity and flood duration) (Galasso et al., 2021; Mohanty et al., 2020; Nofal & Van De Lindt, 2022; Pregolato et al., 2015). For this reason, instead of translating these epistemic uncertainties into a probability map, some researchers have aimed to estimate the confidence intervals of the water-depths exceedance curves at the points of interest, reflecting all possible forcing events and inundation model's parameters (G. T. Aronica et al., 2012; Nuswantoro et al., 2016; Romanowicz & Kiczko, 2016).

This review of the literature on uncertainty quantification in flood hazard assessments shows that epistemic uncertainties are always kept separate from aleatory uncertainty. As a result, the hazard output is always in the form of a distribution of the probability of exceeding an IM level; whether it is given as a “probability of flood map” for different return periods (Bharath & Elshorbagy, 2018; Di Baldassarre et al., 2010; Domeneghetti et al., 2013; Kiczko et al., 2013; Neal et al., 2013; Stephens & Bledsoe, 2020; Zahmatkesh et al., 2021), or as confidence intervals of IM exceedance curves for each point in space (G. T. Aronica et al., 2012; Nuswantoro et al., 2016; Romanowicz & Kiczko, 2016). While this separation is useful to identify ways of reducing uncertainty, it has been shown to be challenging for proper communication and interpretation, even leading to inconsistent decision making (Der Kiureghian & Ditlevsen, 2009; Fawcett & Green, 2018; Fenton & Neil, 2013; Fox & Ülkümen, 2011). An alternative to this, that to the author's knowledge has not been implemented before in the context of flood hazard assessments, is to include epistemic uncertainty into a single measure of probability by integrating out over all possible forcing events (e.g., discharge events) and all possible inundation models. Within the Bayesian view of probabilities, this is known as “predictive posterior distribution,” and represents the distribution of future unobserved quantities given present data and knowledge (Gelman et al., 2013). Its use as a coherent measure of hazard that includes epistemic uncertainty has been explored in the area of risk-based engineering and design for many decades now (Cornell, 1972; Der Kiureghian & Ditlevsen, 2009; Li et al., 2022; Merz & Thieken, 2005). As discussed in Fawcett and Green (2018) in the context of environmental extremes, this single posterior probability estimate is easier to deal for practitioners and decision-makers, and it is shown that it has better statistical properties than other single metrics obtained from confidence intervals.

Overall, there seems to be a lack of flood hazard studies that include epistemic uncertainties in both the recurrence and inundation model, while also providing probabilistically coherent and useful input for further risk assessment and decision-making. Therefore, the objective of this work is to propose a methodology to integrate epistemic uncertainties into flood hazard assessments via the Bayesian predictive posterior distribution of the IMs, and discuss its implications as compared to the classical approach. Uncertainty in the parameters of the discharge recurrence model is estimated from a Bayesian Peaks-Over-Threshold (POT) approach and 20 years of daily discharge observations. Uncertainty in the inundation model, on the other hand, is computed for the channel and floodplain roughness parameters from the Generalized Likelihood Uncertainty Estimation (GLUE) framework and a single flood extent satellite observation. The predictive posterior distribution of water depths is then obtained empirically, by simulating from the uncertain parameters posterior distributions and computing the corresponding flood map for each. Flood hazard maps for different return periods can, then, be obtained by computing the corresponding marginal predictive distribution of water depths for each point in space. This novel methodology has the advantage over current approaches, of providing single hazard estimates and flood hazard maps that are useful for damage assessments and decision-making, while also providing a coherent treatment and inclusion of model's epistemic uncertainties. A simple case riverine case study is used to understand the implications of the proposed approach and to compare with the classical approach. However, it is important to highlight that the work does not intend to provide an exhaustive consideration of all sources of epistemic uncertainty or all modeling strategies for uncertainty quantification.

Section 2 describes the mathematical model used to compute hazard estimates, a framework to include epistemic uncertainties through model's parameters posterior distributions, and a simulation procedure for its numerical evaluation. A small case study of riverine flooding is described in Section 3 and used as a working example to

test this methodology. In Section 4, the resulting hazard curves and maps are compared to the traditional approach where no epistemic uncertainties are included. Insights in the hypothesis, results and implications of the model are analyzed in the discussions of Section 5, while a summary of main takeaways and potential future lines of research are drawn in the final section.

2. Methodology

2.1. The Hazard Model

As discussed in the introduction, flood hazard can be quantified as the annual probability of exceedance of a given IM level y , at any location of interest. Mathematically, this probability is calculated by a stochastic time process model. The most used ones in flood hazard analysis are derived from the standard Extreme Value Theory for stationary processes (Bezak et al., 2014; Bousquet & Bernardara, 2021; Fawcett & Walshaw, 2016). These come in the form of Bernoulli process (i.e., independent and identically distributed) of Annual Maxima (AM), or by the more general Homogeneous Poisson Process (HPP) for which events occur discretely with independent and exponentially distributed inter-arrival times with mean rate λ_0 . The HPP process will be used in this work as it remains a standard approach in flood frequency analysis and has several advantages over the simpler AM approach, particularly for short observation records (Bezak et al., 2014; Tabari, 2021). Under this model, the probability of exceedance over a timespan T can be computed as per Equation 1.

$$p_T(y) = 1 - \exp(-\lambda_0 T p(Y \geq y)) \quad (1)$$

where Y is the random IM for any given event, T is the timespan of interest, and $p(Y \geq y)$ is the probability of exceedance of level y for any given event (this probability is constant over time in the HPP).

The hazard is then computed by setting $T = 1$ in Equation 1 to obtain the annual probability of exceedance. For events with low recurrence λ_0 and low exceedance probability $p(Y \geq y)$, as is mostly the case in disaster risk analysis, the probability of Equation 1 can be further simplified as in Equation 2.

$$p_T(y) \approx \lambda_0 p(Y \geq y) \quad (2)$$

This is equivalent to the mean rate of exceedance of $Y \geq y$ or its multiplicative inverse, the mean time between occurrences $\text{Tr}(y)$, also known as “return period” (see Equation 3). In practical terms, hazard is measured by the annual probability of exceedance or by the mean rate of occurrence of IM level y , which are practically equivalent.

$$\lambda_0 p(Y \geq y) = \lambda(y) = \frac{1}{\text{Tr}(y)} \quad (3)$$

Since direct observations of water depths (or IMs in general) during flood events are very rare, probabilistic characterization of Y is usually done via mechanistic fluid-dynamics models, here called “inundation model” or simply “simulator.” This model depends on a number of observable boundary conditions X that are considered to vary event to event, such as upstream river discharge, rainfall intensity or sea-level rise. It also depends on a set of unobserved calibration parameters β considered constant over events, such as the soil roughness parameters or the channel cross-section geometry (see Equation 4).

$$Y = S(X, \beta) \quad (4)$$

In this context, an “event” is characterized by a magnitude X which describes the impact potential of the phenomenon. For example, in riverine flooding, X can represent the river discharge flow and an event is triggered when it surpasses a given threshold. Analogously, in coastal flooding, X might stand for sea-level extreme rise, or in pluvial flooding where X stands for rainfall intensity. In more complex scenarios, X can be a vector representing multiple quantities, such as flow discharge and volume, rainfall intensity and duration, or a combination of flow discharge and sea-level rise. For the sake of simplicity, this work will focus on scalar X .

Since Y is a function of X , the probability $p(Y \geq y)$ in Equation 2 can be computed by conditioning on the probability distribution of the event's magnitude X as given by,

$$p(Y \geq y) = \int_x \mathbf{1}\{S(x, \beta) \geq y\} p(x|\theta) dx \quad (5)$$

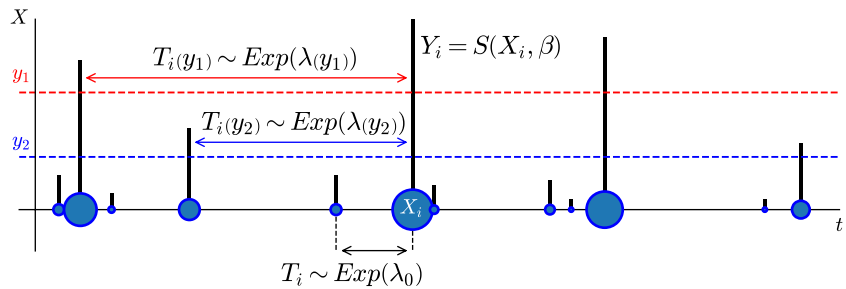


Figure 1. Schematic illustration of a realization of the HPP model, with two arbitrary IM levels y_1 and y_2 to define the hazard.

where $\mathbf{1}\{\text{cond}\}$ is an indicator function that returns 1 when cond is true and 0 otherwise and θ is a vector of parameters that describe the probability distribution of X .

This expression is useful as long as it is easier to define the probability distribution of events magnitudes $p(x|\theta)$ than the distribution of IM levels $p(Y \geq y)$ from data or expert knowledge. As mentioned before, this is the typical case in flood hazard, where we usually have relatively robust historical measurements of river flow discharges or rainfall intensity, but very few of water depths at points of interest in the floodplain.

Introducing Equation 5 into Equation 2, we obtain the full expression for the flood hazard,

$$\lambda(y) = \int \underbrace{\mathbf{1}\{S(x, \beta) \geq y\}}_{\text{Inundation model}} \underbrace{\lambda_0 p(x|\theta)}_{\text{Events recurrence model}} dx \quad (6)$$

An illustrative scheme of a realization of the described time process is shown in Figure 1. The varying sizes of the blue bubbles reflect the magnitude X_i of the events, while the black bars reflect the IM level (i.e., water depth) for each. According to the HPP model, the time T_i between events follows an exponential distribution with mean rate λ_0 , while the time between IM exceedances $T_i(y)$ (the black bars that cross the dotted red line) follows an exponential distribution with mean rate $\lambda(y)$ as described in Equation 6.

It is important to highlight that the model summarized here is replicated when analyzing the hazard for other types of natural phenomena. In the case of seismic hazard, X is the moment magnitude and spatial epicenter location of the earthquake and their probability distribution is typically given by the Gutenberg-Richter law and the source-to-site propagation model is defined by the Ground Motion Prediction Equations (GMPEs) (Baker et al., 2021). For typical hurricane winds hazard, the recurrence model describes the likelihood of the hurricane's central pressure and track, while the propagation model is described through a wind field model (Vickery et al., 2006).

2.2. Including Epistemic Uncertainties

The hazard problem is, as described by Equation 6, tightly related to predicting an uncertain event in the future. Thus, it is strictly an uncertainty quantification task. At its core, that expression is a mathematical representation of what is known as “aleatory uncertainty,” here characterized by the exponentially distributed inter-arrival times with mean rate λ_0 and the probability distribution of the event's magnitude $p(x|\theta)$.

Aleatory uncertainty is considered an inherent component of the physical process and it does not depend on the amount of knowledge and information the modeler has. However, there are other sources of uncertainty around the estimation of the hazard that are related to our incomplete knowledge about the physical process and data available to characterize it. These are commonly known as “epistemic uncertainties” (Spiegelhalter & Riesch, 2011).

As described by Spiegelhalter and Riesch (2011), epistemic uncertainty stems mainly from (a) limited information to properly characterize the models and variables involved and (b) limited knowledge to properly describe the

true physical processes through the selected models. This more operational description of epistemic uncertainties allows for a more rigorous way of including them in the mathematical model.

Limited information appears in practice, as limited-length data, observation errors, or missing variables. It can, typically, be represented through uncertainty in the parameters that describe the models as data is not sufficient to perfectly identify them. Limited knowledge, on the other hand, is usually represented through simplifying assumptions, such as the ones in the HPP model, the distribution family chosen for $p(x|\theta)$, or the particular physics-based model chosen for S . These can be harder to represent mathematically, although it can be done through averaging model ensembles, such as Bayesian Model Averaging (Madadgar & Moradkhani, 2014), or via statistical representations of model deficiencies as developed in Abbaszadeh et al. (2019) and Pathiraja et al. (2018) for dynamical hydrological models or in J. W. Hall et al. (2011) and Balbi and Lallemand (2023) for hydraulic inundation models.

In particular, this work focuses on the inclusion of epistemic uncertainty through model's parameters as a broad representation of limited data to define the models. This is not intended to provide a comprehensive treatment of epistemic uncertainties, but rather analyze the potential influence of parametric uncertainties in hazard assessments. Other sources of epistemic uncertainties, such as structural model uncertainty, can be straightforwardly included in this same methodology. In this context, hazard as calculated in Equation 6 can be understood as being conditional to a given set of models and parameters as given by,

$$\lambda(y|\beta, \lambda_0, \theta) = \int \mathbf{1}\{S(x, \beta) \geq y\} \lambda_0 p(x|\theta) dx \quad (7)$$

As discussed in the introduction, the proposed way of incorporating uncertainty regarding the values of the set of parameters $\{\beta, \lambda_0, \theta\}$ is provided by the Bayesian predictive posterior distribution. This estimate is obtained by averaging the conditional hazard of Equation 7 over all possible values of the parameters $\{\beta, \lambda_0, \theta\}$ weighted by their posterior distribution $p(\Theta|data)$ as per Equation 8.

$$\lambda(y|data) = \int_{\Theta} \lambda(y|\lambda_0, \beta, \theta) p(\lambda_0, \beta, \theta|data) d\lambda_0 d\beta d\theta \quad (8)$$

In the Bayesian framework, the posterior distribution of the parameters $p(\lambda_0, \beta, \theta|data)$, is the probability conditional on the available data and modeler's prior knowledge obtained by means of Bayes' Theorem (Gelman et al., 2013). The posterior distribution is proportional to the probability of observing the data given a set of parameters, also known as "likelihood function," multiplied by the probability of a given set of parameters before incorporating the data, also known as "prior distribution" (see Equation 9). This can be colloquially described as the modeler's knowledge (i.e., prior distribution) times the information contained in the observations (i.e., the likelihood function).

$$p(\lambda_0, \beta, \theta|data) \propto p(data|\lambda_0, \beta, \theta) p(\lambda_0, \beta, \theta) \quad (9)$$

Equation 8 allows us to compute the hazard curve of water depths (or the IM chosen for the analysis) for any given point in space. Or inversely, compute the water depth for a given rate or return period. Hence, we can develop the T-years flood hazard map by marginally computing the y level for that return period from the expression.

In the following sub-sections we describe the methodology to estimate the posterior probability distributions of the parameters from Equation 9, and the simulation methodology to estimate the hazard as per Equations 7 and 8.

2.2.1. A Bayesian Recurrence Model

In the framework described above, the recurrence model aims to quantify the mean rate of occurrence λ_0 of events, and characterize the distribution of the magnitude X and its parameters θ for any given event. These can be obtained from the statistical analysis of time series of past events. Poisson Point Process theory, as a generalization of the well-known Peaks-Over-Threshold (POT) methodology, provides a robust framework for this (Bezak et al., 2014). Extreme events are individualized from historical records of daily discharges, by selecting an appropriate minimum threshold u and time separation to ensure independence. This results in a data set of observed independent times between events \hat{T} and a data set of observed event's magnitudes \hat{x} . A Generalized Pareto Distribution (GPD) is then used as the probability model for the exceedances above the threshold $x - u$, and the inter-arrival time between events is assumed to be exponentially distributed. This is,

$$T \sim \text{Exp}(t|\lambda_0) \quad (10)$$

$$X - u \sim \text{GPD}(x|\xi, \sigma) \quad (11)$$

where λ_0 is the mean rate of arrival, ξ and σ are the shape and scale parameters that define the GPD distribution, and u an appropriately defined threshold.

Hence, two probability models are required to describe the occurrence of events. An exponential distribution model of parameter λ_0 for the time between arrivals, and a GPD of parameters $\theta = \{\xi, \sigma\}$ for the magnitude of each event. Bayesian statistics provide an ideal framework to compute uncertainty in model's parameters that are consistent with the modeler's prior knowledge and proposed model (Bousquet & Bernardara, 2021).

For the data set of observed interarrival times \hat{T} , the likelihood function is simply a product of n exponential densities, where n is the number of observations. The posterior distribution of the mean rate λ_0 can be obtained by assuming a weakly informative $\text{Gamma}(1/2, 1/2)$ prior distribution. A weakly informative prior distribution is relatively flat in the entire range of plausible values for the parameter. For this choice of prior, the posterior distribution has a closed form solution as given in Equation 12 since it is a conjugate pair for the Exponential likelihood (Gelman et al., 2013).

$$p(\lambda_0|\hat{T}) = \text{Gamma}(n + 1/2, t + 1/2) \quad (12)$$

where n is the number of events and $t = \sum_{vi} \hat{T}_i$ is the total number of years in the series.

The most likely value of the rate of occurrence given the observations is given by the mode of the posterior probability of Equation 12, also known as the Maximum A-Posteriori (MAP) estimate. The MAP estimate and the mean value of the posterior distribution for λ_0 are given by Equations 13 and 14 respectively.

$$\lambda_0^* = (n - 1/2)/(t + 1/2) \quad (13)$$

$$\overline{\lambda_0} = n/t \quad (14)$$

For the data set of observed event's magnitudes \hat{x} , the likelihood function is given by a product of n GPD densities. There is no conjugate model for this likelihood, but a non-informative prior can be built for the shape and scale parameters following Castellanos and Cabras (2007) (Equation 15).

$$p(\xi, \sigma) \propto \sigma^{-1}(1 + \xi)^{-1}(1 + 2\xi)^{-1/2} \quad (15)$$

Valid for $\xi > -0.5$ and $\sigma > 0$.

Then, the un-normalized expression for the posterior can be obtained by Bayes theorem as per Equation 16, and the predictive posterior distribution for X can be subsequently computed as per Equation 17. In both cases, there is no analytic solution, and samples from the distribution can be done via standard Markov Chain-Monte Carlo (MCMC) methods (Gelman et al., 2013). These can also be used to compute posterior mean and MAP estimates for ξ^* , σ^* .

$$p(\xi, \sigma|\hat{\mathbf{x}}) \propto p(\xi, \sigma) \prod_{i=1}^n (1 + \hat{\mathbf{x}}_i \xi / \sigma)^{-(1+\xi)/\xi} \quad (16)$$

$$p(x - u|\hat{\mathbf{x}}) = \int \text{GPD}(x - u|\xi, \sigma) p(\xi, \sigma|\hat{\mathbf{x}}) d\xi d\sigma \quad (17)$$

2.2.2. Probabilistic Inundation Model

The inundation model is, in this context, a computational solver of some simplified version of the fluid-dynamics equations that depend on variable inputs X and calibration parameters β . Epistemic uncertainties might come from lack of sufficient information to calibrate the parameters, observation errors, mechanistic simplifying assumptions, and numerical simplification of the equations solver (Kennedy & O'Hagan, 2001). We assume here, due to simplicity, that for a given simulator $S(X, \beta)$ these can be represented by uncertainty in the model's calibration parameters β . More complex procedures to include model uncertainty can be used to include uncertainty in the

Table 1
Summary of Variables and Symbols

Variable	Description
X	Flood event's magnitude (i.e. river peak discharge)
Y	Flood IM (i.e. flood depth) at a given point in space
λ_0	Mean rate of occurrence of events $X \geq 0$
$\lambda(y)$	Mean rate of occurrence of events $Y \geq y$
β	Inundation simulator calibration parameters
$S(X, \beta)$	Inundation simulator
ξ	GPD shape parameter
σ	GPD scale parameter
u	Threshold value for X POT model
$\bar{(\cdot)}$	Mean value of parameter
$(\cdot)^*$	MAP value of parameter (mode of its posterior distribution)

model structure. For example, a formally probabilistic calibration procedure that includes model structural uncertainty as an additive Gaussian Process is discussed in Balbi and Lallemand (2023).

Parameters' distributions can be obtained using nominal probability models from expert's knowledge (Kalyanapu et al., 2012; Stephens & Bledsoe, 2020) or statistically calibrated ones generally via the GLUE methodology (G. T. Aronica et al., 2012; Di Baldassarre et al., 2010; Kiczko et al., 2013; Romanowicz & Kiczko, 2016; Zahmatkesh et al., 2021). In this work, epistemic uncertainty will be represented by probability distributions in the roughness parameters only, for the floodplain and for the channel, considering all other parameters, such as DEM or channel bathymetry, as constant regarding the calibration procedure. This choice does not intend to imply that the uncertainty in the rest of the parameters is non-significant in this case study, and serves the purpose of providing a particular example of how uncertainty in the inundation model can be quantified and how it might affect hazard estimates. In any case, roughness parameters are generally ideal candidates to be used as calibration parameters since they are hard to estimate from direct observations or from physical principles, and their values significantly affect the model's output (Papaioannou et al., 2017; Sreedevi & Eldho, 2019).

The posterior distributions of these parameters will be obtained by means of the GLUE framework, where all possible sets of parameters are assigned a normalized score (i.e., pseudo-likelihood) from an appropriately selected scoring rule. In the case of flood extent binary observations (as in the case study developed in this work), it is typical to use the F-score (as per Equation 18), a variant of the classical Jaccard Index (G. T. Aronica et al., 2012; Papaioannou et al., 2017).

$$F(\beta) = \frac{A - B}{A + B + C} \quad (18)$$

Where A is the number of correctly predicted pixels, B the number of over-predicted pixels (predicted flooded, observed non-flooded), and C is the number of under-predicted pixels (predicted non-flooded, observed flooded).

The details of the calibration procedure using the GLUE framework can be found in Balbi and Lallemand (2023), but they can be summarized in four steps:

1. Sample a large set of β from their prior distribution
2. Compute the F-score for the sampled β
3. Reject all "non-behavioral" models using some thresholding criteria: $F < f^*$
4. Standardize the resulting F-scores so that they are all positive and integrate to 1

The model fit for each value of β is, then, a measure of its uncertainty, or pseudo-posterior probability (as it is not strictly obtained from a probabilistic likelihood). In addition, the MAP (i.e., equivalent to the Maximum Likelihood Estimate for a flat prior distribution) value for parameter β is the one that yields the best fit (i.e., largest F-score), and is the set of parameters generally used when defining an "optimal" deterministic model in the classical approach.

2.3. Numerical Implementation

Computing the integral from Equation 8 requires numerical procedures since no analytic solution exist for the posterior distributions of the parameters just described. Since many parameters are involved in its computation, a summary of variables and symbols can be found in Table 1.

Equation 8 can be slightly simplified, however, by noting that $\lambda(y|\lambda_0, \beta, \theta)$ is linear on λ_0 and its posterior distribution (Equation 12) is independent from the rest of the parameters as given by Equation 19.

$$\lambda(y|data) = \bar{\lambda}_0 \int_{\beta, \xi, \sigma} p(Y \geq y|\beta, \xi, \sigma) p(\beta, \xi, \sigma|data) d\beta d\xi d\sigma \quad (19)$$

where $\bar{\lambda}_0$ is the mean of the posterior distribution of λ_0 given by Equation 14.

Standard Monte-Carlo (MC) integration techniques can be employed to compute such integral. Conceptually the task is straightforward: we need to sample from the posterior distribution of Y , by sampling first from the posterior of X . This can be done through the following steps:

1. Sample N values from the posterior distribution of β (as per Section 2.2.2) and $\{\xi, \sigma\}$ (from Equation 16)
2. For each sample of $\{\xi_i, \sigma_i\}$, sample x_i from Equation 17
3. For each sample x_i and β_i , compute water depth at all points of interest from the simulator $y_i = S(x_i, \beta_i)$
4. Estimate the mean rate of exceedance of y as:

$$\lambda(y|\text{data}) \approx \frac{\bar{\lambda}_0}{N} \sum_i \mathbf{1}\{S(x_i, \beta_i) \geq y\}$$

The number of samples N required for the simulation depends on the percentile of the curve (i.e., return period) we are trying to estimate and the precision desired. For example, to estimate the 100 years return level y_{100} we need to estimate an exceedance probability $p(Y \geq y_{100}) = (100\lambda_0)^{-1}$. According to the standard theory of empirical estimates of probabilities, based on the Central Limit Theorem (CLT), we can obtain an approximate minimum number of simulations for a 95% confidence interval as per,

$$N > \frac{1.96}{\varepsilon^2} \sqrt{\frac{1-p}{p}} \quad (20)$$

where p is the actual probability being estimated (not exactly known) and ε is the width of the relative interval (Melchers & Beck, 2018).

On the other hand, the computation of the hazard in the classical approach (as given by Equation 5), where no epistemic uncertainties are considered, is much simpler:

1. Obtain the return levels of the GPD distribution for each return period Tr of interest, and for fixed parameters ξ^* and σ^* as given by (see Appendix A for details),

$$x_{\text{Tr}} = u + \begin{cases} \frac{\sigma^*}{\xi^*} \left\{ (\lambda_0^* \cdot \text{Tr})^{\xi^*} - 1 \right\}, & \text{if } \xi^* \neq 0 \\ \sigma^* \ln(\lambda_0^* \cdot \text{Tr}), & \text{if } \xi^* = 0 \end{cases}$$

2. For each Tr , compute water depth at all points of interest for fixed parameters β^* from the simulator $y_{\text{Tr}} = S(x_{\text{Tr}}, \beta^*)$

That is, we compute x for different return periods of interest (also known as return levels), and then evaluate the inundation model at each. It is important to note, that this two-step approach can be followed but for an entire ensemble of posterior realizations of parameters $\{\beta_i, \xi_i, \sigma_i\}$, to obtain an estimate of the predictive posterior estimate including epistemic uncertainties. This method requires many times more the number of calls to the inundation simulator S relative to the four-step procedure described above, but has the advantage of obtaining credible intervals for the estimate.

3. Case Study

The proposed methodology described in Section 2 is applied here in a real-world case study, with the purpose of analyzing the influence of the inclusion of epistemic uncertainties in the recurrence model of river discharges (as per Section 2.2.1) and in the inundation model (as per Section 2.2.2).

3.1. Models and Data

The case study is based on a short reach on the upper river Thames in Oxfordshire, England, just downstream from a gauged weir at Buscot (Figure 2). The river at this reach has an estimated bankfull discharge of 40 m/s³ and drains a catchment of approximately 1,000 km². The topography was obtained from stereophotogrammetry at a 50 m scale with a vertical accuracy of ± 25 cm, obtained from large-scale UK Environment Agency

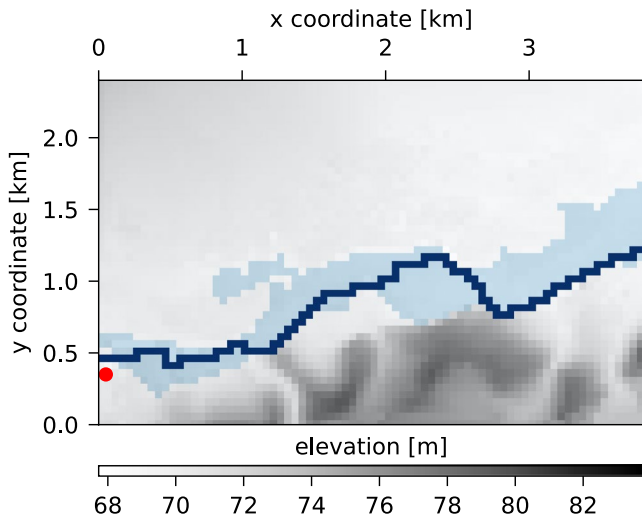


Figure 2. Floodplain topography at Buscot, SAR imagery of 1992 flood event (light blue), channel layout (dark blue) and gauge station location (red dot).

maps and surveys. This reach has also been study previously in G. Aronica et al. (2002), J. W. Hall et al. (2011), and Balbi and Lallemand (2023).

The events are characterized by the river discharge flow only. To develop the recurrence model for events, a publicly available daily discharge data series at Buscot weir was obtained from the UK National River Flow Archive (see Figure 3). The series spans from 19 years from 1980 to 1998 with some minor gaps that are not expected to affect the extreme statistics analysis to perform.

On the other hand, for the calibration of the inundation model, a satellite observation of the flood extent of 1-in-5 years event occurred during December 1992 was used (see Figure 2). The satellite SAR (synthetic aperture radar) image of the flood was captured 20 hr after the flood peak when discharge was at a level of $73 \text{ m}^3/\text{s}$ (Bradbrook et al., 2004; Horritt & Bates, 2001). The resolution of the image is 50 m.

The computational inundation model used is the raster-based Lisflood-fp model (Neal et al., 2012). Lisflood-fp couples a 2D water flow model for the floodplain and a 1D solver for the channel flow dynamics. Its numerical structure makes it computationally efficient and suitable for the many simulations needed for probabilistic flood risk analysis and model calibration.

A simplified rectangular cross-section is used for the channel with a constant width of 20 m for the entire reach and a bankfull depth of around 2 m to obtain a bankfull discharge of around $40 \text{ m}^3/\text{s}$ as defined by UK's Environment Agency (Bradbrook et al., 2004; Horritt & Bates, 2001). The observed event is defined by the boundary condition of a fixed input discharge of $x = 73 \text{ m}^3/\text{s}^3$ at the geographic location of the gauging station shown in Figure 2, and by a downstream fixed free surface elevation of approximately 90 cm above the channel bed height, obtained from an optimal fit to the flood extent observation as discussed in Horritt & Bates (2001). The short length of the reach and the broadness of the hydrograph imply that a steady-state hydraulic model is sufficiently accurate for the calibration (G. Aronica et al., 2002).

The model's parameters used for calibration are the Manning's roughness parameters for the channel r_{ch} and for the floodplain r_{fp} , both considered spatially uniform in the domain of analysis. That is, $\beta = \{r_{ch}, r_{fp}\}$. For the calibration method described in Section 2.2.2, the inundation model was ran for a fixed observed discharge of $73 \text{ m}^3/\text{s}$ and for a uniform prior for both parameters in the range 0.01–0.15.

3.2. Computational Implementation

The statistical models and simulation method described in Section 2.3 were implemented in Python 3.X language (Van Rossum & Drake, 2009), using a 10-core Intel i9-10700k processor computer. Each evaluation of the

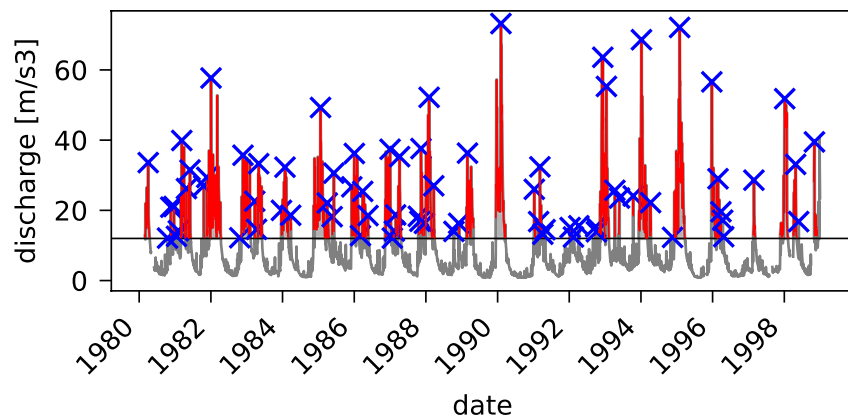


Figure 3. Daily discharge for Buscot and identification of flood events by clustering with a $12 \text{ m}^3/\text{s}^3$ threshold and 7 days of minimum return. Blue cross indicates event's peak discharge.

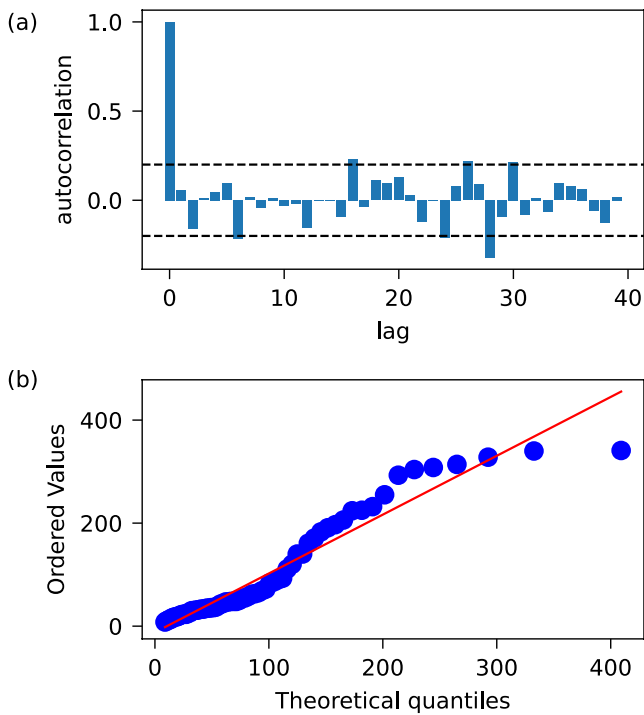


Figure 4. (a) Autocorrelation plot of discharge series; (b) Probability plot of interarrival times compared to the exponential distribution.

inundation model $S(X, \beta)$ takes approximately 4s. For the calibration of the inundation model 19,600 evaluations of the simulator were needed to cover the entire grid of β values, and around 100,000 evaluations were needed for the hazard simulation procedure from Section 2.3.

4. Results

4.1. Discharge Recurrence Model

To define the events and their magnitudes, a threshold of $u = 12 \text{ m}^3/\text{s}$ and minimum distance between clusters of 7 days (i.e., there has to be 7 days of values below the threshold for two events to be considered as separate events) were selected aiming to satisfy the conditions required by POT standard theory (Bousquet & Bernardara, 2021):

- The minimum threshold for which the modified scale and shape parameters of the fitted GPD of the exceedances remain constant for higher thresholds.
- The resultant threshold exceedances (cluster's peaks) should form an independent sample.

A total of 73 clusters were identified in 18.8 years of data as shown in Figure 3. That is, on average, 3.9 events per year, and it shows the relative advantage of this type of analysis versus the standard annual maximum approach for which there would only be 18 data points. The posterior distribution of the mean rate λ_0 , as given by Equation 12, has a mode (i.e., MAP) $\lambda_0^* = 3.8 \text{ yrs}^{-1}$ and a mean value $\bar{\lambda}_0 = 3.9 \text{ yrs}^{-1}$. Statistical graphical tests, shown in Figure 4, showed that the resulting series of extreme discharges can

be considered independent and that the time between events has a good fit to the exponential model as assumed in the HPP model.

Samples of the posterior distribution of the GPD parameters (Equation 16) were drawn by a standard MCMC algorithm of 4 chains of 15,000 samples each. Discarding the first half of sample from each as burn-in stage, convergence of the chains was assessed by verifying that Gelman-Rubin R-scores remains below 1.01 (Gelman et al., 2013). Goodness-of-fit tests showed a good agreement of the exceedances with the GPD. The shape parameter ξ is centered around -0.05 while the scale parameter σ is centered around 16.5, both with a relatively small skewness (see Figure 5). The MAP values for the parameters practically coincide with these values.

For each posterior sample of ξ and σ , the probability distribution of the discharges follows a GPD. With the ensemble of distributions for each sample, we computed the mean curve (i.e., the predictive posterior distribution of X) and the 90% confidence posterior intervals. These are shown as return period curves in Figure 6 as computed by,

$$\text{Tr}(x) = 1/\lambda_0^* p(X \geq x) \quad (21)$$

A “deterministic” hazard curve was also computed using the MAP values for the GPD parameters, following the classical approach. It can be seen that epistemic uncertainties have the effect of increasing the discharges for a given return period, and that this effect increases with increasing return period. This is intuitive, as larger return periods are more uncertain with limited-length data. Similar results have been obtained before (Fawcett & Green, 2018; Merz & Thielen, 2005; Romanowicz & Kiczko, 2016).

4.2. Inundation Model

The statistical calibration of the inundation model was done by using a uniform grid for both parameters in the range (0.01, 0.15) with a step

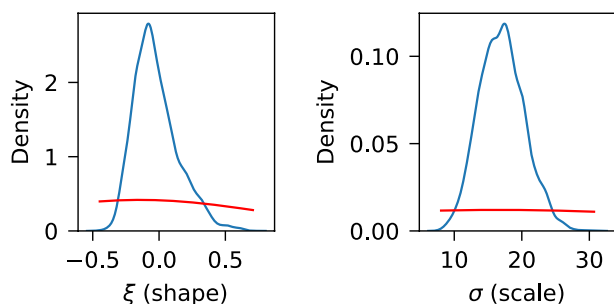


Figure 5. Posterior (blue) and prior (red) distributions of the GPD parameters.

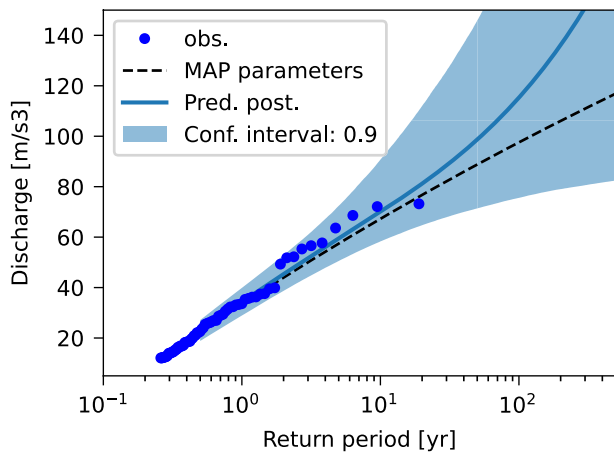


Figure 6. Hazard curves for river discharge.

of 0.01, and a threshold of 0.5 to filter out non-behavioral models. This resulted in a total of 543 accepted simulations out of 19,600. The bivariate pseudo-posterior distribution for the roughness parameters is shown in Figure 7. The set of parameters that yields the maximum F-score (i.e., MAP parameters), and define the “optimal” deterministic model, were $r_{ch} = 0.029$, $r_{fp} = 0.045$ giving $F = 0.54$.

4.3. Flood Hazard

Close to 15,000 thousand posterior samples of water depth Y at all points in the region were obtained, following the simulation procedure described in Section 2.3. This allowed to empirically estimate the posterior exceedance recurrence $\lambda(Y \geq y|data)$ for every pixel and, consequently, the hazard curve. The number of simulations ran implies that exceedance probabilities as small as 10^{-4} can be estimated with a 10% interval according to Equation 20. For a mean value $\bar{\lambda}_0 = 3.8yr s^{-1}$, this is equivalent to RPs of up to 1, 500 years.

Figure 8 shows the flood depth hazard curves for different points in the floodplain. These points were arbitrarily picked with the intention of selecting points on recurrently flooded pixels at both sides of the river channel (points $p1$ and $p2$) and points in regions less frequently flooded, or farther from the channel (points $p3$ and $p4$ respectively). The posterior predictive curves are compared with the classical approach that uses the deterministic discharge hazard curve (dotted black curve in Figure 6) and the MAP parameters for the inundation simulator. In every case, it can be seen that the flood depth values of the posterior predictive curves increase faster than the classical approach as the return period grows, in a similar fashion observed in the discharge hazard model of Figure 6. Furthermore, the two curves are very similar for lower return periods.

The 100 years flood hazard map was developed by computing the 100 years flood depth from the posterior predictive curves at each point (see Figure 9). This map is compared in plot (a) of Figure 10 with the traditional hazard map computed using the optimal deterministic inundation model (i.e., using the MAP roughness parameters) with the classical estimate of the 100 years discharge (see black dotted line in Figure 6). This and the other maps in Figure 10 show the difference between the predictive posterior estimate of the water depths and the classical estimate for a specific return period at every pixel. The yellow dotted line indicates the flood extent for the classical approach map for that RP. The increasing flood depth for the posterior predictive map can be seen to be replicated for every pixel in the region of analysis with the exception of some isolated pixels right next to the channel. This effect, as in the discharge hazard curve, is exacerbated with increasing return periods as can be seen in plot (b) and (c) of the figure for the 250 and 500 years maps comparison.

5. Discussion

5.1. On the Influence of Epistemic Uncertainties in Hazard Estimates

From an engineering design perspective, the results show that the water height used to design a structure for a specified safety level (i.e., return period) will be larger when including epistemic uncertainties. That is, when including our lack of knowledge and information on the process, we need to be more conservative in design to ensure an appropriate level of reliability. Furthermore, these differences increase with the return period as shown in difference maps of Figure 10 and in the hazard curves of Figure 8, and is practically negligible for more recurrent events. This result is somewhat intuitive as we usually have less knowledge on rare events, and similar conclusions have been obtained by other researchers in environmental extremes (Fawcett & Green, 2018; Merz & Thielen, 2005).

As explained in the previous section, results indicate that this is true for every pixel in the region of analysis (see Figure 10). For this particular case

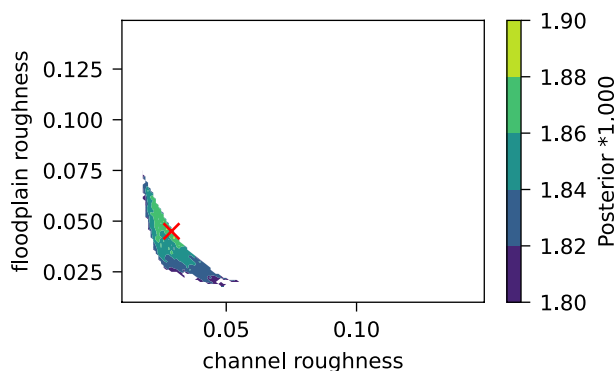


Figure 7. Bivariate posterior distribution for inundation model parameters.

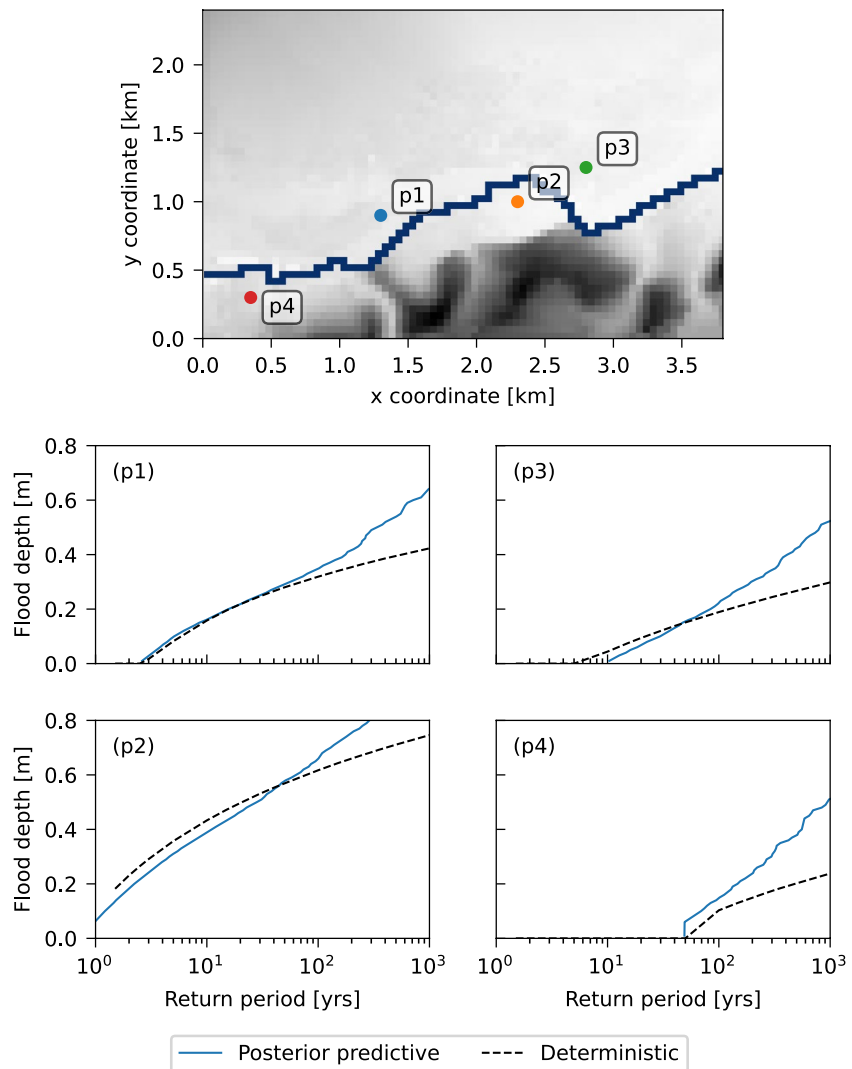


Figure 8. Hazard curves for flood depths at different locations in the floodplain.

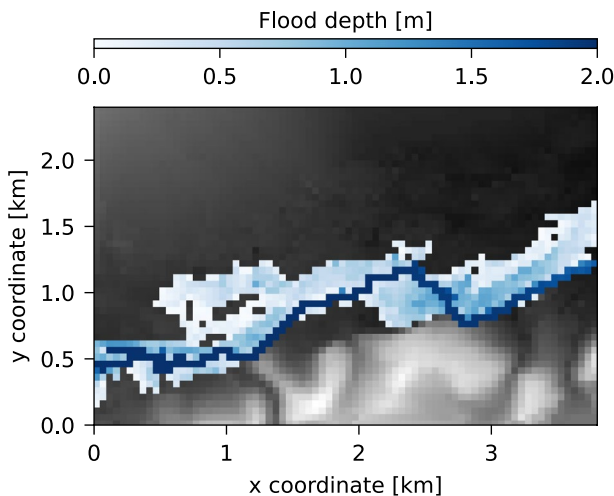


Figure 9. 100 years flood hazard map using posterior predictive flood depth at each point.

study, differences in flood height can be as high as 50% for 500 years as seen in the curves of Figure 8. Even more so, the difference maps of Figure 10 show that some pixels might even appear as flooded when that is not the case for the classical approach. Consequently, epistemic uncertainties can lead, not only to an increase in the water-depth estimate for a given RP, but also to an increase in the flood extent itself.

To further understand the implications and generalization of these results, however, we need to understand the relative influence of epistemic uncertainties on the discharge recurrence model and on the inundation model. To do this, we obtained the predictive posterior hazard curves while including epistemic uncertainties one model at a time, as shown in Figure 11.

5.1.1. In the Discharge Recurrence Model

Figure 11 shows that when epistemic uncertainties are considered only in the discharge recurrence model, predictive estimates of water depths for a given return period are also above the classical approach. This is a consequence of the similar trend found in the predictive posterior estimates of discharges

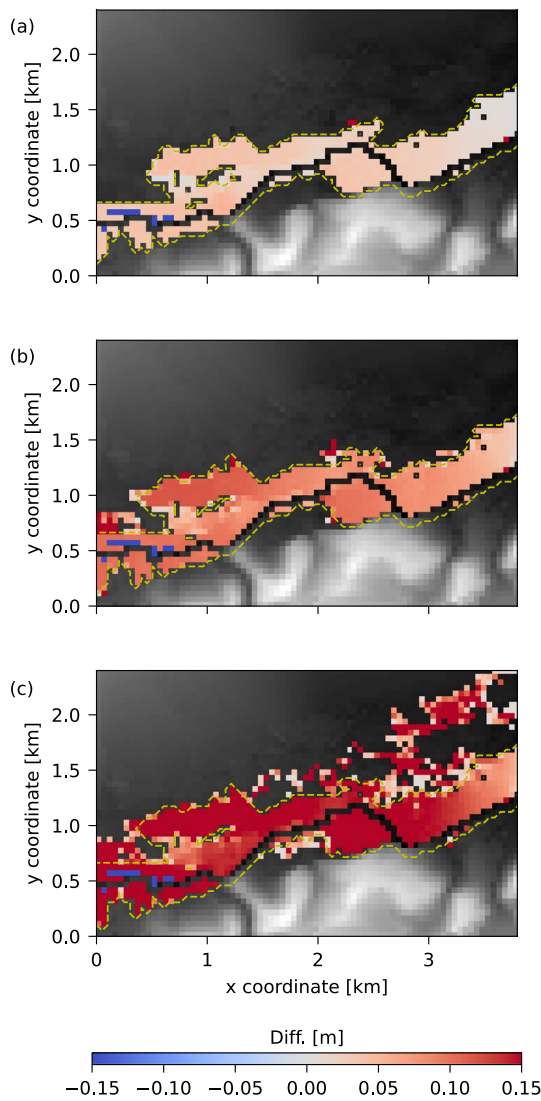


Figure 10. Difference maps between posterior predictive estimates and deterministic estimates for (a) 100 years, (b) 250 years, (c) 500 years. The dotted yellow line indicates the flood extent for the classical approach hazard map for that RP.

levels are relatively constrained by the topography, it is not expected that the inundation simulator presents a radically high non-linearity.

We can infer that the highly skewed shape of the roughness parameters posterior distribution (Figure 7) with respect to the MAP values, might be the main driver responsible for the underestimation in flood hazard. Consequently, the uncertainty quantification method (e.g., GLUE) and the data used (e.g., binary flood extent) can play a major role in the way that uncertainties influence the final hazard estimates. Overall, for this case study, the influence of uncertainty in the inundation model is lower than the one for the discharge recurrence, particularly for larger return periods. However, further analysis is required in order to deeply understand how this influence varies in different settings (i.e., different observations, different calibration methods and inundation models), and understand if this effect can be magnified in some contexts.

in Figure 6, that mainly represents uncertainty due to the limited-length observed time series used to build the model. That is, using an 18-year data record, there are practically no observations of much higher return periods which is reflected in the larger uncertainty.

This result is in line with common findings in the theory of predictive posterior distributions when uncertainty in the parameters of the original distribution is included (Gelman et al., 2013). This has been shown in the context of hydrological analysis of discharge series (Merz & Thielen, 2005) and in the general theory of environmental extremes (Bousquet & Bernardara, 2021; Fawcett & Green, 2018). Accordingly, it is not a specific feature of the POT method used to derive the recurrence of extreme discharges, but rather a general property of statistical estimators under parametric uncertainty using short-length data.

To support this, we show in Figure 12 the recurrence curve for extreme discharges using the typical Annual Maxima approach. This was obtained by fitting a Generalized Extreme Value (GEV) distribution to the 18 annual maxima series, and computing the posterior distribution of the three parameters of the distribution. Once again, it can be seen that the predictive posterior distribution of discharges has a longer tail than the one for the MAP parameters. This time, the difference between the two curves is even larger than for the POT method since the annual maxima series has only 18 observations. As in the POT case, this difference between both curves will be directly translated to the water-depth curves.

5.1.2. In the Inundation Model

When epistemic uncertainty is only considered for the inundation model's parameters, on the other hand, predictive estimates of water depths are lower than for the classical approach as seen in Figure 11. That is, for most sets of roughness parameters in the posterior distribution, water depths seem to be lower than the ones obtained for the MAP estimate. This can be, in part, related to the relative position of the MAP roughness parameters within the overall posterior distribution as shown in Figure 7, but also to the non-linear nature of the S transformation that implies that the average water depth for all parameters is not the same as the water depth for the average (or MAP for the case) parameters. Therefore, the influence of epistemic uncertainty in the parameters of the inundation model is in general related to their posterior distribution and, consequently, to the calibration methodology (i.e., F-score pseudo-likelihood here), the types of observations used for calibration (i.e., binary flood extent observations in this case). In particular, given that water

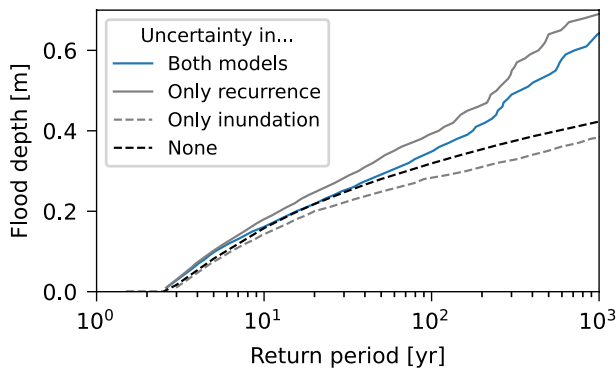


Figure 11. Hazard curves for water depth at coordinates $x = 1.30$ km, $y = 1.05$ km, when considering epistemic uncertainty in both models (recurrence and inundation), only in the recurrence model, only in the inundation model, and in any of both (classical approach).

5.2. On the Usefulness of the Output

From a risk analysis standpoint, we might be interested in computing some damage measure, or any higher-level decision metric, that reflects the impact of the flood in human communities. The framework is analogous to the one described here, but instead we are interested in the distribution of the decision metric Z over all the potential hazard events. We can straightforwardly compute this from the probability distribution of the IM, as in Equation 22. The first factor in the integrand represents the probability of exceeding some impact level z for a given level of IM (e.g., flood depth) as can be computed from a vulnerability model (Galasso et al., 2021; Mohanty et al., 2020; Nofal & Van De Lindt, 2022; Pregolato et al., 2015; Scawthorn et al., 2006; Wang et al., 2021).

$$\lambda(z) \approx \int \underbrace{p(Z \geq z|y)}_{\text{Vulnerability model}} \underbrace{\lambda_0 p(y)}_{\text{Hazard model}} dy \quad (22)$$

Equation 22 shows that we actually need the recurrence of water depth y (and eventually other IMs like duration, or velocity) at any site of interest in order to compute the risk. For most modern vulnerability models then, a probability of flood map for a given return period is not useful since it does not provide the required information. The hazard maps, as developed in this work, provide a reliable estimate of the recurrence $\lambda_0 p(y)$ while also accounting for epistemic uncertainties. Specifically the maps show the water depths for a given return period that can be transformed into an exceedance probability as per Equation 2.

It is important to note that the maps reflect marginal probabilities and do not take into account spatial correlation in the flood process, as they are built by individually computing the hazard curves at each point. In other words, the resulting hazard maps (as in Figure 9) do not show a real flood event. For this reason, the hazard maps are useful for site-specific hazard, and eventually risk analysis, but not for analyzing spatially distributed assets. However, these maps were built from an ensemble of simulated flood maps as per the MC simulation approach described in Section 2.3. This ensemble is a direct output of the inundation simulator, and thus, can be used to estimate damage for spatially distributed exposure while propagating epistemic uncertainties in the hazard model.

5.3. On the Separation of Aleatory and Epistemic Uncertainties

The posterior predictive estimate for the hazard proposed in this work combines in one metric both the aleatory and epistemic uncertainty. While this is important for risk-based decision making, it does not directly help exploiting the main distinction between the two: that epistemic uncertainties can potentially be reduced by further collecting data or improving our models.

Qualitatively speaking, the departure of the posterior predictive curves from the deterministic hazard curve (Figure 11) can be interpreted as a measure of the relevance of epistemic uncertainties on top of aleatory uncertainties. In this sense, it can be noted that for the case study developed, epistemic uncertainty on the future occurrence of discharge events seems to be more impactful than uncertainty on the inundation model parameters; at least for return periods of 100 years and above.

Developing uncertainty bounds for the hazard curve estimates is the typical way of showing the sensitivity of the hazard estimates on the model's parameters, and their overall relevance. This was done for the hazard curve of discharges in Figure 6. Doing the same for the flood depths would require to compute a hazard curve for each posterior sample of parameters with the

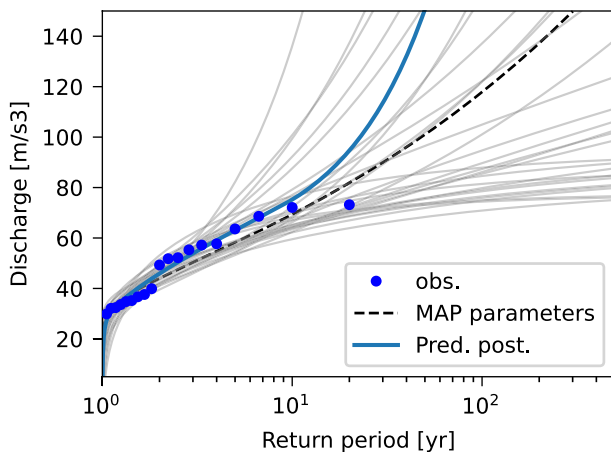


Figure 12. Hazard curves for discharges using the AM approach and a GEV distribution.

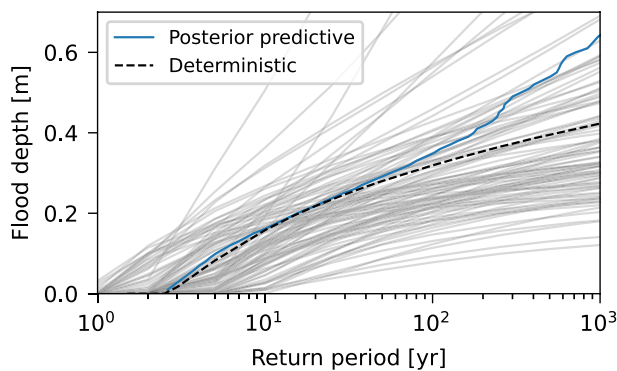


Figure 13. Ensemble of posterior samples of the hazard curves for water depth at location $x = 1.30$ km, $y = 1.05$ km.

consequent added computational demand. An ensemble of 100 hazard curves was computed and is shown in Figure 13 together with the posterior predictive (i.e., the mean curve of the ensemble) and the deterministic hazard curve.

Figure 13 shows that uncertainty in the model's parameters can yield hazard curves that are vastly different from one another, resulting in large uncertainty bounds. This type of analysis can encourage modelers to obtain more data and/or refine the knowledge of the models used in order to reduce it.

5.4. On the Modeling Methodology

The inclusion of epistemic uncertainties in the computation of flood hazard result in a non-uniqueness of the parameters (and models eventually) used to compute the hazard curves. Thus, there is not a single discharge for a given return period, and there is not a single flood map for any given input

discharge. As a result, there is no direct translation between the discharge for a given return period and its corresponding flood map. The water depth for a given return period, as per Equation 19, has now contributions from all possible discharges which is a more accurate representation of knowledge (and uncertainty).

There are many methodologies to include this uncertainty in the modeling process, and we have chosen to rely on rigorous probabilistic modeling based on a Bayesian framework. The Bayesian methodology allows to consistently include modeler's knowledge and data from different sources into posterior estimates of probabilities. In particular, this work has limited the epistemic uncertainties to uncertainty over the parameters of some models appropriately chosen (i.e., the GPD model for the discharges and the Lisflood simulator for the inundation model), but further prior distributions can be set over different models without affecting the workflow of the method proposed.

Finally, other deeper sources of uncertainty cannot be discarded in risk analysis and include what Spiegelhalter and Riesch (2011) named “indeterminacy” and “ignorance.” The former are associated with known limitations in understanding and modeling ability, while the latter is associated with unknown limitations of understanding. Different approaches have been proposed to deal with epistemic uncertainties that are not fully quantifiable including these deeper sources of uncertainties; these were not treated in this work and the reader is referred to (Beven, 2014; Goldstein, 2011; Spiegelhalter & Riesch, 2011).

5.5. On the Computational Challenges

From a computational perspective, the inclusion of epistemic uncertainties via the Bayesian posterior predictive distribution of IMs means that we need to perform lots of simulations of the inundation model in order to compute the hazard curves. This contrasts with the traditional approach where we only need to run the inundation model once to obtain the 100 years flood hazard (see Section 2.3). Furthermore, the number of simulations needed grow with the return period according to Equation 20.

This can result in an unfeasible computational burden, particularly for very large return periods. Ongoing advances in computer technology, on the other hand, are producing faster computers that will make simulation approaches like the one proposed, easier to deal as time progresses. In this context, it is expected that this type of numerical analysis will become more common in future research.

In any case, it is also important the implementation of efficient simulation techniques in order to reduce the computational cost. There are mainly two families of techniques that can be implemented in order to reduce the computational time required to compute the desired probabilities: using a more efficient simulation algorithm that targets the desired return period faster, such as importance sampling (Zio, 2013); and making each run of the inundation model faster by using a statistical emulator (Jiang et al., 2020).

6. Conclusions

We propose and discuss, in this work, a methodology to compute flood hazard estimates that coherently includes epistemic uncertainty in model's parameters through the Bayesian predictive posterior estimates. The study aims to fill a gap in the research of uncertainty quantification in flood hazard assessments, by simultaneously considering uncertainty in the recurrence and inundation models' parameters while also providing a useful input for risk assessments.

Rather than computing probabilities for an uncertain T-yrs peak discharge event, we propose to compute the flood depth distributions from all possible events within a given time-frame. The posterior distribution of the models' parameters were computed to include epistemic uncertainty, and the average recurrence-rate over these distributions (i.e., predictive posterior distribution) was used as a point estimate for the hazard. As a result, the flood hazard maps developed provide information related to the water-depths for different recurrence rates (or return periods) that can be readily used for further damage analysis including the forward propagation of epistemic uncertainties. The mathematical notation was kept intentionally generic to encourage its use in other natural hazards applications.

The results of the real-world case study developed, showed significant differences between the hazard estimates considering epistemic uncertainties and the classical ones without. In particular, the results showed that not considering epistemic uncertainties might underestimate the water-depths hazard at any point in the region of analysis, resulting in less reliable decisions and designs. Furthermore, this tendency aggravates with larger return periods, that tend to be the main focus in risk analysis. A deeper analysis shows that uncertainty in the prediction of future discharges as a product of a short-length observation series, is the main driver responsible for the underestimation in flood hazard. A similar pattern can be observed in the recurrence curves for the peak discharges in line with some results from the literature (Fawcett & Green, 2018; Merz & Thielen, 2005; Romanowicz & Kiczko, 2016).

On the other hand, the influence of the uncertainty in the inundation model parameters (i.e., floodplain and channel roughness) proved to be less significant. Results show that this uncertainty seems to have a constant effect over return periods, toward the conservative side; that is, it yields lower hazard values than using the classical approach. This seemingly non-intuitive influence requires further studies to understand how it generalizes to different applications and contexts (i.e., different calibration approaches, different computational simulators, different available data), although a potential explanation is the highly skewed shape of the posterior distribution (see Figure 7) relative to the MAP parameters used in the classical approach.

On the computational aspects, the proposed numerical methodology requires the simulation of thousands of inundation maps. This ensemble can be straightforwardly used in spatially distributed vulnerability models covering a continuous range of return periods. It comes at the expense, however, of a much larger computational burden than the classical approach where only a few runs for selected return periods are needed. Technological advances are expected to rapidly reduce the development-time of this simulation approach, particularly in applications that are practically feasible today. Additionally, this should also encourage researchers to find ways of optimizing the computation of the estimates by using more efficient sampling algorithms or cheaper emulators of the inundation model.

Overall, we have gone through the computational details to compute the predictive posterior estimates of water depths, and discussed its use a single hazard estimate that includes epistemic uncertainties. We have shown that the inclusion of these uncertainties can significantly affect the hazard estimates, and that the specific methodology for uncertainty quantification of the model's parameters can also be a relevant factor on the final estimates. Finally, this work has not intended to compare different uncertainty quantification methodologies or to provide an exhaustive review of uncertainty sources, but rather to provide a framework on which to include them and discuss how they can potentially affect decision-making. The results from this study will, hopefully, advocate for a more comprehensive and coherent consideration of epistemic uncertainties in hazard assessments.

Appendix A: The GPD Distribution

This appendix summarizes the probability functions for the Generalized Pareto Distribution (GPD), to avoid confusion in the definition and meaning of the parameters used.

$$p(x|\xi, \sigma) = \begin{cases} \left(1 + \frac{\xi}{\sigma}y\right)^{-\frac{\xi+1}{\sigma}}, & \text{if } \xi \neq 0 \\ \exp\left(-\frac{y}{\sigma}\right), & \text{if } \xi = 0 \end{cases} \quad (\text{A1})$$

$$F(x|\xi, \sigma) = \begin{cases} 1 - \left(1 + \frac{\xi}{\sigma}y\right)^{-1/\xi}, & \text{if } \xi \neq 0 \\ 1 - \exp\left(-\frac{y}{\sigma}\right), & \text{if } \xi = 0 \end{cases} \quad (\text{A2})$$

where the support of X is $x \geq 0$ when $\xi \geq 0$, and $0 \leq x \leq -\sigma/\xi$ when $\xi < 0$.

Return levels x_{Tr} for this distribution can be computed from,

$$Tr = \frac{1}{1 - F(x_{Tr}|\xi, \sigma)} \quad (\text{A3})$$

Data Availability Statement

All the data used as input in this work (DEM, daily discharge series, flood extent observation) is publicly available and the sources were mentioned in the manuscript. The open-source software Lisflood-fp was used as inundation simulator (<http://www.bristol.ac.uk/geography/research/hydrology/models/lisflood/>). All the simulations and figures were performed Python 3.X (<https://www.python.org/>) scripts developed by the authors. All the code used to develop the results and figures mentioned in this manuscript, as well as the input data and the Lisflood-fp binaries used, are publicly available in a Zenodo repository at DOI: <https://doi.org/10.5281/zenodo.8336368> (Balbi, 2023).

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