

Ultrafast Charge Transfer and Recombination Dynamics in Monolayer-Multilayer WSe₂ Junctions Revealed by Time-Resolved Photoemission Electron Microscopy

Ce Xu,¹ Natalie Barden,¹ Evgeny M. Alexeev,² Xiaoli Wang,³ Run Long,³ Alisson R. Cadore,² Ioannis Paradisanos,² Anna K. Ott,² Giancarlo Soavi,^{2,4} Sefaattin Tongay,⁵ Giulio Cerullo,^{6,7} Andrea C. Ferrari,^{2,} Oleg V. Prezhdo,^{8,*} and Zhi-Heng Loh^{1,*}*

¹ School of Chemistry, Chemical Engineering and Biotechnology, and School of Physical and Mathematical Sciences, Nanyang Technological University, Singapore 637371, Singapore

² Cambridge Graphene Centre, University of Cambridge, Cambridge CB3 0FA, UK

³ College of Chemistry, Key Laboratory of Theoretical and Computational Photochemistry, Beijing Normal University, Beijing 100875, People's Republic of China

⁴ Institute of Solid State Physics, Friedrich Schiller University Jena, Max-Wien-Platz 1, 07743, Jena, Germany

⁵ School for Engineering of Matter, Transport and Energy, Arizona State University, Tempe, Arizona 85287, United States

⁶ Department of Physics, Politecnico di Milano, Piazza Leonardo da Vinci 32, I-20133 Milano, Italy

⁷ IFN-CNR, Piazza Leonardo da Vinci 32, I-20133, Milano, Italy

⁸ Department of Chemistry, University of Southern California, Los Angeles, California 90089, United States

* Corresponding authors e-mail: acf26@cam.ac.uk (A.C.F.), prezhdo@usc.edu (O.V.P.), zhiheng@ntu.edu.sg (Z.-H.L.)

Abstract

The ultrafast carrier dynamics of junctions between two chemically identical, but electronically distinct, transition metal dichalcogenides (TMDs) remains largely unknown. Here, we employ time-resolved photoemission electron microscopy (TR-PEEM) to probe the ultrafast carrier dynamics of a monolayer-to-multilayer (1L-ML) WSe₂ junction. The TR-PEEM signals recorded for the individual components of the junction reveal the sub-ps carrier cooling dynamics of 1L- and 7L-WSe₂, as well as few-ps exciton-exciton annihilation occurring on 1L-WSe₂. We observe ultrafast interfacial hole (h) transfer from 1L to 7L-WSe₂ on a ~ 0.2 -ps timescale. The resultant excess h density in 7L-WSe₂ decays by carrier recombination across the junction interface on a ~ 100 -ps timescale. Reminiscent of the behavior at a depletion region, the TR-PEEM image reveals the h density accumulation on the 7L-WSe₂ interface, with a decay length $\sim 0.60 \pm 0.17 \mu\text{m}$. These charge transfer and recombination dynamics are in agreement with *ab Initio* molecular dynamics. The computed orbital densities reveal that charge transfer occurs from the basal plane, which extends over both 1L and ML regions, to the upper plane localized on the ML region. This mode of charge transfer is distinctive to chemically homogeneous junctions of layered materials and constitutes an additional carrier deactivation pathway that should be considered in studies of 1L-TMDs found alongside their ML, a common occurrence in exfoliated samples.

Keywords: transition metal dichalcogenides, lateral junction, interfacial charge transfer, time-resolved photoemission electron microscopy, ultrafast spectroscopy, nonadiabatic *ab initio* molecular dynamics

Layered materials (LMs) are at the center of an ever-expanding research effort.¹⁻⁷ Numerous electronic¹⁻⁵ and optoelectronic^{1,3,6,7} properties have been uncovered in semiconducting transition metal dichalcogenides (TMDs), such as layer-sensitive electronic structures,⁸⁻¹⁰ high carrier mobilities ($\sim 10^1 - 10^3 \text{ cm}^2 \cdot \text{V} \cdot \text{s}^{-1}$),¹¹⁻¹³ superconductivity,^{14,15} large exciton binding energies (hundreds meV)¹⁶⁻¹⁹, nonlinear optical response [$\chi^{(2)} \sim 10^{-12} \text{ m} \cdot \text{V}^{-1}$, $\chi^{(3)} \sim 10^{-17} - 10^{-19} \text{ m}^2 \cdot \text{V}^{-2}$],²⁰⁻²⁴ and optical properties dominated by excitonic transitions.^{16-19,25-29} Along with the ability to fabricate TMDs on wafer-scale,³⁰⁻³² these allow the realization of ultrathin nanoelectronic⁵ and optoelectronic devices,⁶ with with diverse applications, such as transistors,¹¹⁻¹³ photodetectors,^{7,33-35} and electroluminescent devices.³⁶⁻³⁹

Layered materials heterostructures (LMHs) comprising two chemically distinct TMDs juxtaposed either vertically or laterally have also been prepared.^{31,40} Extensive experimental⁴¹⁻⁴⁴ and theoretical⁴⁵ studies revealed photoresponse^{7,46} and photovoltaic response,^{47,48} high ($>10^5$) field-effect ON/OFF ratio,⁴⁹ and rectification,⁵⁰ as well as intra- and interlayer excitonic physics.⁵¹⁻⁵⁵ The behavior of carriers at heterojunctions is dictated by the band alignment of the two TMD components.⁵⁶⁻⁵⁸ In the case of type-I band alignment, with valence band maximum (VBM) and conduction band minimum (CBM) in the same layer,⁵⁹ both electrons (e) and holes (h) transfer to the same TMD, thereby supporting applications that require radiative recombination, such as light-emitting diodes.³⁸ In the case of type-II band alignment, with VBM and CBM in different layers,⁵³ photocarriers undergo charge separation and transfer across these heterojunctions, giving rise to applications in photodetectors⁷ and photovoltaics.^{57,60} Investigations of type-II vertical LMHs by pump-probe spectroscopy revealed interlayer charge transfer within $\sim 50 \text{ fs}$.⁶¹⁻⁶⁷ Time-domain density functional theory and nonadiabatic molecular dynamics simulations suggest that the ultrafast interlayer charge transfer is facilitated by quantum coherence and e delocalization.⁶⁸

Electronic structure calculations reveal strong interlayer coupling at the Γ valley of the valence band (VB) and the Q valley of the conduction band (CB), suggesting that these mediate interlayer charge transfer.⁶⁹ For lateral LMHs, exciton transfer across a type-I 1L-MoS₂-1L-MoSe₂ heterojunction with a velocity⁷⁰ $\sim 10^4$ m·s⁻¹ and sub-ps e transfer across a type-II composition-graded 1L-WSe₂-1L-WSe₂ interface were reported.⁷¹

TMD junctions are a complement to LMHs.⁷²⁻⁷⁶ Unlike LMHs, a LM junction (LMJ) comprises the same material at the interface. However, the opposite sides of the interface exhibit distinct bandgaps⁷³⁻⁷⁵, tunable by varying phase,⁷⁷ doping,⁷⁸ substrate,⁷⁹ and number of layers, N .^{72,75,76,80,81} We refer to the LMJ between a single-layer (1L) and a multilayer (ML) LM as 1L-ML-LMJ. This can often be found in samples prepared by micro-mechanical cleavage (MC) of bulk (B)-TMDs, in which different regions correspond to different N .^{72-74,80} The 1L region of a 1L-ML-LMJ composed of TMDs has a direct bandgap,^{82,83} whereas an indirect bandgap is present in the ML region.^{82,83} In the case of WSe₂, experimental^{80,81} and theoretical⁷⁵ studies found that juxtaposing 1L-WSe₂, which has a direct bandgap ~ 1.64 eV,⁸⁴ with ML-WSe₂, whose indirect bandgap evolves from 1.51 eV ($N = 2$) to 1.45 eV ($N \geq 4$),⁸⁴ yields an interface with a type-I band alignment.^{75,80,81} Measurements on a 1L-3L-MoS₂ LMJ by scanning photocurrent microscopy suggested type-II band alignment,⁷² whereas Kelvin probe force microscopy on a 1L-14L-MoS₂ LMJ pointed to type-I band alignment.⁸⁵

Compared to the extensive ultrafast spectroscopy studies performed to date on TMD LMHs,^{61-67,70,71} the ultrafast dynamics of 1L-ML-LMJs is, to the best of our knowledge, hitherto unexplored, mainly due to the need to combine sub-100-fs temporal- and sub-100-nm spatial resolution to study the dynamics at the interface. The typical μm -scale sizes of MC-TMDs⁸⁶ implies similar dimensions for 1L-ML-LMJs, therefore the need for an ultrafast spectroscopy

technique that can simultaneously allow μm to sub- μm resolution. Time-resolved photoemission electron microscopy (TR-PEEM) is complementary to ultrafast optical microscopy⁸⁷⁻⁸⁹ for investigating spatially resolved ultrafast phenomena. It can resolve the dynamics of trap states in B-semiconductors⁷¹ and perovskite thin films,^{90,91} image e motion in B-semiconductors⁹² and LMJs,⁹³ and reveal spatially heterogeneous ultrafast dynamics of TMDs.^{94,95}

Here, we use TR-PEEM to investigate the ultrafast e and h dynamics of a 1L–7L WSe₂ type-I LMJ. In addition to sub-ps carrier relaxation dynamics within the individual components, we observe a ~ 0.2 -ps h transfer, followed by ~ 100 -ps charge recombination, across the LMJ. We use nonadiabatic *ab Initio* molecular dynamics to calculate the time constants for h transfer and charge recombination, in agreement with experiments. Analysis of the PEEM images reveals the width of the depletion region at the 1L–7L-WSe₂ interface.

Results and Discussion

The LMJ is prepared as follows. B-WSe₂ crystals are grown by the flux zone method.¹⁶ These are exfoliated by MC on Nitto Denko tape,⁸⁶ then again on a polydimethylsiloxane (PDMS)⁹⁶ stamp placed on a glass slide for inspection under an optical microscope. Optical contrast⁹⁷ is optimized to identify 1L and 1L–7L-WSe₂ prior to transfer. The samples are then placed on 90-nm-SiO₂/Si at 40 °C using *xyz* micro-manipulators under an optical microscope, before increasing the temperature to 60 °C, so that they detach from PDMS and adhere preferably to SiO₂.⁹⁶

Figure 1a reveals regions of different N within the same flake. To characterize and identify N , we perform Raman spectroscopy and atomic force microscopy (AFM). Raman measurements are done with a Horiba LabRam Evolution system equipped with 1800 l/mm grating and volume Bragg filters with a cut-off frequency $\sim 5 \text{ cm}^{-1}$ at 532 nm, with a 100 \times objective (numerical aperture,

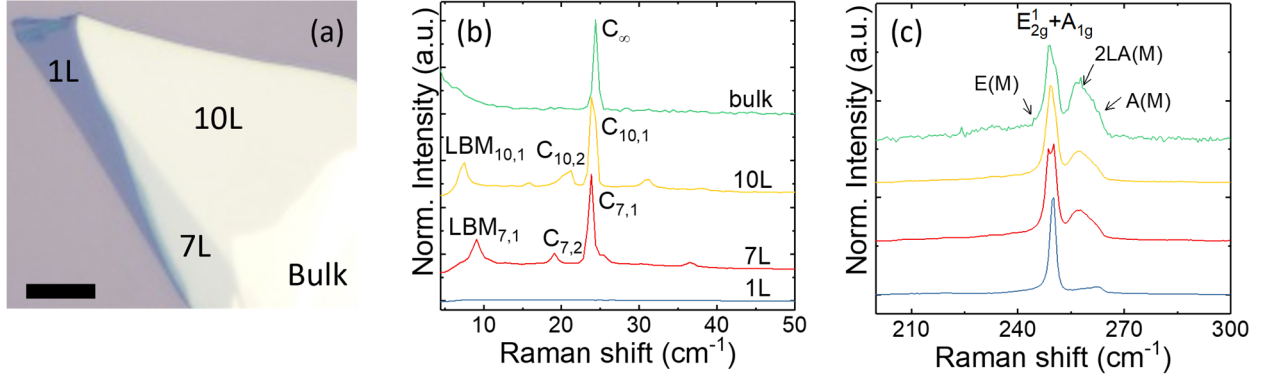


Figure 1. (a) Optical image of 1L-ML-WSe₂. Scale bar: 10 μ m. (b) Low-frequency and (c) high-frequency Raman spectra as a function of N at 532 nm excitation.

NA=0.9), resulting in a spot size $\sim 1\mu$ m. AFM measurements are performed with a Bruker Dimension Icon in tapping mode.

Figure 1b plots the low-frequency ($<50\text{ cm}^{-1}$) Raman spectra of the different regions of a WSe₂ flake, and of B-WSe₂. The Raman modes in this frequency range originate from relative motion of the layers and consequently are absent in 1L-WSe₂.⁹⁸⁻¹⁰² The shear modes (C) are due to the relative motions of the planes perpendicular to their normal,⁹⁸⁻¹⁰² while the layer breathing modes (LBM) are parallel to the normal.⁹⁸⁻¹⁰²

The position of the highest frequency C peak, $\text{Pos}(C_{N,1})$, can be used to derive N as:^{15,99}

$$N = \frac{\pi}{2 \cos^{-1}[\text{Pos}(C_{N,1})/\text{Pos}(C_{\infty})]}, \quad (1)$$

where $\text{Pos}(C)_{\infty}$ corresponds to B-WSe₂. Figure 1b gives $\text{Pos}(C)_{\infty} \sim 24.4 \pm 0.06\text{ cm}^{-1}$. The orange spectrum in Fig.1b has $\text{Pos}(C_{N,1}) \sim 24.0 \pm 0.06\text{ cm}^{-1}$. From Eq. 1 we get $N \sim 10 \pm 1$. The red spectrum in Fig.1b has $\text{Pos}(C_{N,1}) \sim 23.8 \pm 0.06\text{ cm}^{-1}$, thus $N \sim 7$. Fig.1b for $N = 7$ also shows one LBM at $\text{Pos}(\text{LBM}_{7,1}) \sim 9.1 \pm 0.06\text{ cm}^{-1}$ and an additional $\text{Pos}(C_{7,2}) \sim 19.1 \pm 0.06\text{ cm}^{-1}$, while for 10L-WSe₂ we have $\text{Pos}(\text{LBM}_{10,1}) \sim 7.5 \pm 0.06\text{ cm}^{-1}$ and $\text{Pos}(C_{10,2}) \sim 21.2 \pm 0.06\text{ cm}^{-1}$. In Methods we report a detailed discussion of the spectral fitting accuracy and its influence on N .

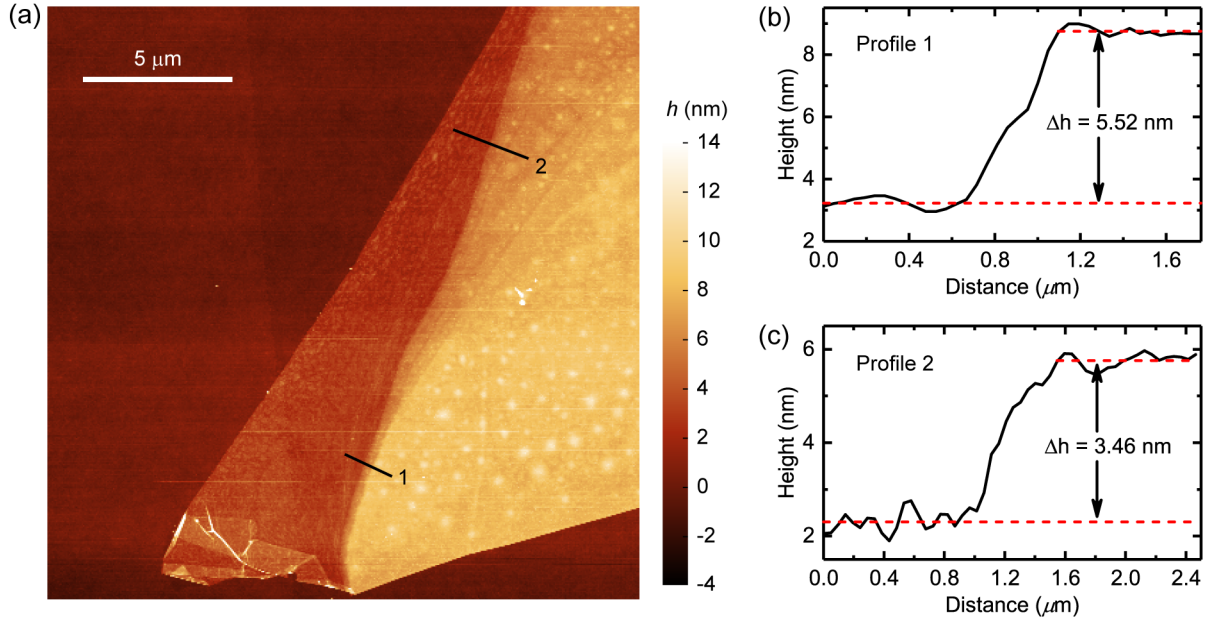


Figure 2. (a) AFM image of 1L-ML-WSe₂ LMJ. (b,c) Height profiles along (b) line 1 and (c) line 2 taken across the LMJ.

Fig.1c plots the high-frequency ($200 - 300 \text{ cm}^{-1}$) Raman spectra. For 1L-WSe₂, a single peak is observed $\sim 250 \text{ cm}^{-1}$, associated with the two degenerate, first-order A and E Raman modes.^{28,103-107} In B-WSe₂, the spectra show a split for the E_{2g}¹ and A_{1g} modes due to a red (blue) shift in the E_{2g}¹ (A_{1g}) mode with increasing N .¹⁰⁴⁻¹⁰⁶ The broad peak $\sim 260 \text{ cm}^{-1}$ can be deconvolved into 2LA(M) and A(M) bands.^{105,107} The 2LA(M) mode at $\sim 262 \text{ cm}^{-1}$ corresponds to the overtone of the LA phonon branch at the M point of the Brillouin zone (BZ),^{105,107} whereas the A(M) mode $\sim 258 \text{ cm}^{-1}$ corresponds to A-symmetry optical branch at the M point of the BZ.^{105,107} The E(M) mode $\sim 242 \text{ cm}^{-1}$ creates an asymmetry in the lower energy shoulder of E_{2g}¹+A_{1g}.^{105,107} This mode red shifts with increasing N .¹⁰⁴⁻¹⁰⁶

Fig.2a is an AFM image of the 1L-ML-WSe₂ LMJ. The line profiles taken in two different parts of the LMJ (Figs.2b,c) show that the ML regions are predominantly $N \sim 10$ (profile 1) and $N \sim 7$ (profile 2), consistent with the Raman estimate, separated from the $\sim 1\text{L}$ region by a sub- μm -wide $N \sim 6$ strip. For the estimation of N , we consider a 1L-WSe₂ thickness $\sim 0.6 \text{ nm}$.³¹ As the peak

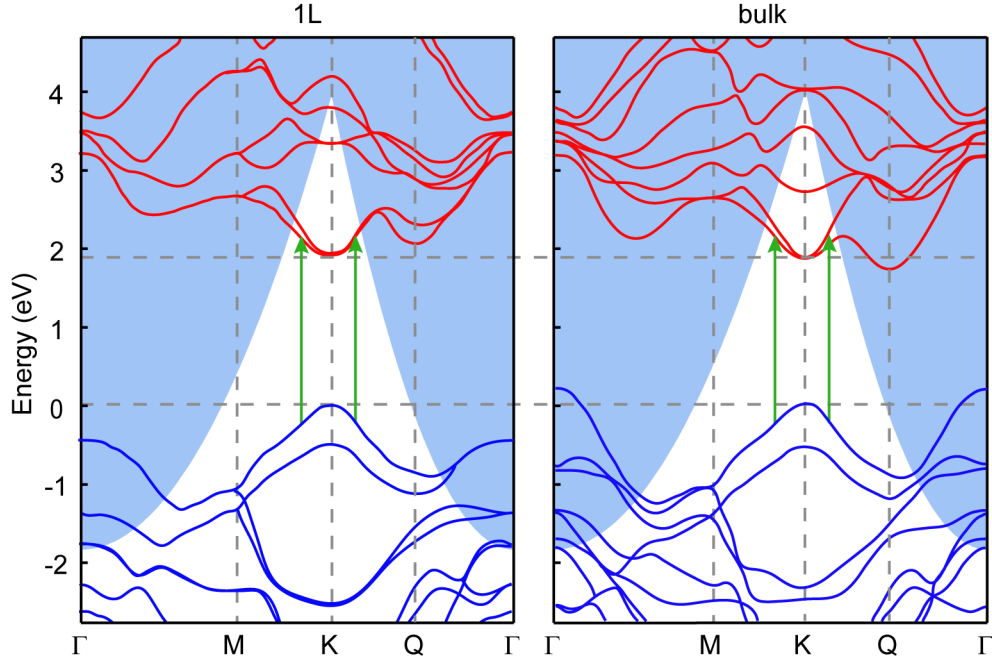


Figure 3. Band structures of 1L- and bulk B-WSe₂ from Ref.108. B-WSe₂ serves as a model for the 6–10L-WSe₂ regions. The 1L–7L WSe₂ LMJ has type-I band alignment, with CBM and VBM residing on 7L-WSe₂. The blue regions are the two-photon probe windows, as required by in-plane momentum conservation, within which photoemission occurs.

positions of the indirect band gap transitions in the photoluminescence (PL) spectrum of ML-WSe₂ remain unchanged within ~ 1 meV for $N \gtrsim 5$,^{8,84} we do not differentiate the 6,7,10L regions in our subsequent analysis, and we refer to these collectively as 6–10L.

Our TR-PEEM setup employs 2.41-eV (515-nm) pump and 3.61-eV (343-nm) probe pulses, with an instrumental response function (IRF) full width at half maximum (FWHM) ~ 55 fs. The fluences of the pump and probe pulses are 14 and 1 $\mu\text{J}\cdot\text{cm}^{-2}$, respectively. Fluence-dependent measurements indicate that pump and probe interactions with the sample involve one and two photons, respectively (see Supporting Information). According to the band structures of 1L- and B-WSe₂ (Fig.3),¹⁰⁸ the latter being a model for 6–10L-WSe₂, photoexcitation at 2.41 eV is a one-photon process at the K valley. Due to the need to conserve lateral momentum in photoemission, the K valleys of 1L- and B-WSe₂ lie beyond the two-photon UV probe window. The probe

windows in Fig.3 are calculated based on ionization potentials of 5.38 and 4.98 eV for 1L- and B-WSe₂, respectively.¹⁰⁹ Therefore, the dynamics of the K valley does not contribute to the PEEM signal. Instead, this originates from Q valleys,⁹⁴ which reside within the probe window. Following above band-gap photoexcitation of 1L-WSe₂ near the K valley, e scatter to the Q valley by carrier thermalization. This process, previously shown to occur on the ~10-fs timescale in TMDs,¹¹⁰ takes place within our IRF FWHM, and leads to the initial population of the conduction band Q valley. The build-up of e population in the Q valley ceases after carrier thermalization is completed on the ~10-fs timescale.¹¹⁰ As a result of the well-defined probe window (Fig.3) and the restricted regions in the first BZ to which carriers can flow following photoexcitation, energy and/or momentum filtering are not required and not critical for the interpretation of the observed dynamics. The use of two-photon UV probing^{94,111} yields dynamics in regions of k space otherwise inaccessible via a one-photon probe.¹¹²

The interaction with the UV probe at 3.61 eV must be a two-photon process, since one-photon probing does not access the region of the conduction band within which the photoexcited e resides (see Supporting Information). The Q valley lies within the probe window, and can be populated within the width of the IRF by intervalley scattering on a ~10fs timescale,¹¹⁰ as explained in the Supporting Information. For 7L-WSe₂, the VBM at the Γ point also lies within the probe window and can therefore contribute to the PEEM signal.

The sub-80-nm spatial resolution of our TR-PEEM^{94,95} is well-suited for resolving the carrier dynamics of 1–7L-WSe₂ LMJ. The TR-PEEM image acquired at 0 fs time delay (Fig.4a) shows that the signal for 1L-WSe₂ is ~50% larger than 7L-WSe₂. This is consistent with the previously reported non-monotonic change in the PEEM intensity as a function of layer number, N , attributed to abrupt changes in the UV photoionization cross-section with N .¹¹³ To investigate the ultrafast

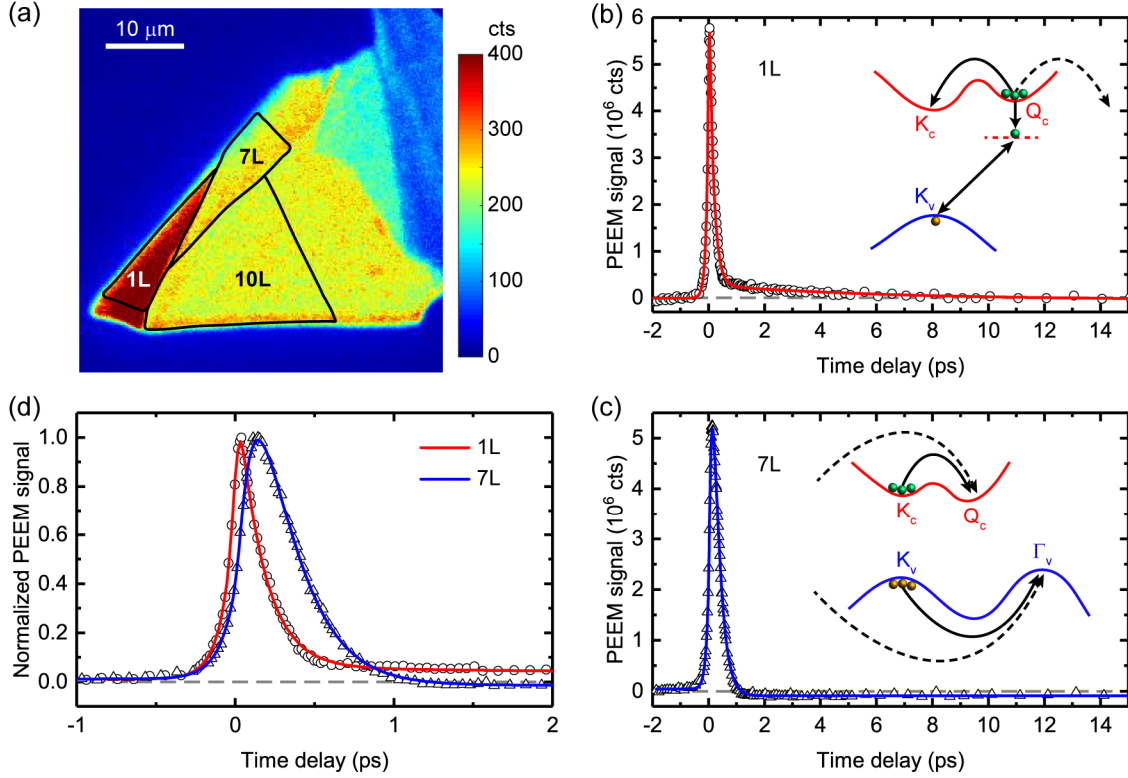


Figure 4. (a) PEEM image of 1L-ML-WSe₂ at 0 fs time delay. (b) Spatially integrated time-dependent PEEM signal from 1L-WSe₂. The inset shows e cooling, dark exciton formation and subsequent exciton-exciton annihilation within 1L-WSe₂, which leads to the bi-exponential decay. Interfacial e transfer to ML-WSe₂ (dashed line) is energetically possible, but not observed. (c) Spatially integrated time-dependent PEEM signal from 7L-WSe₂. The inset shows pathways for e and h cooling within 7L-WSe₂, as well as interfacial charge transfer from 1L-WSe₂ (dashed lines). The exponential rise and decay of the PEEM signal are assigned to e cooling and interfacial h transfer, respectively. (d) Magnified view of normalized time traces of 1L- and 7L-WSe₂ regions at short (<2 ps) time delays. At negative time delays the UV probe arrives at the sample before the pump. The grey dashed line in (b–d) mark the zero baseline.

dynamics of the LMJ, we measure spatially integrated time-dependent PEEM from 1L-WSe₂ (Fig.4b) and 7L-WSe₂ (Fig.4c), with pump and probe fluences of 14 and 1 $\mu\text{J}\cdot\text{cm}^{-2}$, respectively.

TR-PEEM of 1L-WSe₂ exhibits a bi-exponential decay, with time constants $\tau_1^{1L} = 0.16 \pm 0.01$ ps and $\tau_2^{1L} = 5.13 \pm 0.97$ ps, and an amplitude ratio $A_1^{1L}/A_2^{1L} = 24.9 \pm 2.4$. For 7L-WSe₂, TR-

PEEM shows a delayed rise followed by a decay, with $\tau_r^{7L} = 0.11 \pm 0.01$ ps and $\tau_d^{7L} = 0.22 \pm 0.01$ ps, respectively (Fig.4d). The decay is followed by a weak, long-lived negative offset, due to the generation of excess h in 7L-WSe₂. The peak of the 1L-WSe₂ signal (Fig.4d) is delayed~31fs relative to time-zero. However, this does not reflect the finite time for intervalley e scattering from K to Q valley, estimated to occur with a time constant of 16 ± 5 fs.¹¹⁴ Instead, it arises from the finite IRF FWHM~54fs, obtained from the global fit. This is consistent with Ref.115, which showed that K and Q valleys are simultaneously populated by above-band-gap, 2.48-eV photoexcitation.¹¹⁵ Our ~50-fs time resolution does not allow the timescale for K to Q intervalley scattering to be precisely determined, since it occurs within our temporal resolution. On the other hand, the delay in the peak of the 7L-WSe₂ signal can be ascribed to the ~0.1-ps K to Q intervalley e scattering (see below).

Following our previous TR-PEEM investigation of CVD-grown 1L-WSe₂,⁹⁴ we assign τ_1^{1L} to depopulation of the Q valley, based on intervalley scattering to the K valley being energetically favorable (Fig.3), and τ_2^{1L} to exciton-exciton annihilation, based on the observed acceleration of the annihilation process with higher excitation density.^{116,117} Note that the PEEM signal does not decay completely on the sub-ps timescale. At 500-fs time delay, it is still ~10% of the peak signal. Hence, after initial e cooling on the timescale of τ_1^{1L} , there exists a small, but non-negligible, residual population in the Q valley, suggestive of dark exciton formation.^{115,118} The observed dynamics differ from previous works that employed resonant excitation of the A exciton transition,^{114,115} which reveal exciton dynamics that evolve on the ps timescale.^{114,115} Our experiments employ above-band-gap excitation at 2.41 eV, where free carriers dominate the initial ultrafast dynamics. We now consider the various possible pathways by which e can leave the conduction band Q valley of 1L-WSe₂; control experiments performed on an isolated 1L-WSe₂

flake (see below) are then used to eliminate some of these pathways. First, since the K valley is lower than the Q valley in the conduction band of 1L-WSe₂,^{108,119,120} carrier cooling via intervalley scattering²⁸ leads to the transfer of e population from the Q valley to the K valley. Second, Q valley e can transfer across the LMJ interface to the lower-lying Q valley of 7L-WSe₂. Third, they can form dark excitons,^{115,118} comprising Q valley e and K valley h (VBM), where e and h have different momenta, therefore cannot undergo radiative recombination. The observed ~0.3-ps delay, assigned to indirect exciton formation following above-band-gap excitation of 1L-WSe₂,¹¹⁵ is consistent with our τ_1^{1L} . These dark excitons, which reside in the probe window and have non-vanishing momenta, can subsequently undergo exciton-exciton annihilation,¹¹⁸ thereby resulting in the observed few-ps decay. A similar Auger-mediated annihilation dynamics of dark excitons in 1L-WSe₂ was identified by time-resolved mid-infrared (~6–9 μm) probing of intra-excitonic transitions.¹¹⁸ Global fitting of the time traces at different excitation fluences (11 – 21 $\mu\text{J}\cdot\text{cm}^{-2}$) yields an annihilation rate constant $\gamma = 0.46 \pm 0.02 \text{ cm}^2\cdot\text{s}^{-1}$ (see Supporting Information for details), consistent with $\gamma \sim 0.35 \text{ cm}^2\cdot\text{s}^{-1}$ obtained from a combination of PL spectroscopy and Monte-Carlo simulations of 1L-WSe₂,¹²¹ and with those obtained from time-resolved optical microscopy for 1L-MoSe₂ ($0.33 \pm 0.06 \text{ cm}^2\cdot\text{s}^{-1}$)¹²² and 1L-WSe₂ ($0.41 \pm 0.02 \text{ cm}^2\cdot\text{s}^{-1}$).¹¹⁶

To understand the temporal behavior of the TR-PEEM signal for 7L-WSe₂ (Fig.4c), we first note that CBM and VBM of ML-WSe₂, located at the Q and Γ valleys, respectively, both reside within the probe window (Fig.3). The Q valley is located 150 meV below the K valley in the CB, while the Γ valley lies 180 meV above the K valley in the VB.¹⁰⁸ Photoexcitation of 7L-WSe₂ at 2.41 eV occurs in the vicinity of the K valley, and is followed by carrier cooling, channeling e from K to Q valley (CBM), and h from K to Γ (VBM). Since the acquisition of TR-PEEM images involves referencing to the PEEM image collected with long (250 ps) temporal separation of the

pump and probe pulses (see Methods), the appearance of e (h) in the probe window leads to a rise (decay) of the TR-PEEM signal. The 7L-WSe₂ signal also indicates charge transfer across the 1L–7L-WSe₂ interface. Since CBM and VBM of 7L-WSe₂ both reside in the probe window, e (h) transfer would result in the appearance of excess e (h) in 7L-WSe₂, in turn giving rise to a positive (negative) offset in the TR-PEEM signal. Fig.4c shows a negative baseline offset at time delays >1 ps, suggesting the presence of sub-ps h transfer across the LMJ. According to scanning tunneling spectroscopy, the VB offset between 1L- and 2L-WSe₂ is 0.12 eV,⁸⁰ thus making h transfer from 1L- to ML-WSe₂ energetically favorable. As such, we assign the $\tau_d^{7L} \sim 0.22$ ps component to h transfer. On the other hand, we attribute $\tau_r^{7L} \sim 0.11$ ps to e cooling via K \rightarrow Q intervalley scattering, slower than that for 1L-WSe₂. We note that Ref.123 analyzed the temperature-dependent optical reflectance of 1L- and 2L-WS₂ to extract their homogeneous linewidths. Their results suggest enhanced exciton-phonon scattering in 2L-WS₂ compared to 1L-WS₂. However, homogeneous linewidths give optical dephasing times,¹²⁴ and do not directly probe the intervalley scattering timescales.¹²⁵ A more direct comparison of K to Q intervalley scattering times can be obtained from time- and angle-resolved photoemission spectroscopy measurements of 1L-WSe₂¹¹⁵ and B-WSe₂.¹²⁶ While photoexcitation of 1L-WSe₂ does not reveal any noticeable delay between the population of the K and Q valleys,¹¹⁵ photoexcitation of B-WSe₂ yields a delayed appearance of the Q valley, with its population peaking ~ 0.2 ps after photoexcitation, from which an intervalley scattering timescale $\sim 70 \pm 15$ fs was inferred.¹²⁶ These results are consistent with ours, which suggest a more rapid K to Q intervalley scattering for 1L-WSe₂ than 7L-WSe₂. The few-ps decay observed in 1L-WSe₂, assigned to exciton-exciton annihilation,⁹⁴ is absent because the small exciton binding energies of B-TMDs, typically on the order of 10 meV,¹²⁶⁻¹²⁸ do not support stable excitons in 7L-WSe₂ at room temperature.

Note that the negative offset in Figs.4c,d, assigned to h transfer, could also potentially be due to matrix elements effects,¹²⁹ causing the photoionization cross-section to be larger for the CB Q valley than the VB Γ valley. To verify the occurrence of ultrafast h transfer and to elucidate possible ultrafast e- and/or exciton transfer across the 1L–7L WSe₂ interface, we perform TR-PEEM on an isolated 1L-WSe₂ flake under identical experimental conditions (see Supporting Information). This cannot exhibit any charge or energy transfer dynamics. Its TR-PEEM time trace, shown in the Supporting Information, can be fit to a bi-exponential decay, with a fast $\tau_1^{1L} = 0.13 \pm 0.01$ ps, a slow $\tau_2^{1L} = 3.28 \pm 0.10$ ps, and $A_1^{1L}/A_2^{1L} = 9.0 \pm 0.4$. As for the 1L-WSe₂ in our LMJ, the fast and slow decays are attributed to e leaving the Q valley and exciton-exciton annihilation, respectively. Global fitting of the slow decay component at different excitation fluences yields $\gamma \sim 0.30 \pm 0.04$ cm²·s⁻¹ (see Supporting Information). The nearly identical τ_1^{1L} for both isolated 1L-WSe₂ and that in the LMJ rules out e transfer as an additional deactivation pathway for the Q valley e of 1L-WSe₂ in our LMJ. Compared with isolated 1L-WSe₂, the slower exciton population decay τ_2^{1L} of the 1L-WSe₂ in our LMJ excludes the possibility of ultrafast exciton transfer occurring at the 1L–7L-WSe₂ LMJ, which would accelerate the decay of the exciton component of the TR-PEEM signal. Instead, the slower exciton population decay of 1L-WSe₂ in our LMJ is consistent with ultrafast h transfer depleting the initial density of dark excitons, hence decelerating exciton-exciton annihilation.¹¹⁶ A lower initial exciton density also reduces the relative contribution of exciton-exciton annihilation to the overall PEEM signal, thereby accounting for the larger A_1^{1L}/A_2^{1L} for 1L-WSe₂ in our LMJ. Comparing A_1^{1L}/A_2^{1L} for LMJ and the isolated flake, we find that the initial exciton density in the LMJ is ~40 % that of the isolated flake. A similar reduction in the initial exciton density is obtained when one considers the measured τ_2^{1L} and γ for both samples (see Supporting Information). Our interpretation that the observed negative offset in the 7L region

of 1L-7L-WSe₂ arises from interfacial h transfer is consistent with a previous time-resolved photoemission study of bulk-WSe₂,¹²⁶ which did not observe the 0.22-ps decay component that we ascribe to h transfer. Instead, the dynamics reported in Ref. 126 are dominated by a long-lived (tens of ps) population of Q valley electrons. Our control experiment on an isolated 1L-WSe₂ flake (see Supporting Information) proves that e transfer across the 1L-7L-WSe₂ interface does not occur, thus allowing us to attribute any differences in the ps dynamics of excitons to h transfer giving rise to a lower initial exciton density.

The absence of exciton transfer across the interface, despite the type-I band alignment of our 1L-7L WSe₂ LMJ, can be rationalized in terms of the large exciton binding energy (0.37 eV)¹³⁰ of 1L-WSe₂, the vanishingly small exciton binding energy of 7L-WSe₂,¹²⁷ and the small VB and CB offsets at the 1L-7L-WSe₂ LMJ. These factors make exciton transfer energetically unfavorable. The apparent absence of interfacial e transfer requires further investigation. We note that exciton formation does not explain the absence of e transfer across the LMJ, since h transfer may also be similarly impeded. One possible explanation is that ultrafast K to Q intervalley e scattering within 7L-WSe₂, with $\tau_r^{7L} = 0.11 \pm 0.01$ ps, could inhibit e transfer by Pauli blocking. Given that e transfer is mediated by the strong interlayer coupling at the Q valley,⁶⁹ it is conceivable that the population of the Q valley of 7L-WSe₂ could inhibit e transfer across the LMJ.

The negative baseline offset that appears in the TR-PEEM time trace of 7L-WSe₂ in our LMJ (Fig.4c) points to the existence of a long-lived h population on 7L-WSe₂. Fig.5a shows the TR-PEEM images for pump-probe time delays >1 ps. Extending the pump-probe time delay to 250 ps shows that the negative offset decays with a time constant $\sim 108 \pm 9$ ps (Fig.5b), signaling the h disappearance from 7L-WSe₂ on this timescale. TR-PEEM is unable to detect carrier recombination within 7L-WSe₂ because both its VBM and CBM are within the probe window.

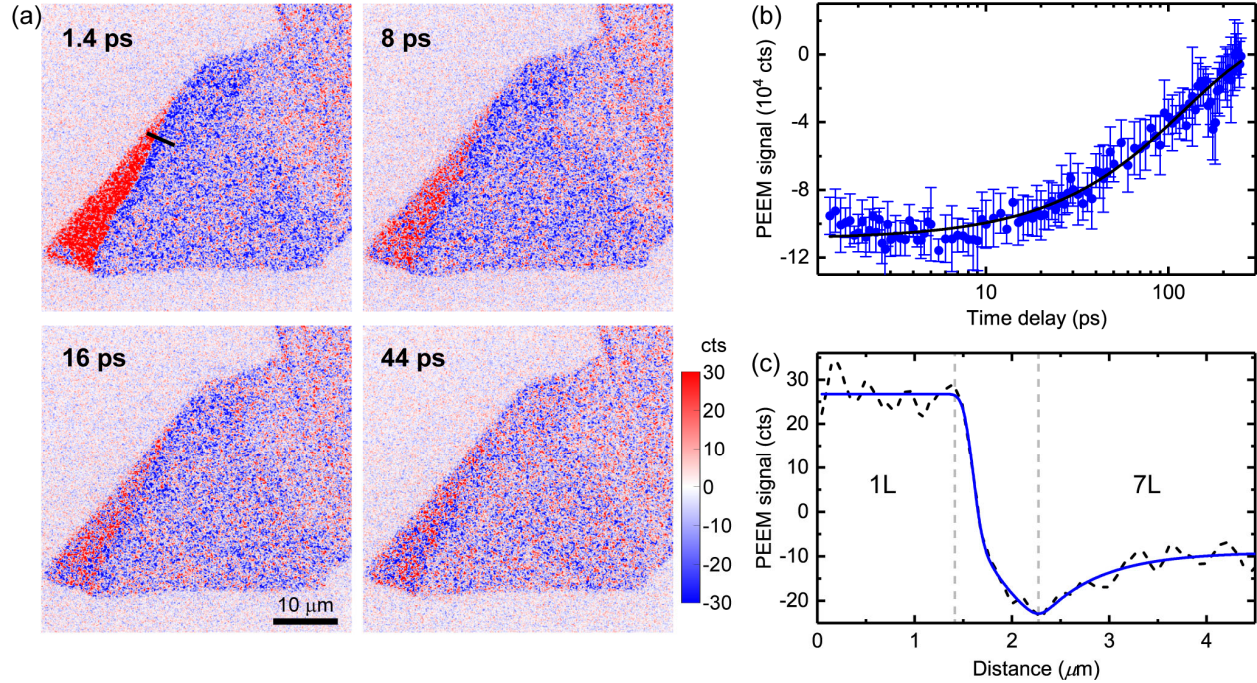


Figure 5. (a) Differential PEEM images with time delays from 1.4 to 44 ps. (b) Time trace of 7L-WSe₂ PEEM with pump-probe time delay up to 250 ps, undergoing an exponential decay. The black line shows the fit to a single exponential decay. (c) PEEM signal profile along the black line on the 1.4-ps image in (a). The PEEM signal changes from positive, in the 1L region, to negative in 7L, and has a rise within the 7L region fitted with an exponential function

The h disappearance from the probe window is thus attributed to carrier recombination across the 1L–7L junction. To the best of our knowledge, the interfacial carrier recombination times for TMD 1L–ML LMJs and lateral TMD LMJs were not previously reported. The ~100-ps recombination time is in the range observed for vertical TMD LMJs.^{61,64,131} Inspection of the TR-PEEM images collected for the 7L-WSe₂ region at >1-ps time delays, when carrier cooling no longer contributes to the signal, reveals h accumulation at the 1L–7L-WSe₂ interface (Fig.5a). The higher h density at the interface can also be seen from the lineout of the TR-PEEM signal (Fig.5c), which reveals a decrease in h density with distance from the 1L–7L-WSe₂ interface. This might be assigned to the depletion region that exists at the 1L–7L-WSe₂ interface. Fitting the h density distance dependence (see Supporting Information) suggests a depletion width $\sim 0.60 \pm 0.17 \mu\text{m}$,

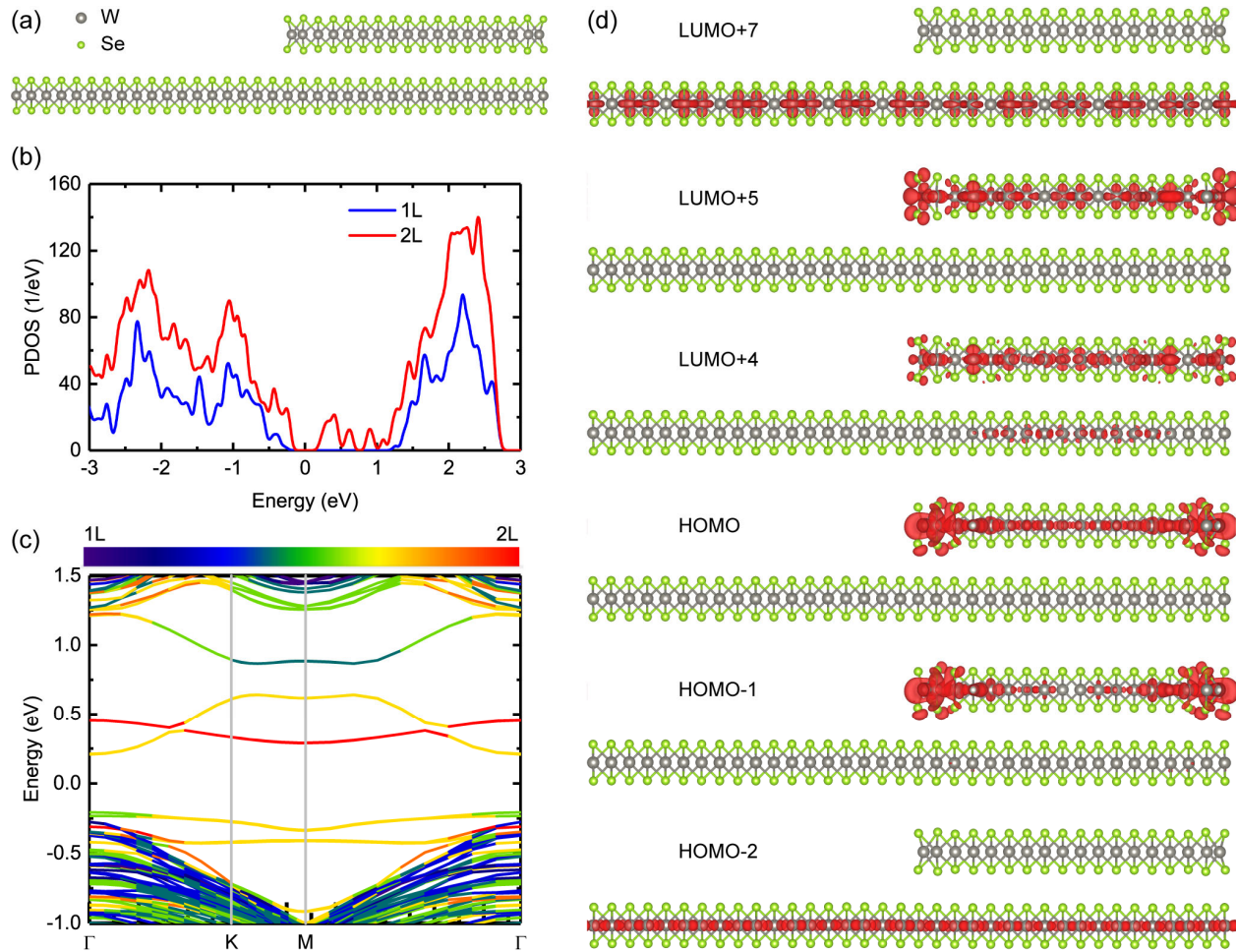


Figure 6. (a) Side view of optimized geometry of 1L–2L-WSe₂ LMJ. (b) Partial density of states and (c) band structure of 1L–2L-WSe₂. The states in the band gap represent edge states. The zero energy corresponds to E_F . The band structure is color coded to show the relative contributions of 1L and 2L regions to the individual bands. (d) Charge densities of the various states involved in the ultrafast dynamics at the 1L–2L-WSe₂ LMJ. The isosurface is set at $0.001 e/\text{\AA}^3$.

similar to the $0.32\mu\text{m}$ for 1L-WSe₂-1L-MoS₂ LMJ.¹³² The existence of a depletion region is consistent with h transfer across the LMJ, since it would not exist without excess carriers.¹³²

To get further insights on the ultrafast dynamics of our LMJ, we perform *ab Initio* quantum dynamics on a model 1L–2L-WSe₂ LMJ (Fig.6a, see Supporting Information for details). The 162-atom structure was previously used to study electronic properties of WSe₂ LMJs, exhibiting properties similar to those of structures with a larger N .⁷⁵ Including all 7 layers would make the

calculations prohibitively expensive computationally. The bottom 1L-WSe₂ contains 108 atoms periodically replicated in two-dimensions. To create a 2L-WSe₂, a second layer is added on half of the bottom 1L-WSe₂. Geometry optimization gives a Se···Se distance~3.36 Å between the two 1L-WSe₂, in agreement with Ref.75. The calculated density of e states and band structure for the model 1L–2L-WSe₂ LMJ are shown in Figures 6b and 6c, respectively. The charge densities of the key states involved in the excitation dynamics are in Fig.6d. The simulated system can be viewed either as a 108-atom bottom 1L-WSe₂ with a 54-atom top half-layer, or as a 54-atom 1L-WSe₂ on the left and a 108-atom 2L-WSe₂ on the right. Necessarily, the top half-layer contains edges, which create defect states inside the bandgap of 1L-2L-WSe₂. The defect states appear mid-gap (Fig.6b) and can be identified by the flat band dispersion (Fig.6c) as well as by their charge densities (see Supporting Information). Because the size of the top layer is large in experiments, on the order of ~1 μm (Fig.1a), the relative contribution of edges to the overall dynamics is likely insignificant. Therefore, the defect states created by edges are excluded in the simulations.

We simulate h and e dynamics to provide insights into why only interfacial h transfer is observed, without interfacial e transfer, even though both processes are energetically favourable. The simulated h and e dynamics are in Figs.7a,b, respectively. h transfer occurs from the top of the 1L-WSe₂ VB, represented by the HOMO–2 orbital, to the top of the 2L-WSe₂ VB region, represented by the HOMO (Fig.6d). The simulations give a time constant~339 fs for h transfer, in agreement with the measured $\tau_d^{7L} \sim 0.22$ ps. The transfer is ultrafast because it occurs through a dense manifold of VB states (Fig.6c). The average absolute nonadiabatic coupling between HOMO–2 and HOMO is 10.5 meV. The simulated time constant for h cooling within 2L-WSe₂ is 904 fs, ~3× longer than the interfacial h transfer time. Hence, h cooling might not be observed experimentally because it is outpaced by interfacial h transfer.

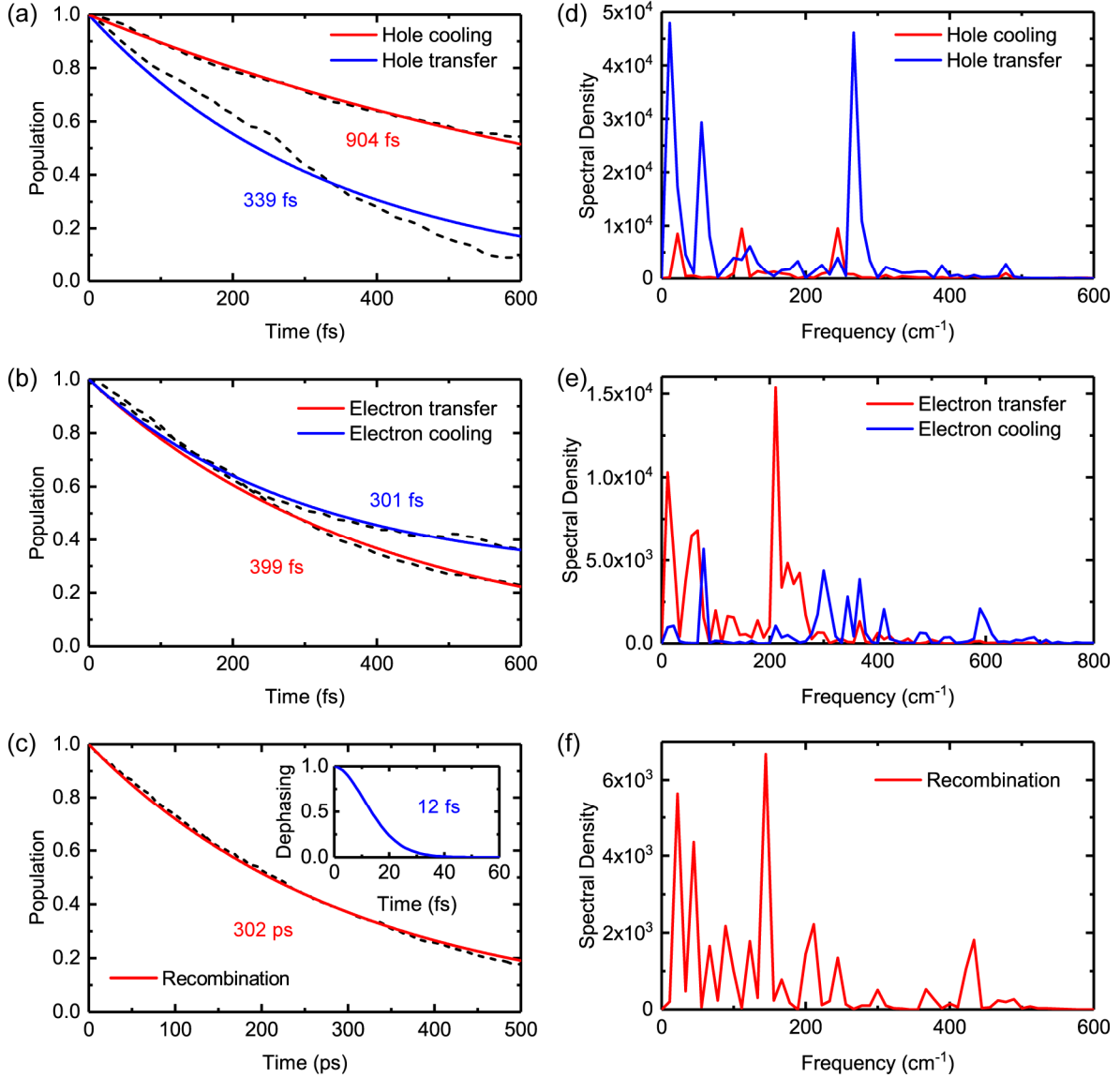


Figure 7. Simulated dynamics for (a) h transfer and cooling, (b) e transfer and cooling, (c) interfacial e-h recombination. Spectral densities characterizing phonon modes involved in the charge dynamics for (d) h transfer and cooling, (e) e transfer and cooling, (f) e-h recombination.

Beyond h transfer, the simulations also elucidate why interfacial e transfer is not observed, despite the type-I band alignment at the 1L-7L-WSe₂ interface. The simulated time constant for e transfer from the CBM of 1L-WSe₂ (LUMO+7 in Fig.6d) to the CBM of 2L-WSe₂ (LUMO+4) is 399 fs (Fig.7b), whereas that for e cooling within 2L-WSe₂ is 301 fs, i.e. $\sim 1.3\times$ faster than e transfer.

Thus, e transfer is suppressed at the expense of e cooling. Given that e transfer is mediated by the strong interlayer coupling at the Q valley,⁶⁹ it is conceivable that the population of the Q valley of 7L-WSe₂ by e cooling could inhibit e transfer across the LMJ.

To explain charge recombination being two orders of magnitude slower compared to interfacial h transfer, we model recombination across the 1L–7L-WSe₂ interface by considering the LUMO+7 and HOMO orbitals (Fig.6d), which correspond to the CBM of 1L-WSe₂ and the VBM of 2L-WSe₂, respectively. The simulations give a recombination time~302 ps (Fig.7c), consistent with the experimental~108 ps. Charge recombination is slower than charge transfer for several reasons. First, recombination occurs across a large energy gap (1.31 eV). Second, the nonadiabatic coupling between the orbitals that participate in charge recombination (1.35 meV) is one order of magnitude smaller than between the orbitals that participate in e (12.2 meV) and h (10.5 meV) transfer. Third, recombination involves a rapid 12-fs loss of quantum coherence (Fig.7c, inset), which slows down quantum dynamics. This is exemplified by the quantum Zeno effect,¹³³ whereby transitions stop completely if one attempts to measure continuously and precisely the quantum state of the system, giving rise to infinitely fast coherence loss.¹³³

The simulations also provide insights into the relative importance of carrier cooling vs. carrier transfer for e and h. The frequencies of the phonon modes that accommodate the excess energy lost by the electronic subsystem during these nonradiative processes are in Figs.7d,e for h and e transfer, respectively, and in Fig.7f for e-h recombination. These spectral densities are obtained as Fourier transforms of the phonon-induced fluctuations of the corresponding energy gaps. A higher intensity of a peak at a given frequency and the presence of multiple phonon modes favor stronger nonadiabatic coupling. Fig.7d shows that the intensity of major phonon modes for h transfer is ~5× larger than that for h cooling, leading to stronger nonadiabatic coupling, thus

faster h transfer. The situation changes for e dynamics. Even though the peaks are higher for e transfer than cooling, the difference is less pronounced. In addition, e cooling is promoted by several high frequency modes $\sim 300\text{--}400$ and 600 cm^{-1} , which do not participate in e transfer. As a result, e cooling is faster than e transfer (Fig.7b). The peak $\sim 267\text{ cm}^{-1}$, contributing strongly to the h transfer process, can be assigned to the 2LA(M) mode, observed at $\sim 260\text{ cm}^{-1}$ in the Raman spectra (Fig.1c). The frequencies $<250\text{ cm}^{-1}$ can be attributed to various transverse and longitudinal acoustic modes, shear modes, and their overtones or combinations. Long-wavelength acoustic modes influence charge wave functions over nanometer scales, facilitating charge transfer.^{68,95} Multiple vibrations contribute to the charge dynamics because the interface between 1L and ML regions breaks the symmetry and relaxes electron-phonon coupling selection rules for pristine systems. The electron-vibrational coupling matrix elements, $\langle i|\nabla_r|j\rangle$, for nonradiative charge transfer and recombination are different from the Raman matrix elements,¹³⁴ and have weaker selection rules, because optical spectra are determined by operators with high symmetries describing, e.g., linearly polarized light, while the gradients with respect to vibrational motions, ∇_r , represent many different symmetries. This fact rationalizes why more modes participate in the charge dynamics than the Raman spectra.

The salient experimental and theoretical observations are summarized below.

- (1) The sub-ps decay constants for the 1L-WSe₂ region of the 1L-7L-WSe₂ LMJ ($\tau_1^{1L} = 0.16 \pm 0.01\text{ ps}$) and for an isolated 1L-WSe₂ flake ($\tau_1^{1L} = 0.13 \pm 0.01\text{ ps}$) are similar. τ_1^{1L} is assigned to the depopulation of the Q valley in 1L-WSe₂. The similarity of τ_1^{1L} rules out sub-ps electron transfer from the 1L- to the 7L-WSe₂ region of the LMJ, which would accelerate the decay.
- (2) The few-ps decay of 1L-WSe₂ is slower for the 1L-7L-WSe₂ LMJ ($\tau_2^{1L} = 5.13 \pm 0.97\text{ ps}$) than for the isolated 1L-WSe₂ flake ($\tau_2^{1L} = 3.28 \pm 0.10\text{ ps}$). τ_2^{1L} is assigned to exciton-exciton

annihilation in 1L-WSe₂. The slower exciton-exciton annihilation for the LMJ than the isolated flake, according to second-order kinetics,^{116,117} is suggestive of the initial exciton density being lower in the LMJ than the isolated flake. Since e do not transfer from 1L- to 7L-WSe₂ in the LMJ, its lower initial exciton density suggests h transfer from 1L- to 7L-WSe₂.

- (3) The 7L-WSe₂ region of the LMJ exhibits an ultrafast decay ($\tau_d^{7L} = 0.22 \pm 0.01$ ps) and a long-lived, >100-ps negative offset. This implies h transfer because both CBM and VBM of 7L-WSe₂ reside in the probe window, such that the appearance of excess h in 7L-WSe₂ would yield a lower PEEM signal, resulting in a negative offset, that could also arise from matrix element effects.¹²⁹
- (4) Ab initio nonadiabatic molecular dynamics simulations on a 1L–2L-WSe₂ LMJ (used as a model for the experimental 1L–7L-WSe₂ LMJ) reveal that h transfer from 1L- to 2L-WSe₂ is $\sim 3\times$ faster than h cooling within 2L-WSe₂. Hence, we assign the ultrafast decay in the 7L-WSe₂ region to h transfer from 1L-WSe₂ instead of h cooling within 7L-WSe₂.
- (5) A section of the PEEM image normal to the 1L–7L-WSe₂ junction reveals a depletion region (Fig.5a). This, and the negative PEEM signal, imply h accumulation in the 7L-WSe₂ region. Note that a depletion region, by definition, requires the presence of excess carriers.¹³⁵

Conclusions

We studied the dynamics of photoexcited carriers at the 1L–7L-WSe₂ interface by using a combination of TR-PEEM and nonadiabatic *ab Initio* molecular dynamics. Since the low-energy, 7.22-eV two-photon photoionization probe provides a well-defined probe window and carriers can only flow to restricted regions of the first Brillouin zone, energy and/or momentum resolution are not required for the interpretation of the experimental results. Instead, interpretation of the observed ultrafast dynamics is based primarily on comparing the ultrafast dynamics of the 1L–7L-

WSe₂ LMJ sample to those of the isolated 1L-WSe₂ flake. The experimental and theoretical results, summarized above, suggest interfacial h transfer from 1L- to 7L-WSe₂ within the LMJ on a ~0.2-ps timescale. The resultant excess h density in 7L-WSe₂ eventually decays by carrier recombination across the 1L–7L-WSe₂ interface on a 100-ps timescale. The experimental timescales for interfacial h transfer and e-h recombination are consistent with *ab Initio* quantum dynamics simulations. These results suggest that ML regions alongside 1L ones can influence the ultrafast carrier dynamics of the latter. As such, analysis of time-resolved data should consider ultrafast charge transfer across the 1L–ML interface as an additional carrier deactivation pathway. Charge transfer does not occur in-plane, unlike lateral LMJs.^{70,71} Instead, as the charge density plots in Fig.6d suggest, h transfer involves the shift of h density from the basal plane (HOMO–2), extended over 1L and 2L regions, to the top plane (HOMO), localized on the 2L region. The interfacial charge transfer in 1L–7L-WSe₂ is thus more akin to that occurring in vertical LMJs, albeit with chemically identical bottom and top layers. Such a mode of charge transfer is distinctive to LMJs.

The e transfer dynamics of 1L-MoSe₂–1L-MoSe₂, 1L-WS₂–1L-WS₂, and 1L-WSe₂–1L-WSe₂, each with an underlying graphene substrate, was previously reported.¹³⁶ However, in Ref.¹³⁶ the underlying graphene substrate also participates in ultrafast charge transfer.¹³⁷ While picosecond interlayer e transfer following above-band-gap photoexcitation was resolved in Ref.¹³⁶, the timescale for h transfer to the Γ valley remains elusive. The h dynamics at the Γ valley is of particular interest because the spatial extension of the Γ valley wave functions in the out-of-plane direction allows it to play an important role in mediating interlayer h transfer.⁶⁹ Our results yield $\tau_d^{7L} \sim 0.2$ ps for h transfer to the Γ valley of 7L-WSe₂, suggesting that LMJs can also support ultrafast interlayer h transfer.

Methods

Ultra-low frequency Raman spectral fitting accuracy. Raman spectroscopy can determine N in TMDs.⁹⁸⁻¹⁰² However, accurate estimation for $N > 3$ requires measurements of $\text{Pos}(C_{N,1})$ with high precision (typical shift ranging from 0.05 to 0.3 cm^{-1} vs. a typical spectral resolution $\sim 0.6 \text{ cm}^{-1}$). Peak position evaluation with sub-pixel accuracy can be achieved via spectral fitting. We demonstrate the feasibility of this approach by measuring the changes of $\text{Pos}(C_{N,1})$ in 2–12L-MoS₂ (Fig.8). Regions of different thickness are identified using optical contrast and confirmed by AFM. $\text{Pos}(C_{N,1})$ is in Fig.8b (black circles), showing an increase with N in excellent agreement with Eq.

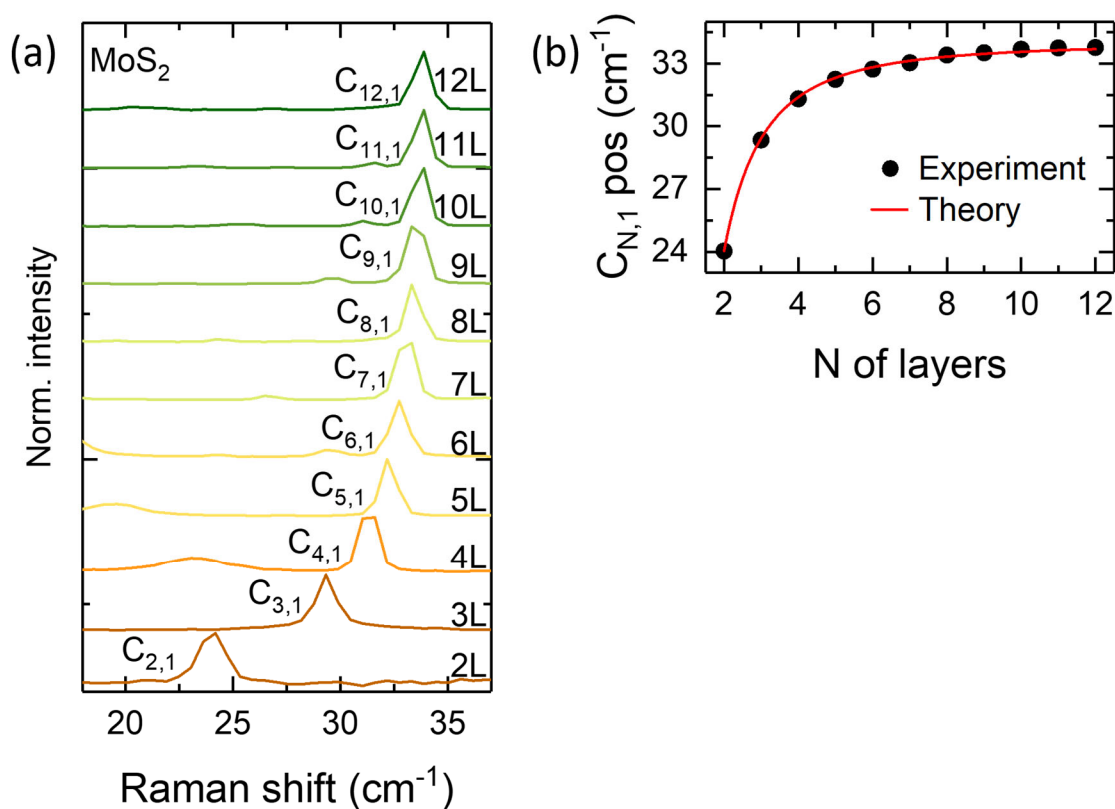


Figure 8. (a) Raman spectra normalized to their maximum intensities showing the $C_{N,1}$ peak in 2–12L-MoS₂. (b) $\text{Pos}(C_{N,1})$ vs. N : experiments (black circles) are in agreement with Eq. 1 (red line).

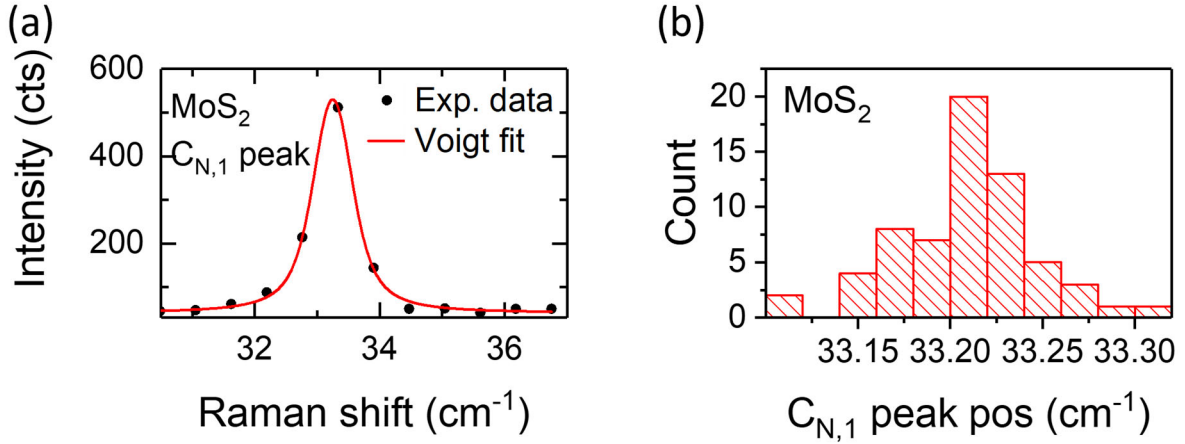


Figure 9. (a) An example $\text{Pos}(C_{N,1})$ fitting for a $N > 15$ ML-MoS₂ flake. Black dots: experimental data. Red curve: Voigt fit. (b) Histogram showing the variation of $\text{Pos}(C_{N,1})$ by acquiring spectra at 64 different points.

1, with $\text{Pos}(C_{\infty}) \sim 33.99 \text{ cm}^{-1}$. $C_{11,1}$ and $C_{12,1}$ can be resolved in Fig.8a, even though $\text{Pos}(C_{12,1}) - \text{Pos}(C_{11,1}) \sim 0.02 \text{ cm}^{-1}$. There are three key factors that contribute an error to $\text{Pos}(C_{N,1})$: 1) general fitting error, 2) statistical error, and 3) sub-pixel specific fitting error.

First, we evaluate general fitting error. Fig.9a is an example of spectral fitting, with black circles representing experimental data and the red line a Voigt fit. The fitted curve is in a good agreement with experimental data, with coefficient of determination $R^2 \sim 0.99$. The typical $\text{Pos}(C_{N,1})$ error is $\sim 0.02 \text{ cm}^{-1}$ and likely represents the lower boundary.

Second, we look at statistical error, i.e., variations of $\text{Pos}(C_{N,1})$ in different areas with the same N , which can be caused by changes of material properties (e.g. strain or disorder), as well as random noise on the CCD detector. The latter can have a strong effect on $\text{Pos}(C_{N,1})$ due to the small number of data points (5 – 7) used for spectral fitting. To evaluate typical values of statistical error, we acquire spectra in 64 areas within a $N > 15$ ML-MoS₂. Fig.9b is an histogram of fitted $\text{Pos}(C_{N,1})$, with a mean $\sim 33.2 \text{ cm}^{-1}$ and standard deviation $\sim 0.04 \text{ cm}^{-1}$, consistent with other samples.

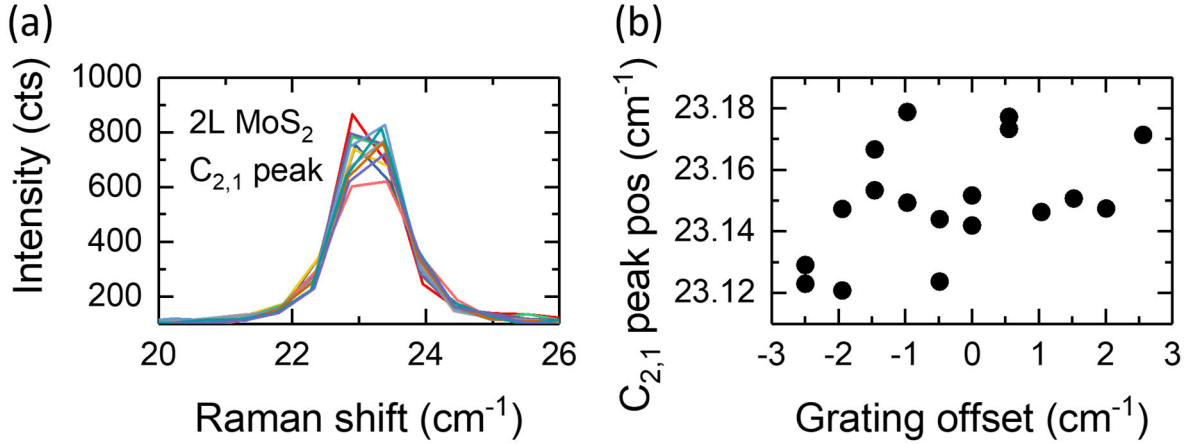


Figure 10. (a) $C_{2,1}$ for different positions of the spectrometer grating. (b) $\text{Pos}(C_{2,1})$ as a function of relative grating position offset compared to the original one.

Third, we consider the error associated with subpixel fitting. Since $\text{FWHM}(C_{N,1})$ is comparable with the spectral resolution, the extracted $\text{Pos}(C_{N,1})$ can be very sensitive to pixel registry, i.e., microscopic alignment of the light dispersed by grating and CCD pixel array. To investigate this, we record the variation of $\text{Pos}(C_{N,1})$ with grating angle, projecting the same signal onto different combination of CCD pixels. Fig.10a,b plot Raman spectra and $\text{Pos}(C_{2,1})$, respectively, for 2L-MoS₂ and different grating positions, indicated by the relative offset to the first two measurements. The variation of $\text{Pos}(C_{2,1})$ has standard deviation $\sim 0.02 \text{ cm}^{-1}$ and a maximum $\sim 0.06 \text{ cm}^{-1}$. As $C_{N,1}$ peaks in regions with different N will be detected differently, depending on pixel registry, we use the highest of these two numbers to evaluate the fitting error.

We can now evaluate the expected error in WSe₂ thickness identification. Table 1 summarizes $\text{Pos}(C_{N,1})$ and corresponding errors for thickness evaluation. Fig.11 compares Eq. 1 (black) with fitted $\text{Pos}(C_{N,1})$ for the ML-WSe₂ of Fig.1. Solid lines correspond to the mean value and dashed lines indicate position error. We identify Region 1 as $N = 7$ and Region 2 as 10 ± 1 .

Table 1. $Pos(C_{N,1})$ and associated fitting errors in ML-WSe₂.

Region	$Pos(C_{N,1})$ (cm ⁻¹)	General fitting error (cm ⁻¹)	Statistical error (cm ⁻¹)	Sub-pixel fitting error (cm ⁻¹)	Total error (cm ⁻¹)
1	23.76	±0.01	±0.04	±0.06	±0.06
2	24.03	±0.01	±0.01	±0.06	±0.06
bulk	24.38	±0.01	±0.01	±0.06	±0.06

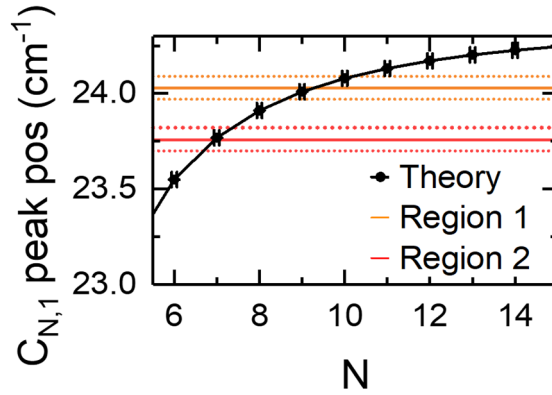


Figure 11. N identification in ML-WSe₂. Black: plot of Eq. 1 based on $Pos(C)_{\infty} \sim 24.38$ cm⁻¹. Colored solid lines are $Pos(C_{N,1})$ for the ML-WSe₂ regions of Figure 1, with dashed lines indicating the total fitting error.

Time-resolved photoemission electron microscopy. We use a high-repetition-rate, high-power Yb fiber laser (Tangerine 30, Amplitude Systemes), which delivers 40 μ J, 320 fs pulses at 0.6 MHz and 1.03- μ m center wavelength (1.20-eV photon energy). After spectral broadening in a Xe-filled hollow-core fiber,¹³⁸ a combination of highly dispersive chirped mirrors and a pair of wedges compress pulses to 50 fs FWHM duration. Second and third harmonics, with photon energies \sim 2.41 and 3.61 eV, are generated through nonlinear frequency conversion in β -barium borate crystals, followed by temporal compression using a prism pair. The FWHM of the second harmonic, which acts as pump beam, is \sim 46 fs, whereas that of the third harmonic, acting as a probe, is \sim 40 fs.

The pump beam is sent into a computer-controlled optical delay line to vary the time delay between pump and probe pulses. The overall time resolution, as determined by pump-probe cross-correlation at the sample position, has FWHM~55fs. The PEEM microscope (Focus GmbH, PEEM-IS) has a spatial resolution~77nm according to the 16–84% criterion, defined as the distance over which the image intensity decreases from 84% to 16% of its maximum.^{91,139} At each time delay, the image acquisition time is 19 s. The PEEM microscope (Focus GmbH, PEEM-IS) has a spatial resolution~77nm according to the 16–84% criterion, defined as the distance over which the image intensity decreases from 84% to 16% of its maximum.^{91,139} At each time delay, the image acquisition time is 19 s. Time-zero is defined as the pump-probe time delay when the peaks of the pump and probe pulse envelopes overlap. It is determined by global fitting of the PEEM signals from 1L- and 7L-WSe₂. This approach determines time-zero with an uncertainty <2 fs. Our measurements employ a time-integrated detector and do not resolve the dynamics of the photoemission process. Thus, the temporal behavior of secondary electron emission does not contribute to the observed pump-probe dynamics.

We now consider possible artifacts associated with surface photovoltage, space-charge, and sample charging effects. Surface photovoltage and space-charge lead to shifts¹⁴⁰ and broadening of the photoemission spectra,¹⁴¹ respectively. These effects do not affect energy-integrated TR-PEEM measurements, such as ours, consistent with the fact that corrections for these effects in energy-resolved measurements do not affect the total number of photoemitted e.^{115,142} For a set of time delays t_i , the data acquisition program collects a PEEM image at t_i , $S(t_i)$, and immediately after that, an image at 250 ps, $S(250_i)$. The differential PEEM signal given by $\Delta S(t_i) = S(t_i) - S(250_i)$. Since the acquisition time of individual images is 19 s, while sample charging builds up over a~1h timescale under our conditions, sample charging is minimized by referencing to the

images collected at 250 ps. As the pump-probe signal is negligible ($\sim 0.2\%$ of the peak pump-probe signal) at this 250-ps time delay, this referencing procedure also allows for the removal of one-color multiphoton pump-only and multiphoton probe-only signals. The spatial dependence of the PEEM signal in the 7L-WSe₂ region, shown in Fig.5c and assigned to the depletion width, cannot originate from surface photovoltage, because our energy-integrated measurements are insensitive to energy shifts induced by surface photovoltage.¹⁴⁰

Ab Initio nonadiabatic molecular dynamics. Simulations based on nonadiabatic molecular dynamics allows us to model quantum transitions between e states responsible for charge transfer and recombination processes accompanied by e-vibrational energy relaxation. Geometry optimization, e structure and adiabatic molecular dynamics simulations are performed with the Vienna *ab initio* simulation package (VASP).^{143,144} The Pedrew-Burke-Ernzerhof¹⁴⁵ functional is chosen to describe the e exchange-correlation energy. The projector-augmented wave¹⁴⁶ approach with a 400eV plane-wave basis energy cutoff is used to treat interactions between ionic cores and valence e. The van der Waals interactions are described with the Grimme DFT-D3 method.¹⁴⁷ The periodic images are separated by ~ 15 Å of vacuum perpendicular to the normal of the 1L/2L WSe₂ plane to screen off spurious interactions. Geometry relaxation stops when the ion forces are $< 10^{-3}$ eV·Å⁻¹.

The nonadiabatic molecular dynamics simulation of the photoinduced charge transfer is performed using the mixed quantum-classical fewest-switches surface hopping technique¹⁴⁸, implemented within the time-dependent Kohn-Sham theory.^{134,149} The e densities of edge states excluded from the simulations are in the Supporting Information. The e-h recombination is modelled by the decoherence-induced fewest-switches surface hopping approach,¹⁵⁰ taking into account loss of coherence in the e subsystem induced by coupling to phonons. The decoherence

time is estimated as the pure-dephasing time of the optical response using the second-order cumulant approximation.^{151,152} The e densities of edge states excluded from the simulations are in the Supporting Information. After geometry optimization, the system is heated to 300 K using uniform velocity rescaling. Then, a 6ps adiabatic MD trajectory is obtained with a 1 fs time step in the microcanonical ensemble. The trajectory is used to perform the NAMD calculations. In order to model e-h recombination over hundreds ps, the 6-ps NAMD Hamiltonian is iterated under the classical path approximation. Detailed information on the simulation algorithms is in Refs.^{153,154}. This methodology was previously used to model excited state dynamics in a broad range of materials, such as semiconductor¹⁵⁵ and metallic¹⁵⁶ quantum dots, nanotubes,¹⁵⁷ metal halide perovskites,¹⁵⁸ plasmonic structures,¹⁵⁹ transition metal oxides,¹⁶⁰ and nanoscale interfaces.¹⁶¹

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Supporting Information

Supporting Information is available free of charge online. Determination of photon order and probe window, kinetic modeling of TR-PEEM, characterization and TR-PEEM time traces of isolated 1L-WSe₂, analysis of decay amplitudes of 1L-WSe₂, estimation of exciton densities of isolated 1L-WSe₂ and 1L-7L-WSe₂, extraction of depletion width and its time dependence, charge density plots of edge states.

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