

**Numerical model-based analysis of energy-efficient reverse osmosis
(EERO) process: Performance simulation and optimization**

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Abstract

We conducted a feasibility study of the energy-efficient reverse osmosis (EERO) process, which is a multi-stage membrane system that integrates single-stage reverse osmosis (SSRO) and a countercurrent membrane cascade with recycle (CMCR). To this end, we developed a numerical model for the 1-2 EERO process (one SSRO stage with two stages in CMCR: one nanofiltration (NF) stage followed by one terminal RO stage), then validated the model using performance data obtained from commercial RO projection software. Retentate recycle ratio was one of the key parameters to determine energy efficiency of EERO. In addition, the implementation of NF membranes in the first stage of CMCR yielded additional improvement in EERO performance and played an important role in determining optimum salt rejection. An optimal design of the NF stage was successfully achieved by hybridization of different NF membranes in a vessel (internally staged design, ISD). Under the conditions optimized, EERO exhibited not only greater energy efficiency (3 – 25%), but lower concentration polarization (CP) and potentials of membrane fouling than conventional SSRO for $\geq 55\%$ overall recoveries because of reduced water flux in the lead elements (averagely 34%). These findings can thus provide insight into optimal design and operation of the EERO process.

Keywords

Reverse osmosis; Seawater desalination; Energy-efficient; Multistage processing; Specific energy consumption

1 **1. Introduction**

2 Two major innovations of membrane development are findings of Loeb–Sourirajan
3 asymmetric and thin-film composite membranes [1]. Recently, research for emerging
4 membranes such as those incorporated with aquaporin and nanomaterials including carbon
5 nanotubes have been thrived as a means of membrane performance enhancement, while
6 challenges remain such as limited salt rejection and commercialization [2]. A central dilemma
7 of membrane development is tradeoff relation of water and salt permeabilities, a major
8 hindrance for developing a high-performance membrane with both high water permeability and
9 salt rejections [3]. Meanwhile, process optimization can play an imperative role in reducing
10 energy consumption, therefore lowering the cost of water production. One of the main benefits
11 of process optimization is its facileness to simulate various membrane configurations without
12 implementation of pilot testing, therefore enable to propose various conceptual and energy-
13 efficient membrane process designs.

14 A single-stage reverse osmosis (SSRO) process, a conventional RO membrane
15 configuration, achieved a high water recovery of ~50% with novel membrane materials and
16 innovative designs of system and membrane module [2]. SSRO has been a preferred design of
17 reverse osmosis (RO) for seawater desalination than two RO stages in series when similar water
18 recovery rate is aimed [4]. This is because reduced energy for two-stage RO membrane does
19 not offset its additional capital cost [2, 4]. Unfortunately, SSRO has also a drawback of being
20 a high recovery process; net driving pressure (NDP) for water permeation is unevenly
21 distributed over the membrane module [4]; NDP is gradually declining along a pressure vessel
22 and it is more exacerbated by increasing either the recovery or the feed concentration at a given
23 recovery [4]. Consequently, an imbalance in water flux accompanies a high degree of
24 thermodynamic irreversibility at lead elements due to membrane fouling, thereby degrading

25 the energy efficiency of RO process [5, 6]. In this respect, two RO stages in series can reduce
26 the thermodynamic irreversibility of SSRO, nonetheless such configuration design is
27 impractical and not viable for achieving a high recovery of > 60% for desalination of high
28 saline feed water (> 35 g/L TDS) [7], hence generally adopted for brackish water reverse
29 osmosis (BWRO) [8]. This is because osmotic pressure differential (OPD) across membranes
30 and operating pressure at the second stage increase excessively, not allowable for the majority
31 of commercial membranes [7]. For improvement of the existing two-stage SWRO system, the
32 Mega-ton Water System project in Japan can be example. Two-stage high recovery RO
33 membrane system, named Low-Pressure Multi-Stage System (LMS), was recently proposed
34 and can achieve 60% recovery by the reduced pressure of the first stage with a short pressure
35 vessel that contains 2-4 elements for the 1st stage, then followed by a relatively long vessel for
36 the 2nd stage [9]. However, it was evaluated that LMS is also difficult to expect further energy
37 reduction as compared to a conventional system, unless LMS applies high efficiency of the
38 elemental technologies developed in the Mega-ton project: a large-scaled high-pressure pump;
39 a new isobaric ERD; and a low-pressure SWRO membrane [9].

40 The hybrid and multi-stage systems have recently emerged as a prospective design of
41 RO process to overcome the aforementioned demerits of conventional RO unit configurations
42 [2]. A key common feature of these two systems is to lower the level of OPD in a RO stage,
43 with osmotic dilution of the seawater feed and a staged membrane operation, respectively.
44 Many studies demonstrated the potential of energy reduction for hybrid systems, where forward
45 osmosis (FO) or pressure retarded osmosis (PRO) is combined with RO as a pre-treatment
46 process [10, 11]. Nevertheless, they still have technological barriers for practical
47 implementation due to the lack of commercial membranes suitable for FO and PRO processes
48 [12]. In case of an ideal multi-stage system, the theoretical minimum energy required for

49 desalination should be close to a thermodynamic limit of concentrates in each stage [2]. This
50 plays a role in reducing the flux imbalance and thermodynamic irreversibility over the vessels
51 of all stages [6]. Lin and Elimelech confirmed the potential of significant energy reduction with
52 the multi-stage systems that employed direct pass and closed-circuit RO configurations [6, 13].
53 In closed-circuit RO (also known as semi-batch RO), however, the continuous mixing of
54 recirculated brine with the incoming fresh feed can limit (degrade) energy efficiency due to
55 entropy generation inside the system [14]. A fully batch RO, hence, has received great attention
56 recently, since it employs a non-pressurized mixing tank to minimize a differential in
57 concentrations of two solutions fed to membrane module, and thereby further reduce energy
58 consumption over semi-batch RO [14]. Nevertheless, these kind of multi-stage systems would
59 be still challenging to be practically implemented due to that: one may need large numbers of
60 stages over eight (theoretically infinite stages) to avoid substantial increases in the OPD and
61 feed pressure required for downstream stages, similar to the two stages in series as described
62 earlier; the others (batch/semi-batch RO) would need robust pumps and ERDs in which the
63 high efficiencies are continuously maintained under operation with continually varying
64 hydraulic pressures [15], and require further development of system operation, such as
65 temporary pressure control to maintain decent recovery during recirculation of the brine back
66 to the feed water [13]. There has been little to no operational experience of a fully batch RO
67 process [15].

68 A promising membrane system design was conceptually proposed by Chong et al.:
69 energy-efficient reverse osmosis (EERO) [7]. The EERO process was configured as multiple
70 stages that incorporate one or more SSRO stages and a countercurrent membrane cascade with
71 recycle (CMCR). In the EERO process, the brine from SSRO is further processed by the CMCR
72 which consists of one or more nanofiltration (NF) stages and a terminal RO stage. This concept

73 was proposed based on optimization strategy for multistage processing with recycling of one
74 or both counter-currently flowing streams (e.g., distillation) [7]. A key feature of CMCR is to
75 lower the OPD across membrane by using (i) NF membrane to allow passage of more salts
76 with water than RO membrane, and (ii) interstage recycling [8]: permeate recycle from the first
77 to subsequent stages; retentate recycle from the last to preceding stages. As a result, the EERO
78 process can achieve a reduction in ~33% in the OPD relative to conventional SSRO
79 configuration, and thus enhance a water recovery at the same quantity of specific energy
80 consumption (SEC) since the reduced energy of 33% is used for producing additional water in
81 CMCR [7]. However, in some cases, EERO energy efficiency was reported to be lower than
82 conventional RO designs, alluding necessity of EERO optimization [16].

83 In previous studies [7, 16], the analytical models, solving a set of algebraic equations,
84 facilitated assessment of the EERO performance with a few system design variables: water
85 recovery and efficiency of ancillary equipment such as energy recovery device (ERD) and
86 booster pumps (BPs). While the previous studies succeeded to conceptually prove the
87 feasibility of EERO, their analytical model has limitations that need to be addressed. For
88 instance, an ideal membrane module that can operate at the thermodynamic limit ($\Delta p = \Delta \pi$)
89 was assumed. Moreover, concentration polarization (CP) and pressure drop along the flow
90 channel due to frictional losses were not taken into account [7, 16], which plays more important
91 roles to determine energy efficiency for systems with higher water recovery [8] and larger scale
92 such as multistage processes. Specifically, operation with a higher recovery causes a high
93 membrane flux, thereby enhancing CP. In addition, many stages (i.e., longer flow channel) can
94 increase the degree of pressure drop. These two phenomena result in the reduced net driving
95 pressure (NDP) for permeate flux across membrane. Their disregard, therefore, inevitably
96 incurs the overestimation of the EERO system performance. Furthermore, the previous model

97 did not embody the properties of specific membranes, so that it may be infeasible to reflect
98 realistic conditions of operation (i.e., dependent strongly on membrane properties) in
99 simulation; for instance, as the rejection of NF membrane was not specified in the previous, it
100 is a challenge to find suitable membranes to satisfy the required rejection.

101 The primary aims of this study are to 1) develop a numerical model for a 1-2 EERO
102 process that consists of one SSRO stage and two stages in CMCR, and subsequently 2) assess
103 energy efficiency of the EERO process, and finally 3) determine optimal conditions for
104 retentate recycle ratio, water recovery rate, and NF module design by hybridization of different
105 NF membranes. CP and pressure drop across a pressure vessel were incorporated in the
106 numerical model in order to realistically simulate transport phenomena. In addition, SEC of
107 the EERO process was compared with conventional SSRO system under various conditions of
108 overall water recovery. This would provide valuable information on acceptable treatment
109 capacity of the EERO process, in terms of electrical operating cost. This study was intended
110 not only to provide optimal design and operating conditions of the EERO process, but also to
111 address a controversial issue regarding applicability of the EERO system for seawater
112 desalination.

113

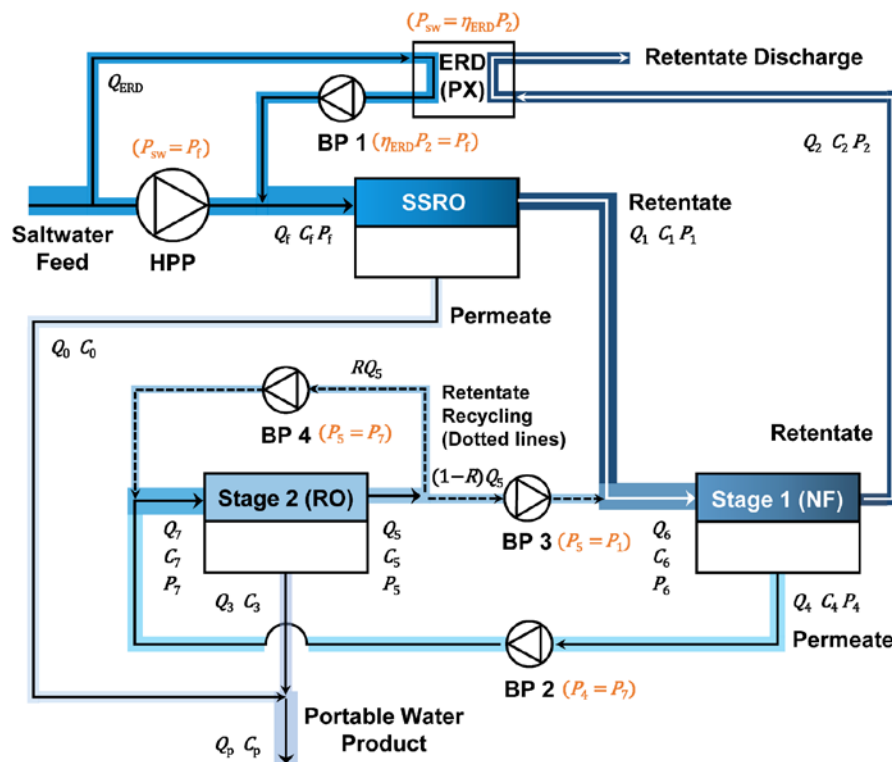
114 **2. Modeling procedure**

115 ***2.1. Process description***

116 Fig. 1 illustrates the configuration of a 1-2 EERO process. This multi-stage system is
117 comprised of a SSRO stage and a two-stage CMCR containing one NF stage and one RO stage.
118 In Stage 1 of CMCR, the retentates (brines) from SSRO stage and recycled from terminal RO
119 stage in CMCR are treated by NF membrane. This plays an influential role in reducing the OPD

120 for the CMCR stages by NF membrane passing more salt with water than RO membrane. In
 121 Stage 2 of CMCR, the permeate from Stage 1 is desalinated using RO membrane to improve
 122 the purity and recovery of the water product. Furthermore, the NF interstage can remove large
 123 portion of divalent ions in the first stage RO brine, allowing for lower saturation indexes in
 124 comparison with two (or multiple) RO stages in series. It will also be operating at lower
 125 salinities in the recirculation step, which potentially could improve the salt rejection slightly.

126



127

128 Fig. 1. A schematic of energy-efficient reverse osmosis (EERO) process where single-stage
 129 reverse osmosis (SSRO) is combined with a countercurrent membrane cascade with recycle
 130 (CMCR). In the example is a 1-2 EERO, where the CMCR consists of two stages; one
 131 nanofiltration (NF) stage and one terminal reverse osmosis (RO) stage.

132

133 It is generally recognized that most of the commercial NF membranes are not designed
 134 to be operated at high pressure, for example NF90 from Dow FilmTec, the recommended

135 pressure limit is 41 bars. For salty water treatment purpose, however, some of commercially
136 available NF membranes can be operated up to a maximum pressure of 83 bar [17]. In this
137 simulation work, we have assumed that the membrane can be operated at higher pressure i.e.
138 up to 69 bar similar to typical RO and the membrane performance is not compromised. Also,
139 from the pilot test conducted for a 1-2 EERO process, the NF membrane can be operated at
140 pressure higher than 41 bars; the results from the pilot test will be reported in a forthcoming
141 paper. Of all streams at Stage 1, the permeate stream is pressurized by an interstage booster
142 pump (BP 2) and fed into Stage 2 (RO). Meanwhile, the hydraulic energy of NF retentate (i.e.,
143 final retentate of EERO process) is recovered by an ERD. This is an additional energy source
144 to pressurize a partial amount of the feed to the SSRO stage, although a booster pump (BP 1)
145 consumes the energy to equalize the feed pressure discharged from the ERD with that from a
146 high-pressure pump (HPP). In the Stage 2, the retentate is split into two recycle streams (dotted
147 lines in Fig. 1), and combined with the brine stream of SSRO and feed stream of Stage 2,
148 respectively. These recycled streams are elevated by BP 3 and BP 4 to make their pressures
149 equal to those of the main feed to Stage 1 and Stage 2 (solid lines in Fig. 1). This retentate
150 recycle not only enriches the feed water quantity to Stage 1 and Stage 2, but also has a dilution
151 effect on the highly concentrated retentate from the SSRO stage. Accordingly, it can diminish
152 the degree of the OPD for the subsequent stages.

153 The 1-2 EERO is a process with “semi-closed loop recycling” unlike semi-batch RO
154 with “full-closed loop recycling” (commonly known as closed-circuit desalination). This is
155 because permeate and retentate streams in CMCR are simultaneously and continuously
156 discharged in an open-loop manner from the point of view of the whole process, while its
157 individual stages are running in a closed-loop manner. The EERO, therefore, would incur an
158 entropy-of-mixing penalty smaller than the semi-batch RO. The mixing of two different

159 concentration solutions itself may not crucial for entropy generation, but continuous
160 accumulation of salt within the system where at least one of outlet streams is (fully or partially)
161 recycled to the inlet feed stream. This is one of main issues of degraded energy efficiency in
162 the semi-batch RO: salt remains until the brine is moved out of the system throughout closed
163 recirculation loops of the brine, thereby causing gradual increases in osmotic pressure in the
164 feed and operating pressure. A series of such (salt) cumulative progress due to closed-loop
165 recycling and mixing can lead to significant entropy generation and thereby entropic energy
166 loss.

167

168 ***2.2. System performance***

169 ***2.2.1 Inlet feed water to CMCR stages***

170 Differential mass balance Eqs. (1) – (4) were employed to quantify the feed water
171 variables, Q_6 , C_6 , Q_7 , and C_7 , under steady-state conditions. Due to mixing of feed and recycled
172 retentate (brine) streams of different salinities for CMCR stages, those variables change with
173 time, but become stationary after certain period (or cycles) of transient behavior. As discussed
174 in the preceding section, CMCR itself is a semi-closed loop process unlike a full-closed loop
175 process such as batch or semi-batch RO. Eqs. (1) – (4) were derived based on conservation
176 laws and several assumptions: complete mixing of two different fluid streams; negligible
177 hydraulic residence time within stages and pipelines.

178

$$179 \quad \frac{dV_6}{dt} = Q_1 + (1 - R)Q_5 \quad (1)$$

180
$$\frac{dC_6}{dt} = \frac{Q_1 C_1 + (1-R)Q_5 C_5}{V_6} - \frac{C_6}{V_6} \frac{dV_6}{dt} \quad (2)$$

181
$$\frac{dV_7}{dt} = Q_4 + RQ_5 \quad (3)$$

182
$$\frac{dC_7}{dt} = \frac{Q_4 C_4 + RQ_5 C_5}{V_7} - \frac{C_7}{V_7} \frac{dV_7}{dt} \quad (4)$$

183

184 where V , Q , and C are the volume, volumetric flow rate, and solute concentration of the fluid,
 185 respectively. R is the retentate recycle ratio in Stage 2. Note that hydraulic pressures, P_6 and P_7 ,
 186 are gauge values and constant by adjusting the pressure of two recycle streams using BP 3 and
 187 BP 4.

188

189 **2.2.2 Specific energy consumption**

190 The SEC for 1-2 EERO process can be defined as the ratio of the net rate of work done
 191 by main and ancillary equipment to the total flow rate of the water product, given by:

192

193
$$\text{SEC}_{\text{EERO}} = \frac{\dot{W}_{\text{HPP}} + \dot{W}_{\text{BP1}} + (\dot{W}_{\text{BP2}} + \dot{W}_{\text{BP4}}) + \dot{W}_{\text{BP3}}}{Q_p} \quad (5)$$

194

195 where Q_p is the total permeate flow rate, which is the sum of permeate flow rates of SSRO
 196 stage and Stage 2 (Q_0 and Q_3). SEC_{EERO} is normalized with respect to the feed osmotic pressure
 197 to individual stages, defined as $\text{SEC}_{\text{norm}} = \text{SEC}/\pi_0$ [18]. The work-rate \dot{W} for individual

198 equipment is calculated as follows [18]:

199

$$200 \quad \dot{W}_{\text{HPP}} = \frac{P_f (Q_f - Q_2)}{\eta_{\text{pump}}} \quad (6)$$

$$201 \quad \dot{W}_{\text{ERD}} = \eta_{\text{ERD}} P_2 Q_2 \quad (7)$$

$$202 \quad \dot{W}_{\text{BP1}} = \frac{(P_f - \eta_{\text{ERD}} P_2) Q_2}{\eta_{\text{pump}}} \quad (8)$$

$$203 \quad \dot{W}_{\text{BP2}} + \dot{W}_{\text{BP4}} = \frac{P_7 (Q_7 - K_{\text{STG2}} R Q_5)}{\eta_{\text{pump}}} \quad (9)$$

$$204 \quad \dot{W}_{\text{BP3}} = \frac{(P_1 - P_5)(1 - R) Q_5}{\eta_{\text{pump}}} \quad (10)$$

205

206 where \dot{W}_{HPP} , \dot{W}_{ERD} , \dot{W}_{BP1} , \dot{W}_{BP2} , \dot{W}_{BP3} , and \dot{W}_{BP4} refer to the work-rate done by HPP, ERD, BP
207 1, BP 2, BP 3, and BP 4. Note that the two streams in the ERD are assumed to have the same
208 flow rate ($Q_{\text{ERD}} = Q_2$). Eq. (10) is used for $P_5 < P_6$, whereas \dot{W}_{BP3} is zero for $P_5 \geq P_6$ because BP
209 3 is unnecessary under that condition. P_f and Q_f are the inlet feed pressure and flow rate,
210 respectively. η_{pump} and η_{ERD} are the efficiencies of pumps and ERD (assumed to be 85% and
211 90%, respectively). K_{STG2} denotes the coefficient to account for the pressure difference between
212 inlet (feed) and outlet (retentate) of the RO membrane module for Stage 2. It can be determined
213 as the ratio of P_5 to P_7 . In addition, it should be noted that SEC for conventional SSRO process,
214 SEC_{SSRO} , is expressed as $(\dot{W}_{\text{HPP}} + \dot{W}_{\text{BP1}})/Q_p$. For the calculation of SEC_{SSRO} , P_2 and Q_2 of Eq.
215 (6) to (8) are replaced by P_1 and Q_1 , respectively.

216

217 **2.2.3 RO and NF membrane modules**

218 The water and salt transport of RO and NF membranes can be described by irreversible
219 thermodynamics [19]. The Kedem–Katchalsky (KK) model (Eqs. (11) and (12)) were used to
220 determine the water and salt fluxes, J_w and J_s , in pressure-driven membrane processes [20].
221 The KK model can facilitate modeling of both RO and NF membranes since it has two
222 phenomenological terms accounting for diffusion and convection, while the solution–diffusion
223 model interprets the membrane transport with diffusion [21]. In addition, the KK model is
224 adequate for simply describing the transport of single solute and solvent through the membrane
225 [22], in comparison to other transport models; the Nernst-Planck model and the Donnan–steric–
226 pore model (DSPM), which consider specific transport mechanisms characterized by the
227 electrical and structural properties of the membrane [23]. For RO mode, it was assumed that
228 reflection coefficient, σ , is equal to 1 because diffusion is a dominant mass-transfer process
229 within RO membranes. In contrast, NF membranes are governed by both of diffusion and
230 convection, so that the σ value was set to $0 < \sigma < 1$ because it is correlated with the feed solute
231 concentration [19, 24].

232

$$233 \quad J_w = L_p(\Delta p - \sigma\Delta\pi) \quad (11)$$

$$234 \quad J_s = P_s\Delta c + (1 - \sigma)J_w\bar{c} \quad (12)$$

235

236 where L_p and P_s are the water and solute permeabilities of the membrane, respectively. Δp and
237 $\Delta\pi$ are the trans-membrane hydraulic and osmotic pressures, respectively. $\Delta\pi$ can be expressed

238 by the modified van't Hoff equation [25]: $\Delta\pi = (N_{\text{ion}}R_gT\Delta c)/M_s$; Δc is the solute concentration
 239 difference across the membrane (i.e., $c_m - c_p$). N_{ion} , R_g , T , and M_s denote the number of ions,
 240 the ideal gas constant, the absolute temperature, and the molecular weight of the solute,
 241 respectively. The average concentration across the membrane, \bar{c} , is calculated as the
 242 logarithmic mean of c_m and c_p . To consider local variations in the true (real) rejection of solute
 243 at different flow rates along membrane channel, we employed Eq. (13), which was derived
 244 from the Spiegler–Kedem model suitable for large volume flux and high concentration gradient
 245 processes such as RO and NF membranes [26].

246

$$247 \quad R_s = 1 - \frac{c_p}{c_m} = \frac{\sigma(1 - F_s)}{1 - \sigma F_s} \quad (13)$$

248

249 where F_s is the driving force exerted by solutes and defined as $F_s = \exp[-J_w(1-\sigma)/P_s]$ [22]. The
 250 membrane wall concentration, c_m , can be determined using the film theory model [27]:
 251 $(c_m - c_p)/(c_b - c_p) = \exp(J_w/k)$; c_p is the permeate concentration, calculated as (J_s/J_w) , and c_b is the
 252 feed (bulk) concentration. The c_m for reverse osmosis process was estimated with the
 253 assumption of complete solute rejection, unlike nanofiltration. The solute mass-transfer
 254 coefficient k can be defined as $k = D \cdot \text{Sh}/d_h = a \cdot \text{Re}^b \text{Sc}^c$ [28]. The Sherwood number Sh correlates
 255 with the Reynolds number Re ($= \rho \cdot d_h \cdot u_x/\mu$) and the Schmidt number Sc ($= \nu/D$); D is the solute
 256 diffusivity and d_h is the hydraulic diameter of the flow channel; The parameters ρ , μ , and ν
 257 indicate the density, dynamic viscosity, and kinematic viscosity of the bulk solution,
 258 respectively. The constants a , b , and c were set to 0.065, 0.875, and 0.25, respectively, which
 259 were empirically obtained for spacer-filled channels [28]. Using Eqs. (14) – (16), we

260 considered the spatial variations in local fluid properties inside the flow channel. It allows a
 261 more accurate prediction for the water and solute fluxes in a full-scale membrane module. The
 262 cross-flow velocity u_x , solute concentration c_x , and trans-membrane hydraulic pressure Δp_x at
 263 an arbitrary spatial point can be described by [29, 30]:

264

$$265 \quad u_x = u_0 - \frac{2}{\varepsilon_{sp}} \int_{x=0}^{x=L} \frac{J_w}{H} dx \quad (14)$$

$$266 \quad c_x = \frac{1}{u_x} \left[u_0 c_0 - \frac{2}{\varepsilon_{sp}} \int_{x=0}^{x=L} \frac{J_s}{H} dx \right] \quad (15)$$

$$267 \quad \Delta p_x = \Delta p_0 - \frac{12K\mu}{H^2} \int_{x=0}^{x=L} u_x dx \quad (16)$$

268

269 where u_0 , c_0 , and Δp_0 are the solute concentration, cross-flow velocity, and trans-membrane
 270 hydraulic pressure at the inlet port ($x = 0$), respectively. ε_{sp} is the effective porosity of the flow
 271 channel [30]. H and L are the flow channel height and length, respectively. K is the friction
 272 coefficient for the channel wall and spacer [29]. The permeate flow rate and concentration for
 273 single membrane module are described by:

274

$$275 \quad Q_{\text{module}}^p = \int_{x=0}^{x=TL} J_w W dx \quad (17)$$

$$276 \quad C_{\text{module}}^p = \frac{\int_{x=0}^{x=TL} J_w c_p W dx}{Q_{\text{module}}^p} \quad (18)$$

277

278 where TL denotes the total length of a series of membrane elements in a pressure vessel. W is
279 the width of the flow channel. The fractional water recovery for individual and all modules was
280 defined as the ratio of permeate flow rate to feed flow rate: $Y_{SSRO} = Q_0/Q_f$; $Y_{NF} = Q_4/Q_6$; $Y_{RO} =$
281 Q_3/Q_7 ; $Y_{overall} = (Q_0 + Q_3)/Q_f$ (see Fig. 1).

282

283 ***2.3 Numerical solution of equations***

284 MATLAB software (version. R2017a) was used to compute approximate solutions of
285 the governing Eqs. (1) – (18). For model-based simulation of the 1-2 EERO process, we
286 employed a numerical algorithm, illustrated in Fig. 2:

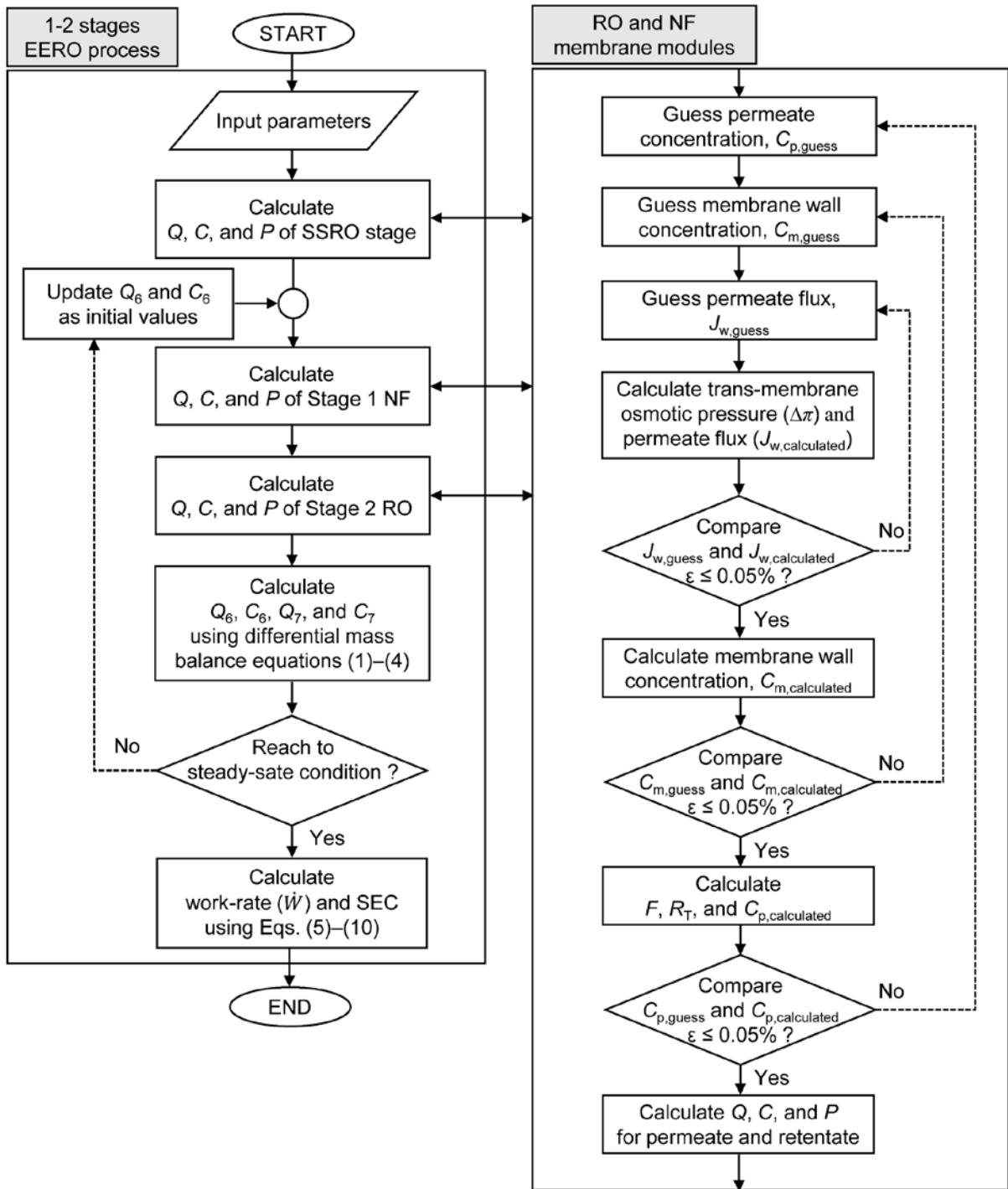
287 (1) Physical and physicochemical variables and parameters, regarding operating conditions,
288 feed water, module, and membrane, are inputted (summarized in Table 1).

289 (2) The performance of each individual stage is obtained by computing the spatial
290 distribution of water and solute transports for RO and NF membrane modules. It can be
291 carried out by employing a finite difference approximation, used in [5]. The flow
292 channel of each membrane module is discretized into finite segments. At each segment,
293 the governing Eqs. (11) – (16) are iteratively solved to calculate the local fluid
294 properties. The numerical calculation procedure is described in detail as follows (right-
295 hand box):

296 a. The permeate and membrane wall concentrations, C_p and C_m , and volumetric
297 permeate flux, J_w , are initially guessed.

298 b. The trans-membrane osmotic pressure, $\Delta\pi$, and J_w are calculated based on the
299 estimated value of C_m using the film theory model.

- 300 c. The preceding procedure is repeated until the error ε between $J_{w,\text{guess}}$ and
301 $J_{w,\text{calculated}}$ is below a tolerance value of 5×10^{-4} . When returning to the guess step,
302 the calculated value is used as a new guess value.
- 303 d. C_m and C_p are recalculated using Eq. (13) once their ε values are below the
304 tolerance. When the ε between the guessed and calculated ones is over the
305 tolerance, a series of previous process is iterated until the ε satisfies the tolerance
306 criterion.
- 307 e. The permeate and retentate flow rates, concentrations, and pressures of a
308 membrane module are calculated using Eqs. (14) – (18).
- 309 (3) The feed water variables, Q_6 , C_6 , Q_7 , and C_7 , are calculated using differential mass
310 balance Eqs. (1) – (4). The obtained values are updated as new input values for those
311 variables to compute the performance for Stage 1 NF and Stage 2 RO at a next time
312 step. A series of the previous steps (2) and (3) are iterated until the variables reach to
313 steady state conditions.
- 314 (4) SEC of the 1-2 EERO process is evaluated by calculating the work-rate \dot{W} of ancillary
315 equipment using Eqs. (5) – (10).



316

317 Fig. 2. Flow chart of the modeling procedure for energy-efficient reverse osmosis (EERO)
 318 process.

319 Table 1 Simulation conditions of 1-2 EERO process.

Parameter	Value	Units
Operating conditions		
Inlet feed flow rate, Q_f	360	m ³ /day
Inlet feed pressure ^a		
SSRO stage, P_f	43.5 – 79.8	bar
Stage 2 RO, P_7	10.3 – 59.9 (up to 107.4 ^b)	bar
Temperature, T	25	°C
Retentate recycle ratio, R	0 – 0.9	-
Pump efficiency, η_{pump}	0.85	-
Energy recovery device efficiency, η_{ERD}	0.90	-
Feed water properties		
Solute concentration, C_f	35	g/L (NaCl)
Solute diffusivity, D_b	1.51×10^{-9}	m ² /s
Dynamic viscosity, μ	1.0978×10^{-3}	Pa s
Kinematic viscosity, ν	9.5×10^{-7}	m ² /s
Module properties ^c		
Spacer thickness, H	7.11 (RO), 8.64 (NF)	10 ⁻⁴ m
Spacer porosity, ε_{sp}	0.8	-
Friction coefficient due to spacer, K	7 (RO), 10 (NF)	-
Membrane area/element	41.0 (RO), 37.2 (NF)	m ²
Leaf width, W	0.72 (RO), 0.66 (NF)	m
Leaf length, L	0.92	m
No. of leaves/element, N_L	31	#
No. of elements/module, N_E	8	# (in series)
No. of modules/stage, N_M	1	#
Membrane properties ^d		
Water permeability, L_p	1.739	L/(m ² h bar)
Solute permeability, P_s	0.064	L/(m ² h)
Reflection coefficient, σ	1	-

320 ^a The range of feed pressures to achieve water recoveries of 20 – 60% (SSRO stage) and 20 –
321 55% (Stage 2 RO) at a retentate recycle ratio of 0.6.

322 ^b Number highlighted in grey are for purpose of comparison and may not be applicable in
323 practice.

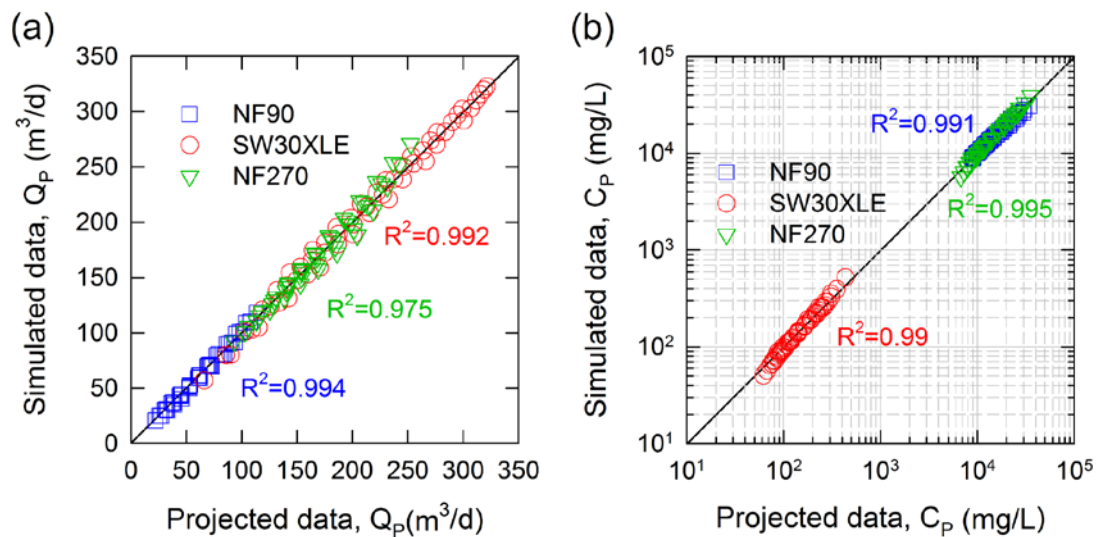
324 ^c The DOW FILMTEC elements, SW30XLE-440i, NF90-400/34i, and NF270-400/34i, were
325 embedded in the RO and NF modules, respectively.

326 ^d The properties, listed in this table, include three membrane transport coefficients for
327 SW30XLE-440i [5]. Those of NF90-400/34i and NF270-400/34i were estimated using
328 empirical correlations, which are described in detail in Appendix A.

329 **3. Results and discussion**

330 **3.1. Model validation**

331 The accuracy of the developed numerical model was validated under various operating
332 conditions prior to simulating the effect of system variables such as retentate recycle ratio and
333 water recovery on the 1-2 EERO process. Fig. 3 presents the comparisons between the
334 simulated data and the projected data from Reverse Osmosis System Analysis (ROSA) 9 that
335 is a commercial projection software provided by the membrane manufacturer, DOW
336 FILMTEC™. The result shows a good agreement ($R^2 > 0.97$) of the permeate flow rates and
337 salt passage between the projected data and simulated data for both RO and NF processes. Note
338 that the performance data for each process were collected based on a module design with a
339 single pressure vessel with eight membrane elements (8-inch) for a single-stage configuration
340 within the range of operating conditions in a 1-2 EERO system.



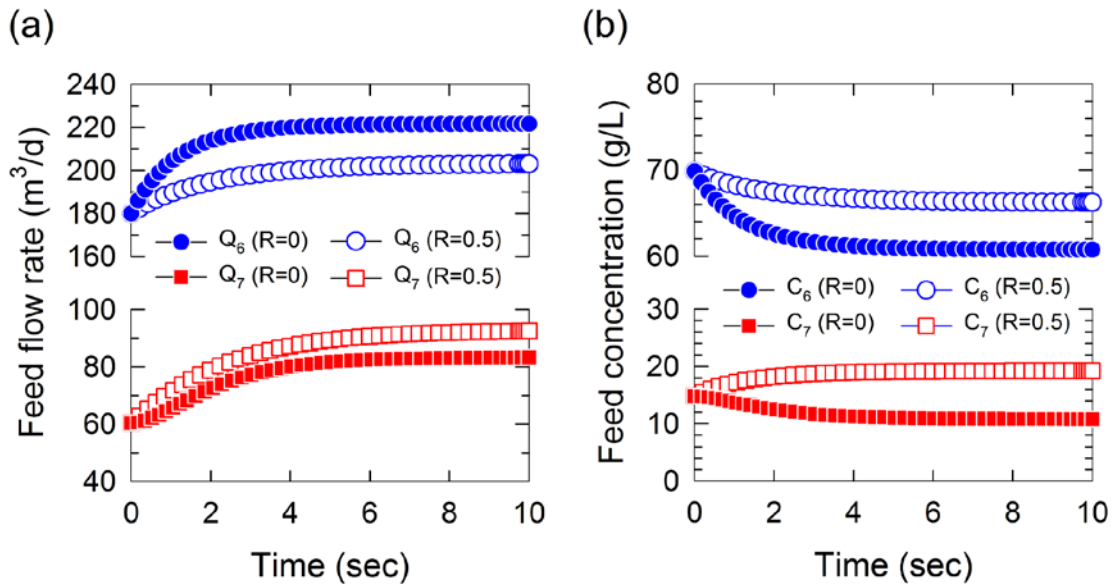
341

342 Fig. 3. Comparisons of the projected (x-axis) and simulated (y-axis) data for (a) permeate flow
343 rate and (b) permeate salt concentration. Individual points indicate the performance obtained
344 under various operating conditions as follows: for SW30XLE-440i – feed concentration (10 –
345 50 g/L at 5 g/L intervals); inlet feed pressure (55 – 80 bar at 5 bar intervals); feed flow rate
346 (360 m^3/d). for NF90-400/34i and NF270-400/34i – feed concentration (50 – 90 g/L
347 at 5 g/L intervals); inlet feed pressure (55 – 75 bar at 5 bar intervals); feed flow rate (190 and 360 m^3/d).

3.2. Dynamic behavior of EERO process

EERO exhibits dynamic behavior of flow rate and concentration at each membrane component until reaching steady state. This dynamic behavior is driven by the mixing process with retentate recycle of Stage 2 RO back to the feed flow of Stage 1 NF. Fig. 4 presents the changes in the flow rate and concentration of the inlet flow to two CMCR stages with time, which was simulated at two different recycle ratios ($R = 0$ and 0.5). The ratio value of 0 indicates that 100% of Stage 2 retentate flow is recycled to Stage 1, whereas the 0.5 value denotes that the recycle flow is divided equally to Stage 1 and 2, respectively. Generally, the variables shown in Fig. 4 either gradually increased or decreased with time and reached at a steady state briefly in 10 seconds of the system operating time. Note that constant pressures of 18.1 and 30.5 bars were employed for the inlet flow pressure of Stage 2 RO (i.e., P_7) at $R = 0$ and 0.5 , respectively, to keep water recovery of Stage 2 at 50%. The inlet feed flow rate, Q_6 , was elevated to $\sim 13\%$ and $\sim 23\%$ by partial ($R = 0.5$) and complete ($R = 0$) retentate recycling to Stage 1, respectively (Fig. 4a). In the meantime, the inlet feed flow, Q_7 , increased to $\sim 53\%$ at $R = 0.5$ and 38% at $R = 0$ due to partial and no retentate recycling to Stage 2, respectively. These would contribute to the OPD reduction for the two CMCR stages because of blending of different concentration streams: lower salinity of the recycled retentate stream (C_5) than the retentate of SSRO stage (C_1); and higher salinity of C_5 than the permeate of Stage 1 (C_4). The inlet flow concentrations of Stage 1 and 2 (C_6 and C_7) at $R = 0.5$ decreased from 70.0 to 66.2 g/L and increased from 14.8 to 19.2 g/L, respectively (Fig. 4b). Those of Stage 1 and 2 at $R = 0$ lowered from their initial values to 60.7 and 10.8 g/L, respectively. Such decreases in concentration difference between C_6 and C_7 confirmed that the OPD can be diminished by the retentate recycle and the degree of its change was determined by the recycle ratio. The effect of the retentate recycle is further scrutinized in the subsequent section.

372



373

374 Fig. 4. Impact of retentate recycle on (a) flow rates and (b) concentrations of inlet feed flows
 375 of Stage 1 NF and Stage 2 RO in 1-2 EERO process. Simulation was performed under the
 376 following operating condition: feed concentration C_f (35 g/L); feed flow rate Q_f (360 m³/d);
 377 SSRO stage recovery (50%); Stage 2 RO recovery (50%); retentate recycle ratio R (0 and 0.5).
 378 Each individual stage employs eight membrane elements in a single vessel, and element type
 379 is as follows: SSRO stage (SW30XLE-440i); Stage 1 NF (NF90-400/34i); Stage 2 RO
 380 (SW30XLE-440i).

381

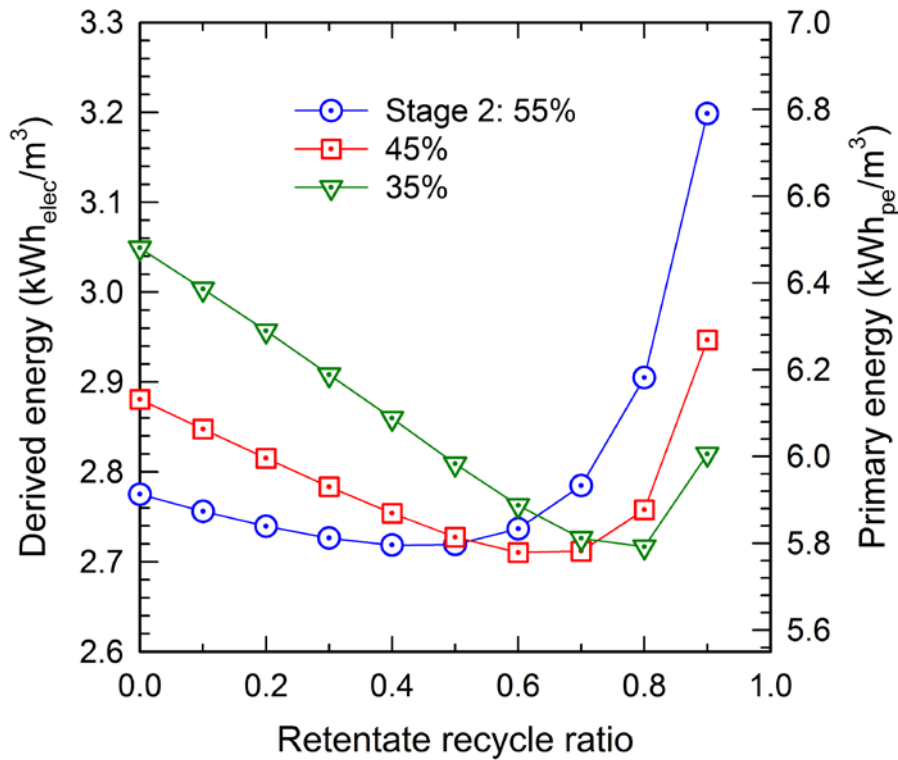
382 3.3. Critical factors affecting EERO process optimization

383 3.3.1 Retentate recycle

384 The ultimate goal of EERO application is to minimize operating cost. As described
 385 earlier, the retentate recycle is a key feature that diminished OPD for the two CMCR stages.
 386 Therefore, it is crucial to scrutinize the optimal recycle ratio for energy minimization. Fig. 5
 387 depicts the profiles of derived and primary energies for the 1-2 EERO process at various
 388 retentate recycle ratios under different conditions of Stage 2 RO recovery with a 45% recovery
 389 of SSRO stage. It should be noted that derived energy is commonly termed specific energy
 390 consumption in membrane processes, so hereinafter it is denoted with SEC. From the result, it
 391 was found that such multistage process must be designed with a pairing of recycle ratio and

392 recovery of Stage 2 RO to reach the optimum SEC when recovery of SSRO is fixed. SEC of
393 the 1-2 EERO can be minimized to $\sim 2.72 \text{ kWh/m}^3$ at which the recycle ratios are 0.8, 0.6, and
394 0.4 corresponding to 35, 45, and 55% recoveries, respectively. SEC decreased monotonically
395 and slowly as increasing retentate recycle ratio until reaching to the optimal points.
396 Subsequently, abrupt increase in SEC was observed above the optimal points. Interestingly, the
397 minimum energy consumptions were all similar regardless of recovery in Stage 2 RO once
398 reaching to the optimum ratio that was inversely proportional to the Stage 2 RO recovery. The
399 increase in the recovery of Stage 2 RO decreases its outlet flow rate (Q_5), therefore its recycle
400 flow rates to both Stage 1 NF and Stage 2 RO were diminished subsequently. At such condition,
401 decreasing retentate recycle ratio can elevate the inlet flow rate of Stage 1 NF (Q_6) and lessen
402 that of Stage 2 RO (Q_7). Consequently, SEC is reduced by increasing work rate of ERD and
403 decreasing work rates of BP 2 and BP 4. The details of system performance (energy
404 consumption, water recovery, concentration, flow rate, pressure), corresponding to Fig. 5, are
405 provided in Supporting Information Table S1. Additionally, primary energy, corresponding to
406 SEC (technically termed “derived energy”), is depicted in the right axis, which can be
407 converted by multiplying SEC and a conversion factor of 2.13 for SWRO proposed in a recent
408 study [31]. Such primary energy analysis is useful for the cross comparison of assorted
409 desalination methods. SEC of a process should be apportioned to the input primary energy,
410 since it is unable to differentiate the grade of energy supplied to processes accurately [31].

411



412

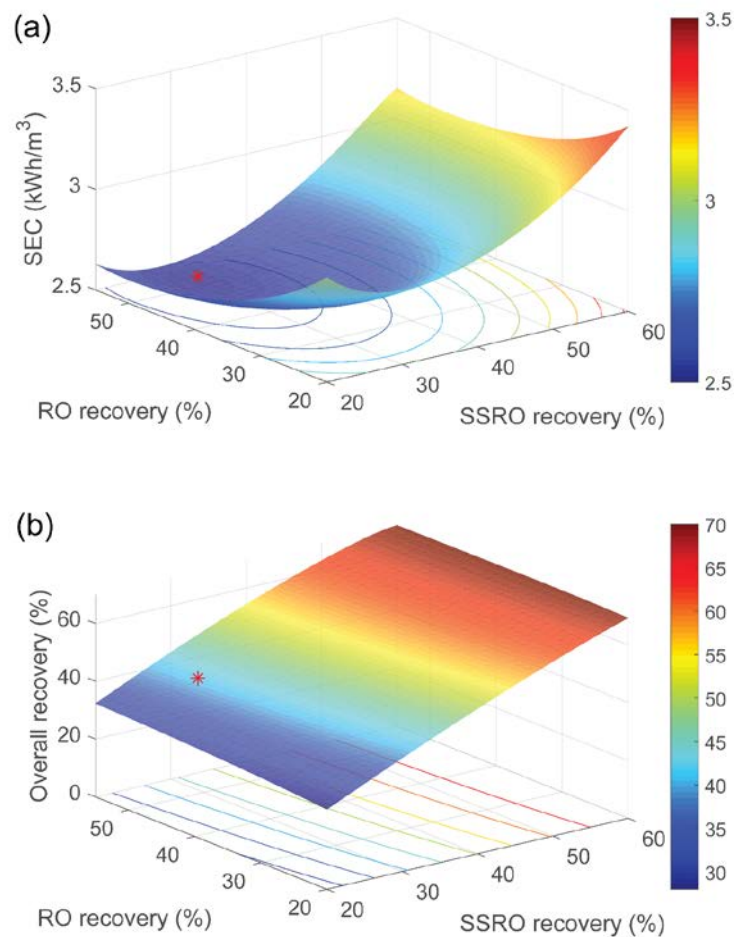
413 Fig. 5. Change in (left axis) derived energy and (right axis) primary energy of 1-2 EERO
 414 process depending on retentate recycle ratio at different recoveries (35 – 55% at 10% intervals)
 415 of Stage 2 RO. Simulation was carried out under the same condition as Table 1. It should be
 416 noted that derived energy is commonly termed “specific energy consumption” (SEC).

417

418 3.3.2 Water recovery of individual stages

419 In the preceding section, the impacts of the retentate recycle ratio of Stage 2 RO was
 420 investigated. Another important operating parameter for overall energy efficiency is SSRO
 421 recovery. Recoveries of SSRO and Stage 2 RO influence their performance interactively,
 422 therefore overall performance and energy efficiency. Figs. 6a and 6b depict SEC and overall
 423 water recovery of the 1-2 EERO process, respectively. Practical range of water recoveries were
 424 tested: 20 – 60% for SSRO stage, ~20 – 45% for Stage 1 NF (see Fig. S1 in Supporting
 425 Information), and 20 – 55% for Stage 2 RO. It demonstrates that the system performance was
 426 highly reliant on the recovery of individual stages. With the given simulation conditions, SEC
 427 varied from 2.52 to 3.42 kWh/m³ when ERD was embedded in this EERO system (Fig. 6a).

428 This result shows that the minimum energy can be achieved by adjusting both recoveries of
 429 SSRO stage and Stage 2 RO. The SEC value displayed a convex (downward) function of
 430 recovery variables in the system. SEC of the system was minimized at 28.3% and 49.0%
 431 recoveries for SSRO stage and Stage 2 RO, respectively. Although the both stages' recovery
 432 values played important roles in determining SEC, overall recovery was predominantly
 433 influenced by SSRO recovery. This is because SSRO stage produces much larger amount of
 434 permeate per unit recovery percentage as compared to Stage 2 RO. The minimum SEC value
 435 was obtained at a recovery of ~42% for the 1-2 EERO system (Fig. 6b).



436

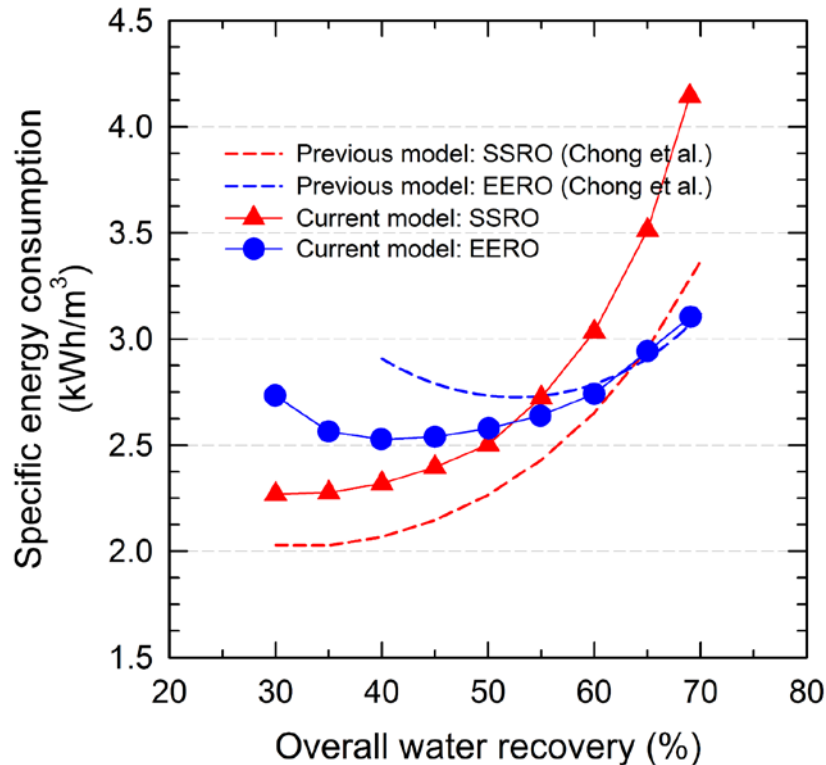
437 Fig. 6. Comparisons of (a) specific energy consumptions and (b) overall water recoveries under
 438 various recovery conditions in SSRO stage and Stage 2 RO in 1-2 EERO process. In the figure,
 439 optimal recovery of the system is indicated by a red-colored star (*) symbol. For simulations,
 440 we employed a retentate-recycle ratio R of 0.6, while the other conditions were the same as
 441 those of Table 1.

442

443 **3.3.3 Overall water recovery**

444 When designing a desalination system, it is reasonable to compare conventional SSRO,
445 one of the most widely implemented configuration, with EERO at a same recovery rate. As
446 presented in the preceding section, the performance of seawater desalination systems can be
447 significantly affected by their water recoveries. Therefore, it would be important to compare
448 each membrane configuration at same overall water recoveries. Fig. 7 depicts the SEC profiles
449 for conventional SSRO and 1-2 EERO processes with respect to overall water recovery at a
450 retentate recycle ratio of 0.6. The minimum SEC values, obtained previously for each overall
451 recovery rate (Fig. 6a), were presented. SEC for conventional SSRO and EERO processes
452 showed exponential and concave upward trends, respectively. The SEC for the 1-2 EERO was
453 reduced up to 2.52 kWh/m³ in the range of 35 – 50%, while conventional SSRO obtained a
454 lower SEC value (2.27 – 2.50 kWh/m³) in the range of 30 – 50%, but was more significantly
455 augmented for the overall recovery greater than 50%. With such a high recovery, its energy
456 efficiency was more rapidly degraded in comparison with the EERO process. As a result, the
457 1-2 EERO becomes more energy-efficient than conventional SSRO at above 55% recovery.
458 The 1-2 EERO exhibited 3.1 – 25.1% lower values of SEC at 55 – 69% overall recoveries with
459 TDS concentration of < 220 mg/L in permeate, which was competitive to that of conventional
460 SSRO (Table 2). This result implies that the 1-2 EERO process can be a promising design
461 option for high-recovery desalination, even though it was prone to more pressure drops: 4.6 –
462 7.4 bars (i.e., a summation of total pressure drops in each individual stages) for 1-2 EERO and
463 2.2 – 3.6 bars for conventional SSRO depending on overall recovery (30 – 69%). Note that
464 each stage of EERO was below the maximum pressure drop across a pressure vessel of ~3.5
465 bar (50 psi): 3.3 bar for SSRO stage, 2.2 bar for Stage 1 NF, and 0.5 bar for Stage 2 RO on
466 average. The details of performance (energy consumption, water recovery, concentration, flow

467 rate, pressure) of the 1-2 EERO, corresponding to Fig. 7, are provided in Supporting
468 Information Table S2.



469

470 Fig. 7. Comparison of specific energy consumptions (SEC) for conventional SSRO and 1-2
471 EERO processes in the range of 30 – 69% overall recovery. Note that system performance for
472 the EERO process was simulated within the range of a maximum (acceptable) operating
473 pressure for commercial reverse osmosis membranes. The dotted red and blue color lines
474 indicate SEC profiles of conventional SSRO and 1-2 EERO processes in the previous work
475 [16].

476

477 In addition, the preceding result was compared with data from previous analytical
478 models (i.e., dotted lines) [16]. The SEC of SSRO for the previous analytical model was about
479 14% lower than for the current numerical model. This was likely because of disregard of CP
480 and pressure drop effects have underestimated the SEC. On the other hand, the SEC for the 1-
481 2 EERO of the previous analytical model was higher than that for the current numerical model.
482 This could be attributed to that the 1-2 EERO of this study was optimized regarding to retentate

483 recycle ratio and recoveries of individual stages. Despite such optimization, an interesting
484 observation was that little/no improvement of the current numerical model in SEC relative to
485 the previous analytical model when an overall recovery was over 50%. This could be explained
486 by the least and excess works of separation (also known as thermodynamic minimum energy
487 and irreversible energy loss, respectively), to which CP and pressure drop effects contribute
488 partly, become more significant in practice, because such limiting factors are greater with a
489 higher recovery. Accordingly, the improved energy (of the current numerical model) was
490 reduced gradually with the recovery, and eventually converged with SEC (of the previous
491 analytical model) at high recovery of > 60%. Nevertheless, a key finding of this result was that
492 the critical recovery (beyond which EERO gives lower SEC relative to conventional SSRO)
493 can be practically shifted from ~65% (the previous analytical model) to ~55% (the current
494 numerical model). This implies that the 1-2 EERO process could be more feasible than
495 expected in the previous assessment.

496 Furthermore, lower membrane fouling propensity of EERO process can be a major
497 benefit over conventional SSRO stage. In order to achieve a same recovery for both
498 conventional SSRO and 1-2 EERO, the amount of water loaded onto each membrane module
499 will be greater for conventional SSRO. It is known that the extent of fouling is proportional to
500 convective flux of foulants toward membrane surface [32]. Therefore, greater recovery
501 (equivalently, flux) per stage would cause greater extent of fouling. By employing more stages,
502 lower recovery for SSRO stage in EERO configuration can be obtained (Table 2). To be specific,
503 1-2 EERO process achieved up to 33.3% lower recovery (26.8% on average) for SSRO stage
504 in EERO than conventional SSRO. While EERO is expected to have lower fouling propensity,
505 its demonstration remains as a future study. In terms of membrane fouling, 1-2 EERO process
506 would be best operated at 60% recovery from a practical point of view. This is to ensure the
507 maximum water flux of all elements in the pressure vessel was below the recommended

508 maximum limit (i.e. 35.7 LMH for seawater pretreated with DOW UF, SDI < 2.5 [33])
 509 (Supporting Information Table S3). To allow higher recovery > 60%, i.e., higher maximum
 510 water flux per element, the system needs to consider pretreatment technologies superior to the
 511 existing UF.

512

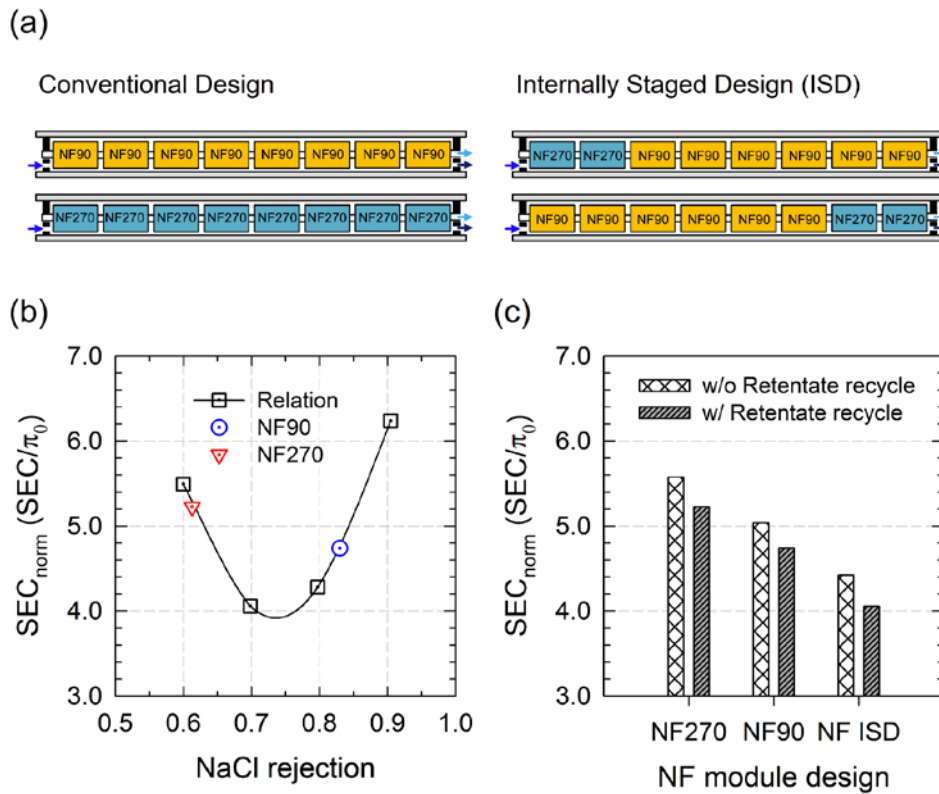
513 Table 2. Simulated profiles of water recovery and final product water concentration for
 514 conventional SSRO and 1-2 EERO processes with respect to overall recovery ^a.

Overall recovery (%)	Conventional SSRO		1-2 EERO ^b		
	Recovery (%)	Permeate concentration (mg/L)	Recovery (%)		Permeate concentration (mg/L)
			SSRO stage	Stage 2 RO	
30	30	217	20.0	33.3	261
35	35	195	22.8	47.8	258
40	40	180	26.9	49.0	237
45	45	170	31.0	53.8	236
50	50	164	36.6	44.1	200
55	55	161	40.7	52.6	217
60	60	158	46.2	51.4	215
65	65	156	53.1	36.9	190
69	69	155	58.6	39.3	210

515 ^a Numbers highlighted in grey are for purpose of comparison and may not be applicable in
 516 practice as either maximum permeate flux or pressure are > 35.7 LMH or > 83 bar, respectively.
 517 ^b Recoveries of individual stages are for conditions of minimum specific energy consumption
 518 (SEC) at each overall recovery (shown in Fig. 7).

519 **3.3.4 NF module design**

520 To improve the energy efficiency of 1-2 EERO process, NF stage of the system needs
 521 to be designed with membranes with the proper rejection and permeability depending on
 522 overall recovery rate. This is because the flow rate, concentration, and applied pressure of Stage
 523 2 inlet stream are significantly influenced by those of Stage 1 outlet (permeate) stream. In this
 524 regard, it would be meaningful to identify the effect of NF module designs in Stage 1 on the
 525 EERO performance. To attain this end, we evaluated the normalized specific energy
 526 consumption (SEC_{norm}) for 1-2 EERO process with 60% overall water recovery, where
 527 conventional and internally-staged designs (ISD) were employed for a single pressure vessel
 528 of NF stage. Note that the conventional design loaded a pressure vessel with single-type
 529 membrane elements, either NF90 or NF270, while both types of membranes were hybridized
 530 for ISD (Fig. 8a).



531

532 Fig. 8. Comparisons of normalized specific energy consumptions for 1-2 EERO processes with
 533 60% overall water recovery, which have single pressure vessel of (a) four distinct

534 configurations of NF membrane elements, (b) different salt rejections, and (c) different modular
535 designs in the presence and absence of retentate recycle. NF ISD, one of NF membrane modular
536 designs in this study, denotes is a hybrid configuration of six NF90-400/34i and two NF270-
537 400/34i.

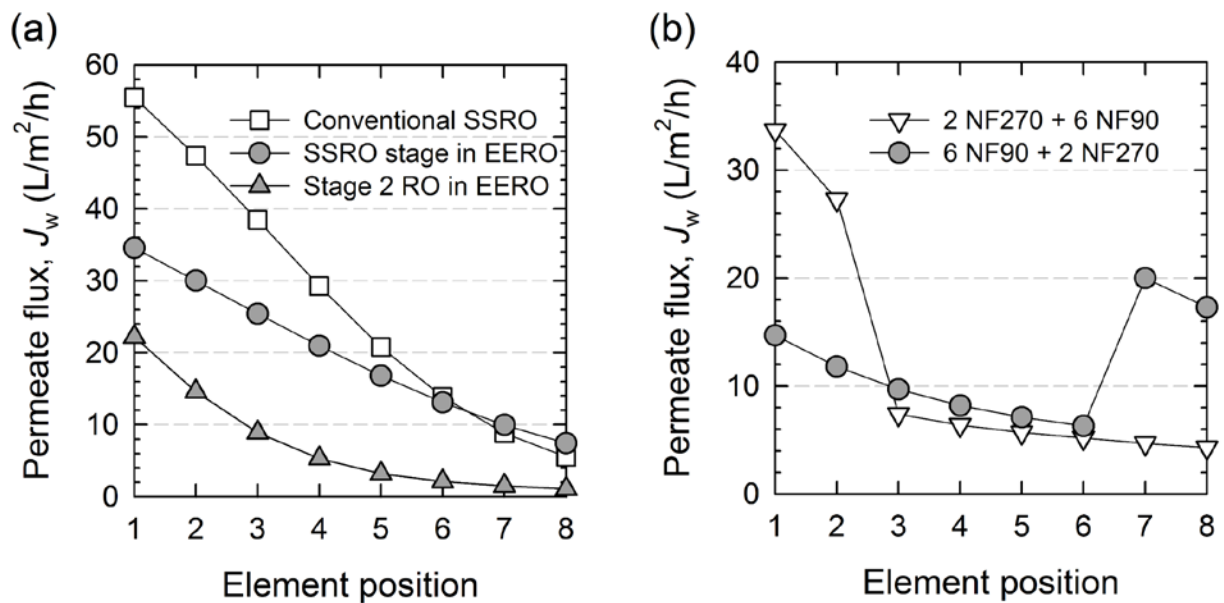
538

539 As a preliminary work, first we tested different NF modules that possess salt rejections
540 ranging 60 – 90% at 10% intervals (Fig. 8b). To perform simulations with different salt
541 rejections, the permeability coefficient P_s , a key parameter determining the membrane solute
542 flux, was adjusted in modeling. From Fig. 8b, the lowest SEC_{norm} value for 1-2 EERO process
543 was found at salt rejection of 70% among the designs with the selected rejections. In addition,
544 according to the black solid curve in relation to the selected rejections, a critical range of salt
545 rejection was found to be 70 – 76% where a relatively low value of SEC_{norm} ($\leq \sim 4$) can be
546 achieved. SEC_{norm} of 1-2 EERO process was considerably increased when salt rejection was
547 either reduced below 60% or raised above 90% from the optimum at 70%. This result could be
548 explained by the trade-off relationship between permeability and selectivity in polymer
549 membranes. A membrane module with very high rejection for NF stage will have low permeate
550 flow rate, as such the feed flow rate for the subsequent RO stage is excessively reduced. In
551 contrast, although a membrane module with very low rejection can lead to a high feed flow
552 rate for the subsequent RO stage, it also increases the feed concentration for the corresponding
553 stage, thereby a greater pressure is required to attain similar target water recovery.

554 As means of further optimization of the NF stage, we analyzed SEC_{norm} of the 1-2
555 EERO process for three cases of NF membrane element configurations with and without
556 retentate recycle (Fig. 8c). ISD can facilitate practical application of optimal rejection of salt
557 to NF stage. As presented in Fig. 8b, the NF90 and NF270 had a salt rejection of 83% and 61%,
558 respectively. The NF ISD, however, acquired the optimum rejection of 70% for NF stage by
559 using six NF90-400/34i and two NF270-400/34i. From Fig. 8c, it was revealed which factor
560 between NF module design and retentate recycle was more sensitive to the EERO system in

561 term of energy reduction. The result showed that SEC_{norm} of NF ISD decreased by averagely
562 18.4% as compared to those of the other configurations (NF90 and NF270). The values of
563 SEC_{norm} depending on the presence and absence of retentate recycle, meanwhile, exhibited <
564 7.0% difference on average for all the designs.

565 Fig. 9 illustrates the profiles of permeate flux in a pressure vessel for individual stages
566 of conventional SSRO and 1-2 EERO processes. The figure demonstrated that the 1-2 EERO
567 process can possess the advantage of mitigating CP and membrane fouling over the
568 conventional processes (Fig. 9a). The two RO stages of the 1-2 EERO maintained the lower
569 level of permeate flux, especially at the lead elements, when compared to the conventional
570 SSRO. With the multi-staged operation, the 1-2 EERO had significantly reduced the fluxes
571 (averagely ~27% and ~76%) of the elements 1 – 5 for SSRO stage and Stage 2 RO, respectively,
572 at the same high overall recovery of 60%. On the other hand, the front element flux for
573 conventional SSRO at 60% recovery has exceeded the maximum recommended limit (i.e. 35.7
574 LMH for seawater pretreated with DOW UF, $SDI < 2.5$ [33]), thus it is only suitable for typical
575 operating conditions of 40 – 45% recoveries (see Supporting Information Table S3). In addition,
576 the conventional SSRO exhibited the highest degree of the flow imbalance over the vessel as
577 observed in Fig. 9a. The corresponding CP values were reduced by 5.2% and 18.3% for the
578 first element of SSRO stage and Stage 2 RO, respectively, compared to the conventional SSRO.
579 An increase in permeate flux at the lead elements causes a higher retentate concentration,
580 thereby increasing feed concentration to the subsequent tail elements. Therefore, such a high-
581 recovery conventional SSRO would have the potential to aggravate not only organic and
582 colloidal fouling at the lead elements, but also scaling of inorganic substances at the tail
583 elements.



584

585 Fig. 9. Permeate flux of element of (a) RO stage in conventional SSRO and 1-2 EERO
 586 processes, and (b) NF stage with ISD in 1-2 EERO processes. The permeate fluxes were
 587 simulated at an overall water recovery of 60%.

588

589 The investigation into ISD for NF stage's module could be informative, because the
 590 permeate flux profile along the element position can be largely changed depending on how we
 591 internally arrange different types of membrane elements within the vessel [5]. In this study, the
 592 permeate flux for two different ISDs were evaluated (Fig. 9b): 1) two NF270-400/34i + six
 593 NF90-400/34i; 2) six NF90-400/34i + two NF270-400/34i. Note that both element
 594 configurations can be considered as a part of ISD options in actual practice, because they
 595 attained the water recovery and salt rejection of near the optimum (70%) from their single
 596 pressure vessels, under almost similar operating conditions in NF stage. From the result, it was
 597 found that the latter configuration was more suitable for NF ISD, since its permeate flux at the
 598 first two elements was significantly lower than that of the former. The permeate flux of the
 599 latter noticeably increased at the last two tail elements, but this design was still expected to
 600 have less fouling potential due to a relatively low level of permeate flux (≤ 20 LMH) over the
 601 vessel.

602

603 **4. Conclusion**

604 This study was primarily aimed at assessing and optimizing the efficiency of a 1-2
605 EERO process. To this end, the 1-2 EERO process was numerically modeled, and its
606 performance was then predicted under various operating conditions. For practical simulations,
607 we considered performance-limiting factors (i.e., concentration polarization and frictional
608 pressure drop) since these are more significant in a full-scale multistage process than a single-
609 stage one. Overall, new findings of this study are listed as below:

- 610 • Retentate recycle flows sufficiently increased the feed flow rates of Stage 1 NF
611 and Stage 2 RO and reduced concentration difference across the membrane,
612 thereby lowering the OPD for CMCR stages. The degree of changes in the feed
613 flow rate and concentration is influenced by the retentate recycle ratio.
- 614 • For the 1-2 EERO process, energy efficiency is highly reliant on retentate recycle
615 ratio. The recycle ratio, particularly for 45% recovery of SSRO stage was optimum
616 at 0.8, 0.6, and 0.4 corresponding to 35, 45, and 55% recoveries of Stage 2 RO,
617 respectively. In addition, SEC increased significantly under the condition smaller
618 and greater than the optimum ratio. This could be attributed to that such a ratio has
619 an influence on the work rate done by the ancillary equipment such as ERD and
620 BPs.
- 621 • We found an optimal water recovery to minimize SEC of the 1-2 EERO process in
622 the presence of ERD: an overall recovery of ~42% with a recovery of 28.3% and
623 49% for SSRO stage and Stage 2 RO, respectively.
- 624 • The 1-2 EERO process can outperform a conventional SSRO process for high
625 overall recovery of $\geq 55\%$ with a decent quality (< 220 mg/L) of the final product

626 water; The EERO process optimized here not only decreased SEC at high water
627 recovery, but also yielded lower potentials of membrane fouling and CP due to
628 reduced permeate flux in the lead elements in SSRO stage and Stage 2 RO.

629 • NF module design had a larger impact on the improvement in energy efficiency
630 for the 1-2 EERO process, than the retentate recycle. The NF stage, therefore,
631 needed be designed in accordance with a criterion of the optimum salt rejection for
632 target recovery: for overall recovery of 60%, a NF module of 70% salt rejection
633 had the lowest SEC_{norm} among the ones in the range of 60 – 90% salt rejections. In
634 this regard, ISD was useful for effectively designing the NF module, because it
635 could be adjusted to the optimum rejection through a hybrid configuration of
636 different NF membranes in a pressure vessel.

637 The numerical model developed here can be a reliable assessment tool, which can help
638 process engineers' decision-making for design and operation of a 1-2 EERO system. In addition,
639 it is also expected that the proposed modeling approach would be a good reference for a
640 modeling of a multi-stage membrane process with CMCR. Lastly, as shown in the work, the
641 NF stage plays a critical role in determining the efficiency of the EERO system. Thus, robust
642 NF membranes such as greater maximum operating pressure (i.e. most of current commercial
643 NF membranes are limited to 41 bar) and wider rejection range are required.

644

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651 **Nomenclature**

$C_{\text{module}}^{\text{p}}$	permeate concentration of a single membrane module (mg/L)
c	concentration (mg/L)
D	diffusion coefficient of solute (m^2/s)
d_{h}	hydraulic diameter (m)
H	channel height (m)
J_{s}	salt flux ($\text{kg}/\text{m}^2 \text{ s}$)
J_{w}	permeate flux (m/s)
K	friction coefficient
k	mass transfer coefficient (m/s)
L	channel length (m)
L_{p}	water permeability coefficient ($\text{L}/\text{m}^2 \text{ h bar}$)
M	molecular weight (g/mol)
N	total number
N_{ion}	ionization number of the solution
P	inlet and outlet flow pressure (bar)
p	pressure (bar)
P_{s}	salt permeability coefficient ($\text{L}/\text{m}^2 \text{ h}$)
Q	inlet and outlet volumetric flow rate (m^3/d)
$Q_{\text{module}}^{\text{p}}$	permeate flow rate of a single membrane module (m^3/d)
R_{g}	ideal gas constant ($\text{cm}^3 \text{ bar}/\text{mol K}$)
Re	Reynolds number
Sc	Schmidt number
SEC	specific energy consumption ($\text{kW h}/\text{m}^3$)

Sh	Sherwood number
T	absolute temperature (K)
TL	total length of flow channel in a pressure vessel (m)
u	cross-flow velocity (m/s)
V	volume (m ³)
W	channel width (m)
\dot{W}	rate of work done (KJ/d)
x	coordinate in channel length direction
Y	water recovery

Greek Symbols

ϵ_{sp}	effective porosity of flow channel created by feed spacer
η	equipment efficiency
μ	dynamic viscosity (Pa s)
ν	kinematic viscosity (m ² /s)
π	osmotic pressure (bar)
σ	reflection coefficient

Subscripts and Superscripts

BPs	booster pumps
b	bulk
E	membrane element
ERD	energy recovery device
elec	electricity
f	feed flow to SSRO stage
HPP	high pressure pump
L	membrane leaf

M	membrane module
m	membrane wall (active layer surface)
NF	nanofiltration
norm	normalized to the feed osmotic pressure
overall	total quantity
p	permeate
pe	primary energy
RO	reverse osmosis
SSRO	single-stage reverse osmosis
STG2	stage 2
s	salt
sw	saltwater
w	water
0	influent (feed)

652

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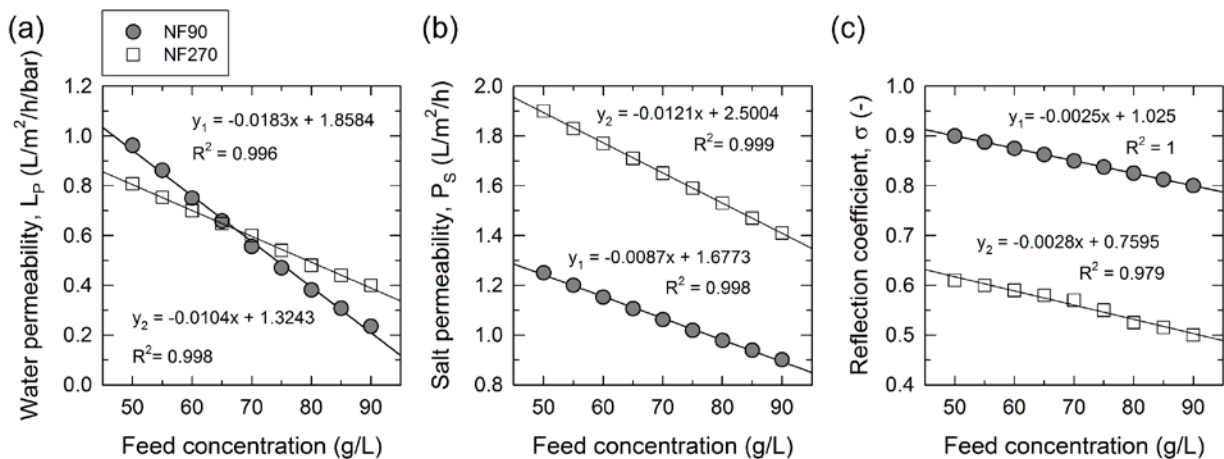
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728

729 **Appendix A. Estimation of intrinsic transport properties of a commercial NF membrane**

730 From the literature [24, 34, 35], it was reported that the membrane transport coefficients
 731 of NF membranes are strongly dependent on the feed concentration of electrolyte solutions,
 732 due to electrostatic interactions between the charged membrane and ions in the solution [34].
 733 They experimentally confirmed the concentration-dependent relations of those parameters, and
 734 further demonstrated it theoretically using membrane transport models. However, it is
 735 challenging to fully describe the behavior of those parameters for various NF membranes with
 736 the wide range of feed concentrations using simple mathematical equations. Therefore, we
 737 believe that the empirical relationship we obtained here (Fig. A1) is sufficient to accurately
 738 estimate the values of the transport coefficients for commercial NF membranes, NF90 and
 739 NF270. It can further allow a successful prediction of the NF module performance in Stage 1
 740 for high feed concentrations as saline as seawater reverse osmosis (SWRO) brine.

741



743 Fig. A1. Empirical linear correlations between the feed solute concentration and intrinsic
 744 transport properties for commercial nanofiltration membranes.

745

746 To obtain the empirical linear equations (shown in Fig. A1), we numerically estimated

747 the values of the water and salt permeability coefficients (L_p and P_s) and the reflection
748 coefficient (σ) by fitting these parameters versus the feed concentration. The value of each
749 individual parameter at a single point of the feed concentration was computed by a best fitting
750 method to minimize an error value (an average error of 2.0%) between the simulated and
751 projected data. Specifically, the ROSA9 software evaluated the permeate flow rates and salt
752 concentrations of the NF90 and NF270 membranes. These performance data were obtained for
753 feed concentrations of 50 – 90 g/L at 5 g/L intervals with a feed pressure of 65 bar, which is
754 normal operating conditions for NF module in the 1-2 EERO process. The parameters L_p , P_s ,
755 and σ were computed using a series of Eqs. (11) – (18) and the performance data obtained at
756 an given condition. With the empirical linear correlations, the developed model provided
757 accurate predictions of permeate flow rates and permeate concentrations of a single membrane
758 module under various conditions of the feed concentration and pressure (see Fig. 3).